

Appendix

1. Code

1.1 C code

1.1.1 C code to implement the adaptation algorithm and generate a Markov Chain (Example 1~3)

1.1.2 C code to implement the adaptation algorithm and generate a Markov Chain (Example 4)

1.2 R code

1.2.1 R code to plot the final $g(X)$ and $\sigma(X)$ (Example 1~3)

1.2.2 R code to plot the final $g(X)$ and $\sigma(X)$ (Example 4)

1.2.3 R code to generate Markov Chain without adaption (Example 1)

1.2.4 R code to generate Markov Chain without adaption (Example 2)

1.2.5 R code to generate Markov Chain without adaption (Example 3)

1.2.6 R code to generate Markov Chain without adaption (Example 4)

1.2.7 R code to compute different efficiency measures (Example 1~3)

1.2.8 R code to compute different efficiency measures (Example 4)

1.2.9 R code to implement OLS in approximation of the final $\sigma(X)$

2. Output

2.1 Example 1: normal distribution in \mathcal{R}^1

2.1.1 kernel function $K(x) = e^{-\frac{|x|^{\alpha_1}}{\alpha_2}}$

2.1.1.1 case 1 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.1.1.2 case 2 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.1.1.3 case 3 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.1.1.4 case 4 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.1.1.5 case 5 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.5, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.1.1.6 case 6 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 2, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.1.1.7 case 7 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 10, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.1.1.8 case 8 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.1.1.9 case 9 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.5, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.1.1.10 case 10 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.01, \gamma = 2$ with fixed bandwidth

$b_n = 1$

2.1.1.11 case 11 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 10$ with fixed bandwidth

$b_n = 1$

2.1.1.12 case 12 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 0.5$ with fixed bandwidth

$b_n = 1$

2.1.1.13 case 13 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 1$ with fixed bandwidth

$b_n = 1$

2.1.1.14 case 14 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 0.1$ with fixed bandwidth

$b_n = 1$

2.1.1.15 case 15 $\eta_n = \frac{1}{(n+5)^{0.8}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$$b_n = 1$$

2.1.1.16 case 16 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$$b_n = 10$$

2.1.1.17 case 17 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$$b_n = 0.1$$

2.1.1.18 case 18 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with decreasing

bandwidth $b_n = \frac{1}{n^{0.2}}$

2.1.2 kernel function $K(x) = \frac{1}{1 + \alpha_1 |x|^{\alpha_2}}$

2.1.2.1 case 19 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.1.2.2 case 20 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.1.2.3 case 21 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth

$$b_n = 1$$

2.1.2.4 case 22 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 10, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.1.2.5 case 23 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$$b_n = 1$$

2.1.2.6 case 24 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.01, \gamma = 2$ with fixed bandwidth

$$b_n = 1$$

2.1.2.7 case 25 $\eta_n = \frac{1}{(n+5)^{0.5}}, \alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 1$ with fixed bandwidth $b_n = 1$

2.1.2.8 case 26 $\eta_n = \frac{1}{(n+5)^{0.5}}, \alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 10$ with fixed bandwidth

$$b_n = 1$$

2.1.2.9 case 27 $\eta_n = \frac{1}{(n+5)^{0.5}}, \alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$$b_n = 10$$

2.1.2.10 case 28 $\eta_n = \frac{1}{(n+5)^{0.5}}, \alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$$b_n = 0.1$$

2.1.2.11 case 29 $\eta_n = \frac{1}{(n+5)^{0.5}}, \alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 0.1$ with fixed bandwidth

$$b_n = 10$$

2.1.2.12 case 30 $\eta_n = \frac{1}{(n+5)^{0.5}}, \alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 2$ with decreasing bandwidth

$$b_n = \frac{1}{n^{0.2}}$$

2.1.2.13 case 31 $\eta_n = \frac{1}{(n+5)^{0.8}}, \alpha_1 = 0.1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth

$$b_n = 10$$

2.1.3 kernel function
$$K(x) = \begin{cases} 0, & |x| \geq 2 * width \\ -1 * height, & width < |x| < 2 * width \\ 1 * height, & |x| \leq width \end{cases}$$

2.1.3.1 case 32 $\eta_n = \frac{1}{(n+5)^{0.5}}, height = 0.5, width = 0.5, C = 1, \gamma = 2$ with fixed

bandwidth $b_n = 1$

2.1.3.2 case 33 $\eta_n = \frac{1}{(n+5)^{0.5}}$, *height* = 0.5, *width* = 0.5, $C = 10, \gamma = 2$ with fixed

bandwidth $b_n = 1$

2.1.3.3 case 34 $\eta_n = \frac{1}{(n+5)^{0.5}}$, *height* = 0.5, *width* = 0.5, $C = 0.1, \gamma = 2$ with fixed

bandwidth $b_n = 1$

2.1.3.4 case 35 $\eta_n = \frac{1}{(n+5)^{0.5}}$, *height* = 0.5, *width* = 0.5, $C = 0.01, \gamma = 2$ with fixed

bandwidth $b_n = 1$

2.1.3.5 case 36 $\eta_n = \frac{1}{(n+5)^{0.5}}$, *height* = 0.5, *width* = 0.5, $C = 0, \gamma = 2$ with fixed

bandwidth $b_n = 1$

2.1.3.6 case 37 $\eta_n = \frac{1}{(n+5)^{0.5}}$, *height* = 0.5, *width* = 0.5, $C = 0.001, \gamma = 2$ with fixed

bandwidth $b_n = 1$

2.1.3.7 case 38 $\eta_n = \frac{1}{(n+5)^{0.5}}$, *height* = 0.5, *width* = 0.5, $C = 0.001, \gamma = 10$ with fixed

bandwidth $b_n = 1$

2.1.3.8 case 39 $\eta_n = \frac{1}{(n+5)^{0.5}}$, *height* = 0.5, *width* = 0.5, $C = 0.001, \gamma = 1$ with fixed

bandwidth $b_n = 1$

2.1.3.9 case 40 $\eta_n = \frac{1}{(n+5)^{0.5}}$, *height* = 0.5, *width* = 0.5, $C = 0.001, \gamma = 0.1$ with fixed

bandwidth $b_n = 1$

2.1.3.10 case 41 $\eta_n = \frac{1}{(n+5)^{0.5}}$, *height* = 1, *width* = 0.5, $C = 0.01, \gamma = 2$ with fixed

bandwidth $b_n = 1$

2.1.3.11 case 42 $\eta_n = \frac{1}{(n+5)^{0.5}}$, *height* = 10, *width* = 0.5, $C = 0.01, \gamma = 2$ with fixed

bandwidth $b_n = 1$

2.1.3.12 case 43 $\eta_n = \frac{1}{(n+5)^{0.5}}$, *height* = 0.1, *width* = 0.5, $C = 0.01, \gamma = 2$ with fixed

bandwidth $b_n = 1$

2.1.3.13 case 44 $\eta_n = \frac{1}{(n+5)^{0.5}}$, *height* = 0.5, *width* = 2, $C = 0.01, \gamma = 2$ with fixed

bandwidth $b_n = 1$

2.1.3.14 case 45 $\eta_n = \frac{1}{(n+5)^{0.5}}$, *height* = 0.5, *width* = 5, $C = 0.01, \gamma = 2$ with fixed

bandwidth $b_n = 1$

2.1.3.15 case 46 $\eta_n = \frac{1}{(n+5)^{0.5}}$, *height* = 0.5, *width* = 0.1, $C = 0.01, \gamma = 2$ with fixed

bandwidth $b_n = 1$

2.1.3.16 case 47 $\eta_n = \frac{1}{(n+5)^{0.5}}$, *height* = 0.5, *width* = 0.5, $C = 0.01, \gamma = 2$ with fixed

bandwidth $b_n = 10$

2.1.3.17 case 48 $\eta_n = \frac{1}{(n+5)^{0.5}}$, *height* = 0.5, *width* = 0.5, $C = 0.01, \gamma = 2$ with fixed

bandwidth $b_n = 0.1$

2.1.3.18 case 49 $\eta_n = \frac{1}{(n+5)^{0.5}}$, *height* = 0.5, *width* = 0.5, $C = 0.01, \gamma = 2$ with

decreasing bandwidth $b_n = \frac{1}{n^{0.2}}$

2.1.3.19 case 50 $\eta_n = \frac{1}{(n+5)^{0.8}}$, *height* = 0.5, *width* = 0.5, $C = 0.01, \gamma = 2$ with fixed

bandwidth $b_n = 1$

2.1.4 kernel function $K(x) = \begin{cases} 0, & |x| \geq 2 * width \text{ or } |x| \leq width \\ 1, & width < |x| < 2 * width \end{cases}$

2.1.4.1 case 51 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.1.4.2 case 52 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C = 10, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.1.4.3 case 53 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C = 0.1, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.1.4.4 case 54 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C = 0.01, \gamma = 2$ with fixed bandwidth

$b_n = 1$

2.1.4.5 case 55 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C = 0.001, \gamma = 2$ with fixed bandwidth

$b_n = 1$

2.1.4.6 case 56 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 1, $C = 0.01, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.1.4.7 case 57 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 5, $C = 0.01, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.1.4.8 case 58 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.1, $C = 0.01, \gamma = 2$ with fixed bandwidth

$b_n = 1$

2.1.4.9 case 59 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 8, $C = 0.01, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.1.4.10 case 60 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 5, $C = 0.01, \gamma = 5$ with fixed bandwidth $b_n = 1$

2.1.4.11 case 61 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 5, $C = 0.01, \gamma = 1$ with fixed bandwidth $b_n = 1$

2.1.4.12 case 62 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 5, $C = 0.01, \gamma = 0.1$ with fixed bandwidth

$$b_n = 1$$

2.1.4.13 case 63 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 5, $C = 0.01, \gamma = 2$ with fixed bandwidth

$$b_n = 10$$

2.1.4.14 case 64 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 5, $C = 0.01, \gamma = 2$ with fixed bandwidth

$$b_n = 0.1$$

2.1.4.15 case 65 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 5, $C = 0.01, \gamma = 2$ with decreasing bandwidth

$$b_n = \frac{1}{n^{0.2}}$$

2.1.4.16 case 66 $\eta_n = \frac{1}{(n+5)^{0.8}}$, width = 5, $C = 0.01, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.1.5 constant $\sigma(x) = C$

2.1.6 varfact comparison

2.1.7 variance comparison

2.1.8 comparison of average squared jump distance

2.1.9 OLS in approximation of the final $\sigma(x)$

2.2 Example 2: mixture of two normal distributions in \mathbb{R}^1

2.2.1 kernel function $K(x) = e^{-\frac{|x|^{\alpha_1}}{\alpha_2}}$

2.2.1.1 case 67 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.2.1.2 case 68 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.2.1.3 case 69 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.2.1.4 case 70 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth

$$b_n = 1$$

$$2.2.1.5 \text{ case 71 } \eta_n = \frac{1}{(n+5)^{0.5}}, \alpha_1 = 0.5, \alpha_2 = 1, C = 1, \gamma = 2 \text{ with fixed bandwidth}$$

$$b_n = 1$$

$$2.2.1.6 \text{ case 72 } \eta_n = \frac{1}{(n+5)^{0.5}}, \alpha_1 = 0.01, \alpha_2 = 1, C = 1, \gamma = 2 \text{ with fixed bandwidth}$$

$$b_n = 1$$

$$2.2.1.7 \text{ case 73 } \eta_n = \frac{1}{(n+5)^{0.5}}, \alpha_1 = 2, \alpha_2 = 1, C = 10, \gamma = 2 \text{ with fixed bandwidth}$$

$$b_n = 1$$

$$2.2.1.8 \text{ case 74 } \eta_n = \frac{1}{(n+5)^{0.5}}, \alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2 \text{ with fixed bandwidth}$$

$$b_n = 1$$

$$2.2.1.9 \text{ case 75 } \eta_n = \frac{1}{(n+5)^{0.5}}, \alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 10 \text{ with fixed bandwidth}$$

$$b_n = 1$$

$$2.2.1.10 \text{ case 76 } \eta_n = \frac{1}{(n+5)^{0.5}}, \alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 1 \text{ with fixed bandwidth}$$

$$b_n = 1$$

$$2.2.1.11 \text{ case 77 } \eta_n = \frac{1}{(n+5)^{0.5}}, \alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 0.1 \text{ with fixed bandwidth}$$

$$b_n = 1$$

$$2.2.1.12 \text{ case 78 } \eta_n = \frac{1}{(n+5)^{0.5}}, \alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2 \text{ with fixed bandwidth}$$

$$b_n = 10$$

$$2.2.1.13 \text{ case 79 } \eta_n = \frac{1}{(n+5)^{0.5}}, \alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2 \text{ with fixed bandwidth}$$

$$b_n = 0.1$$

2.2.1.14 case 80 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with decreasing

bandwidth $b_n = \frac{1}{n^{0.2}}$

2.2.1.15 case 81 $\eta_n = \frac{1}{(n+5)^{0.8}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$$b_n = 10$$

2.2.2 kernel function $K(x) = \frac{1}{1 + \alpha_1 |x|^{\alpha_2}}$

2.2.2.1 case 90 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.2.2.2 case 91 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.2.2.3 case 92 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth

$$b_n = 1$$

2.2.2.4 case 93 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 12, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.2.2.5 case 94 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 5, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.2.2.6 case 95 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 1, \gamma = 10$ with fixed bandwidth

$$b_n = 1$$

2.2.2.7 case 96 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 1, \gamma = 0.1$ with fixed bandwidth

$$b_n = 1$$

2.2.2.8 case 97 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 10, \gamma = 0.1$ with fixed bandwidth

$$b_n = 1$$

2.2.2.9 case 98 $\eta_n = \frac{1}{(n+5)^{0.5}}, \alpha_1 = 10, \alpha_2 = 1, C = 0.1, \gamma = 0.1$ with fixed bandwidth

$$b_n = 1$$

2.2.2.10 case 99 $\eta_n = \frac{1}{(n+5)^{0.5}}, \alpha_1 = 10, \alpha_2 = 1, C = 0.1, \gamma = 0.1$ with fixed bandwidth

$$b_n = 10$$

2.2.2.11 case 100 $\eta_n = \frac{1}{(n+5)^{0.5}}, \alpha_1 = 10, \alpha_2 = 1, C = 0.1, \gamma = 0.1$ with fixed bandwidth

$$b_n = 0.1$$

2.2.2.12 case 101 $\eta_n = \frac{1}{(n+5)^{0.5}}, \alpha_1 = 10, \alpha_2 = 1, C = 0.1, \gamma = 0.1$ with decreasing

bandwidth $b_n = \frac{1}{n^{0.2}}$

2.2.2.13 case 102 $\eta_n = \frac{1}{(n+5)^{0.8}}, \alpha_1 = 10, \alpha_2 = 1, C = 0.1, \gamma = 0.1$ with fixed bandwidth

$$b_n = 1$$

2.2.3 kernel function
$$K(x) = \begin{cases} 0, & |x| \geq 2 * width \\ -1 * height, & width < |x| < 2 * width \\ 1 * height, & |x| \leq width \end{cases}$$

2.2.3.1 case 103 $\eta_n = \frac{1}{(n+5)^{0.5}}, C = 1, \gamma = 2, height = 0.5, width = 0.5,$ with fixed

bandwidth $b_n = 1$

2.2.3.2 case 104 $\eta_n = \frac{1}{(n+5)^{0.5}}, C = 10, \gamma = 2, height = 0.5, width = 0.5,$ with fixed

bandwidth $b_n = 1$

2.2.3.3 case 105 $\eta_n = \frac{1}{(n+5)^{0.5}}, C = 0.1, \gamma = 2, height = 0.5, width = 0.5,$ with fixed

bandwidth $b_n = 1$

2.2.3.4 case 106 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 10, \text{height} = 0.5, \text{width} = 0.5$, with fixed

bandwidth $b_n = 1$

2.2.3.5 case 107 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{height} = 0.5, \text{width} = 0.5$, with fixed

bandwidth $b_n = 1$

2.2.3.6 case 108 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 2, \text{height} = 1, \text{width} = 0.5$, with fixed

bandwidth $b_n = 1$

2.2.3.7 case 109 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 2, \text{height} = 5, \text{width} = 0.5$, with fixed

bandwidth $b_n = 1$

2.2.3.8 case 110 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 2, \text{height} = 0.1, \text{width} = 0.5$, with fixed

bandwidth $b_n = 1$

2.2.3.9 case 111 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 1, \gamma = 0.1, \text{height} = 1, \text{width} = 1$, with fixed

bandwidth $b_n = 1$

2.2.3.10 case 112 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{height} = 1, \text{width} = 5$, with fixed

bandwidth $b_n = 1$

2.2.3.11 case 113 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{height} = 1, \text{width} = 0.1$, with fixed

bandwidth $b_n = 1$

2.2.3.12 case 114 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{height} = 1, \text{width} = 0.1$, with fixed

bandwidth $b_n = 10$

2.2.3.13 case 115 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{height} = 1, \text{width} = 0.1$, with fixed

bandwidth $b_n = 0.1$

2.2.3.14 case 116 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{height} = 1, \text{width} = 0.1$, with

decreasing bandwidth $b_n = \frac{1}{n^{0.2}}$

2.2.3.15 case 117 $\eta_n = \frac{1}{(n+5)^{0.8}}$, $C = 0.1, \gamma = 0.1, \text{height} = 1, \text{width} = 0.1$, with

decreasing bandwidth $b_n = \frac{1}{n^{0.2}}$

2.2.4 kernel function $K(x) = \begin{cases} 0, & |x| \geq 2 * \text{width} \text{ or } |x| \leq \text{width} \\ 1, & \text{width} < |x| < 2 * \text{width} \end{cases}$

2.2.4.1 case 118 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 1, \gamma = 2, \text{width} = 0.5$, with fixed bandwidth $b_n = 1$

2.2.4.2 case 119 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 2, \text{width} = 0.5$, with fixed bandwidth

$b_n = 1$

2.2.4.3 case 120 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 10, \gamma = 2, \text{width} = 0.5$, with fixed bandwidth

$b_n = 1$

2.2.4.4 case 121 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 10, \text{width} = 0.5$, with fixed bandwidth

$b_n = 1$

2.2.4.5 case 122 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{width} = 0.5$, with fixed bandwidth

$b_n = 1$

2.2.4.6 case 123 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{width} = 1$, with fixed bandwidth

$$b_n = 1$$

2.2.4.7 case 124 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{width} = 2$, with fixed bandwidth

$$b_n = 1$$

2.2.4.8 case 125 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{width} = 5$, with fixed bandwidth

$$b_n = 1$$

2.2.4.9 case 126 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{width} = 0.2$, with fixed bandwidth

$$b_n = 1$$

2.2.4.10 case 127 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{width} = 0.2$, with fixed bandwidth

$$b_n = 10$$

2.2.4.11 case 128 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{width} = 0.2$, with fixed bandwidth

$$b_n = 0.1$$

2.2.4.12 case 127 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{width} = 0.2$, with decreasing

bandwidth $b_n = \frac{1}{n^{0.2}}$

2.2.4.13 case 128 $\eta_n = \frac{1}{(n+5)^{0.8}}$, $C = 0.1, \gamma = 0.1, \text{width} = 0.2$, with fixed bandwidth

$$b_n = 1$$

2.2.5 constant $\sigma(x) = C$

2.2.6 varfact comparison

2.2.7 variance comparison

2.2.8 comparison of average squared jump distance

2.3 Example 3: mixture of three normal distributions in \mathcal{R}^1

2.3.1 kernel function $K(x) = e^{-\frac{|x|^{\alpha_1}}{\alpha_2}}$

2.3.1.1 case 129 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth

$$b_n = 1$$

2.3.1.2 case 130 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth

$$b_n = 1$$

2.3.1.3 case 131 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth

$$b_n = 1$$

2.3.1.4 case 132 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 0.5$ with fixed bandwidth

$$b_n = 1$$

2.3.1.5 case 131 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 1, \gamma = 0.5$ with fixed bandwidth

$$b_n = 1$$

2.3.1.6 case 132 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 1, \gamma = 0.5$ with fixed bandwidth

$$b_n = 1$$

2.3.1.7 case 133 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 10, \gamma = 0.5$ with fixed bandwidth

$$b_n = 1$$

2.3.1.8 case 134 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 10, \gamma = 0.5$ with fixed bandwidth

$$b_n = 1$$

2.3.1.9 case 135 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 0.1, \gamma = 0.5$ with fixed bandwidth

$$b_n = 1$$

2.3.1.10 case 136 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 10$

2.3.1.11 case 137 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 0.1$

2.3.1.12 case 138 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 1, \gamma = 0.5$ with decreasing

bandwidth $b_n = \frac{1}{n^{0.2}}$

2.3.1.13 case 139 $\eta_n = \frac{1}{(n+5)^{0.8}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 1, \gamma = 0.5$ with fixed bandwidth

$$b_n = 1$$

2.3.2 kernel function $K(x) = \frac{1}{1 + \alpha_1 |x|^{\alpha_2}}$

2.3.2.1 case 140 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.3.2.2 case 141 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth

$$b_n = 1$$

2.3.2.3 case 142 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth

$$b_n = 1$$

2.3.2.4 case 143 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$$b_n = 1$$

2.3.2.5 case 144 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 10, \gamma = 2$ with fixed bandwidth

$$b_n = 1$$

2.3.2.6 case 145 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 0.5$ with fixed bandwidth

$$b_n = 1$$

2.3.2.7 case 146 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 1, \gamma = 0.5$ with fixed bandwidth

$$b_n = 1$$

2.3.2.8 case 147 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 1, \gamma = 0.5$ with fixed bandwidth

$$b_n = 1$$

2.3.2.9 case 148 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 10, \gamma = 0.5$ with fixed bandwidth

$$b_n = 1$$

2.3.2.10 case 149 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 0.1, \gamma = 0.5$ with fixed bandwidth

$$b_n = 1$$

2.3.2.11 case 150 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 10, \gamma = 0.1$ with fixed bandwidth

$$b_n = 1$$

2.3.2.12 case 151 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 10, \gamma = 1$ with fixed bandwidth

$$b_n = 1$$

2.3.2.13 case 152 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 10, \gamma = 0.5$ with fixed bandwidth

$$b_n = 10$$

2.3.2.14 case 153 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 10, \gamma = 0.5$ with fixed bandwidth

$$b_n = 0.1$$

2.3.2.15 case 154 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 10, \gamma = 0.5$ with decreasing

bandwidth $b_n = \frac{1}{n^{0.2}}$

2.3.2.16 case 155 $\eta_n = \frac{1}{(n+5)^{0.8}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 10, \gamma = 0.5$ fixed bandwidth

$$b_n = 1$$

2.3.3 kernel function
$$K(x) = \begin{cases} 0, & |x| \geq 2 * width \\ -1 * height, & width < |x| < 2 * width \\ 1 * height, & |x| \leq width \end{cases}$$

2.3.3.1 case 156 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.5, width = 0.5, $C = 1, \gamma = 2$ with fixed

bandwidth $b_n = 1$

2.3.3.2 case 157 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.5, width = 0.5, $C = 10, \gamma = 2$ with fixed

bandwidth $b_n = 1$

2.3.3.3 case 158 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.5, width = 0.5, $C = 0.1, \gamma = 2$ with fixed

bandwidth $b_n = 1$

2.3.3.4 case 159 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 2, width = 0.5, $C = 0.1, \gamma = 2$ with fixed

bandwidth $b_n = 1$

2.3.3.5 case 160 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.5, width = 2, $C = 0.1, \gamma = 2$ with fixed

bandwidth $b_n = 1$

2.3.3.6 case 161 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.5, width = 0.5, $C = 1, \gamma = 0.5$ with fixed

bandwidth $b_n = 1$

2.3.3.7 case 162 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.5, width = 0.5, $C = 10, \gamma = 0.5$ with fixed

bandwidth $b_n = 1$

2.3.3.8 case 163 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.5, width = 0.5, $C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 1$

2.3.3.9 case 164 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 2, width = 0.5, $C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 1$

2.3.3.10 case 165 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 5, width = 0.5, $C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 1$

2.3.3.11 case 166 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 10, width = 0.5, $C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 1$

2.3.3.12 case 167 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.1, width = 0.5, $C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 1$

2.3.3.13 case 168 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.1, width = 2, $C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 1$

2.3.3.14 case 169 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.1, width = 8, $C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 1$

2.3.3.15 case 170 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.1, width = 15, $C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 1$

2.3.3.16 case 171 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.1, width = 0.1, $C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 1$

2.3.3.17 case 172 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.1, width = 2, $C = 0.1, \gamma = 0.1$ with fixed

bandwidth $b_n = 1$

2.3.3.18 case 173 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.1, width = 2, $C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 10$

2.3.3.19 case 174 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.1, width = 2, $C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 0.1$

2.3.3.20 case 175 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.1, width = 2, $C = 0.1, \gamma = 0.5$ with

decreasing bandwidth $b_n = \frac{1}{n^{0.2}}$

2.3.3.21 case 176 $\eta_n = \frac{1}{(n+5)^{0.8}}$, height = 0.1, width = 2, $C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 1$

2.3.4 kernel function $K(x) = \begin{cases} 0, & |x| \geq 2 * width \text{ or } |x| \leq width \\ 1, & width < |x| < 2 * width \end{cases}$

2.3.4.1 case 177 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C=1, \gamma=2$ with fixed bandwidth $b_n = 1$

2.3.4.2 case 178 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C=10, \gamma=2$ with fixed bandwidth $b_n = 1$

2.3.4.3 case 179 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C=0.1, \gamma=2$ with fixed bandwidth
 $b_n = 1$

2.3.4.4 case 180 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 2, $C=1, \gamma=2$ with fixed bandwidth $b_n = 1$

2.3.4.5 case 181 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.1, $C=1, \gamma=2$ with fixed bandwidth $b_n = 1$

2.3.4.6 case 182 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C=1, \gamma=0.5$ with fixed bandwidth
 $b_n = 1$

2.3.4.7 case 183 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C=10, \gamma=0.5$ with fixed bandwidth
 $b_n = 1$

2.3.4.8 case 184 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C=0.1, \gamma=0.5$ with fixed bandwidth
 $b_n = 1$

2.3.4.9 case 185 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 2, $C=1, \gamma=0.5$ with fixed bandwidth $b_n = 1$

2.3.4.10 case 186 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 8, $C=1, \gamma=0.5$ with fixed bandwidth $b_n = 1$

2.3.4.11 case 187 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 15, $C=1, \gamma=0.5$ with fixed bandwidth
 $b_n = 1$

2.3.4.12 case 189 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.1, $C=1, \gamma=0.5$ with fixed bandwidth

$$b_n = 1$$

2.3.4.13 case 190 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C=1, \gamma=0.5$ with fixed bandwidth

$$b_n = 10$$

2.3.4.14 case 191 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C=1, \gamma=0.5$ with fixed bandwidth

$$b_n = 0.1$$

2.3.4.15 case 192 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C=1, \gamma=0.5$ with decreasing bandwidth

$$b_n = \frac{1}{n^{0.2}}$$

2.3.4.16 case 193 $\eta_n = \frac{1}{(n+5)^{0.8}}$, width = 0.5, $C=1, \gamma=0.5$ with fixed bandwidth

$$b_n = 1$$

2.3.5 constant $\sigma(x) = C$

2.3.6 varfact comparison

2.3.7 variance comparison

2.3.8 comparison of average squared jump distance

2.4 Example 4: normal distribution in R^2

2.4.1 kernel function $K(x) = e^{-\frac{|x|^{\alpha_1}}{\alpha_2}}$

2.4.1.1 case 194 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C=1, \gamma=2$ with fixed bandwidth $b_n = 1$

2.4.1.2 case 195 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.5, \alpha_2 = 1, C=1, \gamma=2$ with fixed bandwidth

$$b_n = 1$$

2.4.1.3 case 196 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.5, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$$b_n = 1$$

2.4.1.4 case 197 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$$b_n = 1$$

2.4.2 kernel function $K(x) = \frac{1}{1 + \alpha_1 |x|^{\alpha_2}}$

2.4.2.1 case 198 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.4.2.2 case 199 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 1$ with fixed bandwidth

$$b_n = 1$$

2.4.2.3 case 200 $\eta_n = \frac{1}{(n+5)^{0.8}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$$b_n = 10$$

2.4.3 kernel function $K(x) = \begin{cases} 0, & |x| \geq 2 * width \\ -1 * height, & width < |x| < 2 * width \\ 1 * height, & |x| \leq width \end{cases}$

2.4.3.1 case 201 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $height = 0.5, width = 0.5, C = 0.01, \gamma = 10$ with fixed

bandwidth $b_n = 1$

2.4.4 kernel function $K(x) = \begin{cases} 0, & |x| \geq 2 * width \text{ or } |x| \leq width \\ 1, & width < |x| < 2 * width \end{cases}$

2.4.4.1 case 202 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $width = 5, C = 0.01, \gamma = 2$ with fixed bandwidth $b_n = 1$

2.4.5 constant $\sigma(x) = C$

2.4.6 varfact comparison

2.4.7 variance comparison

2.4.8 comparison of average squared jump distance

Appendix

1. Code

1.1 C code

1.1.1 C code to implement the adaptation algorithm and generate a Markov Chain (Example 1~3)

```
#include <stdio.h>
#include <stdlib.h>
#include <math.h>
#include <sys/time.h>

#define RUNLENGTH 10000
#define PRINTSP 100
#define PI 3.1415926536
#define N 10000
#define M 100000
#define B 10000
#define numsig 16000
#define left -30
#define right 30
#define gap 0.01

#define m0 0x100000000LL
#define c0 0xB16
#define a0 0x5DEECE66DLL

double alpha1,alpha2,bn, beta, C, ggamma;
double height, width;
double x[RUNLENGTH],xlist[M];
int accept[RUNLENGTH],addsign[RUNLENGTH];
double appg[numsig],appsig[numsig];

int main()
{
    int i, n, numacc;
    double X, Y, U;
    FILE *fpg, *fpx, *fpsig, *fpout, *fpxlist;
    clock_t start, end;
    double time1,time2,time3,time4;

    double normal();
```

```

double logpi(double);
double g(int, double);
double K(double);
double sigma(int, double), appsigma(double);
double logaccprob(int, double, double), applogaccprob(double, double);
void seedrand();
double mean(double xx[], int nn);
double a(double);
int divides(int, int);
double eta(int);
double sq(double);
int indicator(int);
double mean(double xx[], int nn);
double a(double);

```

```
seedrand();
```

```
/* Initial values. */
```

```

alpha1 = 10.0;
alpha2 = 1.0;
bn = 1.0; /*bandwidth*/
beta = 0.0; /*the initial value for beta*/
C = 1.0; /*one parameter in sigma*/
ggamma = 2.0; /*one parameter in sigma*/
height = 0.5; /*one parameter in the kernel function*/
width = 0.5; /*one parameter in the kernel function*/
X = 0.0;
numacc = 0;

```

```
printf("\nHere we go!\n\n");
```

```
/* Do the run. */
```

```

start = clock();
for (n=0; n<RUNLENGTH; n++) {
    Y = X + sigma(n, X) * normal();
    U = drand48();
    if ( log(U) < logaccprob(n, X, Y) ) {
        X = Y;
        accept[n] = 1;
        numacc++;
        beta = beta + 1.0/pow((n+5), 0.5)*(1.0-0.234);
    }
    else {
        accept[n] = 0;
    }
}

```

```

        beta = beta - 1.0/pow((n+5),0.5)*0.234;
    }
    if ( log(0.234) < logaccprob(n,X,Y) )
        addsign[n] = 1 ;
    else
        addsign[n] = -1 ;
    x[n] = X;
    /*bn = 1.0/pow(n,0.2);*/
    if (divides(PRINTSP,n))
        printf("n=%d, X=%f, Y=%f, K=%f,G=%f,sigma=%f, beta=%f, accept=%d\n",n,
X, Y, K(X),g(n,X),sigma(n,X),beta, accept[n]);
    }
    end = clock();
    time1 = (double) (end - start)/CLOCKS_PER_SEC;
    printf("Accepted %d out of %d (%.3f%%).\n", numacc, RUNLENGTH,
100.0*numacc/RUNLENGTH);
    printf("final beta = %f\n", beta);

    /*calculate g and sigma for some X*/
    start = clock();
    for(i=0;i<numsig;i++){
    X = left + i * gap;
    appg[i] = g(RUNLENGTH-1,X);
    appsig[i] = sigma(RUNLENGTH-1,X);
    }

    /*Plot the resulting g values to a file ... */
    printf("Writing gvals ... \n");
    if ((fpg = fopen("gvals", "w")) == NULL) {
    fprintf(stderr, "Unable to open output file 'gvals'.\n");
    exit(1);
    }
    fprintf(fpg, "gvals = c(");
    for (i=0; i<numsig; i++)
        fprintf(fpg, "%f,\n", appg[i]);
    fprintf(fpg, "%f)\n\n", appg[numsig-1]);
    fclose(fpg);

    /*Plot the resulting sigma values to a file ... */
    printf("Writing sigvals ... \n");
    if ((fpsig = fopen("sigvals", "w")) == NULL) {
    fprintf(stderr, "Unable to open output file 'sigvals'.\n");
    exit(1);
    }

```

```

fprintf(fpsig, "sigvals = c(");
for (i=0; i<numsig; i++) {
    fprintf(fpsig, "%f,\n", appsig[i]);
}
fprintf(fpsig, "%f)\n\n", appsig[numsig-1]);
end = clock();
time2 = (double) (end - start)/CLOCKS_PER_SEC;
fclose(fpsig);

/*Plot the resulting X values to a file ... */
printf("Writing xvals ... \n");
if ((fpx = fopen("xvals", "w")) == NULL) {
    fprintf(stderr, "Unable to open output file 'xvals'. \n");
    exit(1);
}
fprintf(fpx, "xvals = c(");
for (i=0; i<RUNLENGTH-1; i++)
    fprintf(fpx, "%f,\n", x[i]);
fprintf(fpx, "%f)\n\n", x[RUNLENGTH-1]);
fprintf(fpx, "hist(xvals)");
fclose(fpx);

/*generate a Markov chain with scale proposed by the algorithm*/
start = clock();
printf("generating Markov Chain ... \n");
xlist[0] = drand48()*15;
numacc = 0;
for(i=1; i<M; i++){
    X = xlist[i-1];
    Y = X + sigma(RUNLENGTH-1, X) * normal();
    U = drand48();
    if ( log(U) < logaccprob(RUNLENGTH-1, X, Y) ) {
        X = Y;
        numacc++;
    }
    xlist[i] = X;
}
printf("run the M-H algorithm for %d times, and acceptance rate is (%.3f%%).\n",
M, 100.0*numacc/M);

/*save the resulting xlist values to a file*/
printf("Writing xlist vals ... \n");
if ((fpxlist1 = fopen("xlist1", "w")) == NULL) {
    fprintf(stderr, "Unable to open output file 'xlist1'. \n");
}

```

```

exit(1);
}
fprintf(fpulist1, "xlist=c(");
for (i=0; i<(M-1); i++) {
    fprintf(fpulist1, "%f,\n", xlist[i]);
}
fprintf(fpulist1, "%f)\n\n", xlist[M-1]);
fclose(fpulist1);
end = clock();
time3 = (double) (end - start)/CLOCKS_PER_SEC;

/*test alpha(X) and save them to a file ... */
start = clock();
printf("Writing final vals ... \n");
if ((fpout = fopen("out", "w")) == NULL) {
    fprintf(stderr, "Unable to open output file 'out'.\n");
    exit(1);
}
fprintf(fpout, "Accepted %d out of %d (%.3f%%).\n", numacc, M, 100.0*numacc/M);
fprintf(fpout, "final beta = %f\n", beta);
/*for normal distribution in one dimension*/
X = 0;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
X = 2;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
X = 5;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
X = 10;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
X = 20;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
X = 50;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
X = 100;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
X = 150;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
/*for the mixture of two normal distributions in one dimension*/
/*X = 5;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
X = 7;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
X = 10;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
*/

```

```

X = 20;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
X = 30;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
X = 50;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
X = 70;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X)); */
/*for the mixture of three normal distributions in one dimension*/
/*X = 0;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
X = 2;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
X = 5;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
X = 8;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
X = 10;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
X = 13;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
X = 15;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
X = 20;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
X = 30;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X));
X = 50;
fprintf(fpout, "alpha(%f) is %f\n", X, a(X)); */
end = clock();
Time4 = (double) (end - start)/CLOCKS_PER_SEC;
fprintf(fpout, "it takes %f seconds to run the adaptation algorithm\n", time1);
fprintf(fpout, "it takes %f seconds to compute g and sigma\n", time2);
fprintf(fpout, "it takes %f seconds to generate the Markov Chain\n", time3);
fprintf(fpout, "it takes %f seconds to test the local acceptance\n", time4);
fclose(fpout);

printf("Done. \n");
return(0);
}

/* normal: return a standard normal random number. */
double normal()
{

```

```

    double R, theta, drand48();
    R = - log(drand48());
    theta = 2 * PI * drand48();
    return( sqrt(2*R) * cos(theta));
}

/* seedrand: seed random number generator. */
void seedrand()
{
    int seed;
    struct timeval tmptv;
    gettimeofday (&tmptv, (struct timezone *)NULL);
    seed = (int) tmptv.tv_usec;
    srand48(seed);
    (void)drand48(); /* Spin it once. */
}

/*divides: whether aa divides bb. If yes, return 1; otherwise return 0.*/
int divides(int aa, int bb)
{
    return( (bb/aa)*aa == bb );
}

/*logpi: compute logarithm of target distribution*/
/*for normal distribution in one dimension*/
double logpi(double xx)
{
    double sq();
    return( -sq(xx)/2.0 );
}

/*for the mixture of two normal distributions in one dimension*/
/*double logpi(double xx)
{
    double sq();
    if(xx<0.0) return (-sq(xx)/2.0);
    if(xx>10.0) return (-sq(xx-10.0)/2.0);
    return( log( exp(-sq(xx)/2.0) + exp(-sq(xx-10.0)/2.0) ) );
}*/

/*for the mixture of three normal distributions in one dimension*/
/*double logpi(double xx)
{
    double sq();
    if(xx<=-12) return (log(0.3)-sq(xx+10.0)/2.0);
    if(xx>12) return (log(0.3)-sq(xx-10.0)/2.0);
}*/

```

```

return(log(0.3*exp(-sq(xx+10.0)/2.0)+0.4*exp(-sq(xx)/2.0)+0.3*exp(-sq(xx-10.0)/2.0)));
}*/

```

```

/*g: function g*/

```

```

double g(int nn, double xx)

```

```

{

```

```

    int ii;

```

```

    double eta(),K(), val,abdif;

```

```

    val = 0.0;

```

```

    for (ii=0; ii<nn; ii++) {

```

```

        abdif = fabs(xx-x[ii]);

```

```

        val = (1.0 - eta(ii)) * val + eta(ii) * addsign[ii] / bn * K(abdif/bn);

```

```

    }

```

```

    return(val);

```

```

}

```

```

/*K: kernel function*/

```

```

double K(double xx)

```

```

{
    double abdif = fabs(xx);

```

```

    return

```

```

    ( exp(-pow(abdif,alpha1)/alpha2) );

```

```

    /*you can try other kernel function like: */

```

```

    /*( 1.0 / (1.0 + alpha1*pow( abdif, alpha2 ))); */

```

```

    /*height*( 2*indicator(abdif<width) -indicator(abdif<2*width) ); */

```

```

    /* indicator((abdif>=width)&&(abdif<2*width)); */

```

```

}

```

```

/*sigma: function sigma*/

```

```

double sigma(int nn, double xx)

```

```

{

```

```

    double g();

```

```

    /*for normal distribution in 1 dimension*/

```

```

    return( exp(beta) * pow(1.0 + C*fabs(xx), ggamma) * exp( g(nn,xx) ) );

```

```

    /*for the mixture of two normal distributions in 1 dimension*/

```

```

    /*return( exp(beta) * pow(1.0 + C*fabs(xx-5.0), ggamma) * exp( g(nn,xx) ) );*/

```

```

    /*for the mixture of three normal distributions in 1 dimension*/

```

```

    /*return(exp(beta)*pow(1.0+C*fabs(xx-5.0)*fabs(xx+5.0),ggamma)*exp( g(nn,xx) ) );*/

```

```

}

```

```

/*logaccprob: logarithm of acceptance probability from xx to yy*/

```

```

double logaccprob(int nn, double xx, double yy)

```

```

{

```

```

    double sigma(), sq();

```



```

return(logpi(yy)-logpi(xx)+log(sigma(nn,xx))-log(sigma(nn,yy))+sq(xx-yy)*(0.5/sq(sigma(n
n,xx))-0.5/sq(sigma(nn,yy))));
}

```

```

/*eta: function eta*/
double eta(int nn)
{
    return(1.0/pow((nn+5),0.5) );
    /*return(1.0/pow(nn+5,0.8) );*/
}

```

```

/*sq: compute the square of xx*/
double sq(double xx)
{
    return(xx*xx);
}

```

```

/*indicator: return 1/0 if the xx is non-zero/zero*/
int indicator(int xx)
{
    if (xx==0)
        return(0);
    else
        return(1);
}

```

```

/*a: compute the local acceptance rate of X*/
double a(double X)
{
    double appsigma(),applogaccprob(),mean();
    int ii;
    double Y, U, tmpval = 0.0;
    double alphaproposal[N];
    for(ii=0;ii<N;ii++)
    {
        Y = X + appsigma(X) * normal();
        U = drand48();
        if(log(U) < applogaccprob(X, Y))
            tmpval = tmpval + 1;
    }
    return (tmpval/N);
}

```

```

/*appsigma: approximation of sigma*/

```

```

double appsigma(double xx)
{
    double sigma();
    int ii;
    if((xx<left)|| (xx>=right)) return (sigma(RUNLENGTH-1,xx));
    else{
        for(ii=0;ii<numsig;ii++) {
            if((xx>=(left+ii*gap))&&(xx<(left+(ii+1)*gap)))
                return (appsig[ii]);
        }
    }
}

```

*/*applogaccprob: approximation of logaccprob*/*

```

double applogaccprob(double xx,double yy)
{
    double appsigma(), sq();

    return( logpi(yy)-logpi(xx)+log(appsigma(xx))-log(appsigma(yy))+sq(xx-yy)*(0.5/sq(ap
psigma(xx))-0.5/sq(appsigma(yy))) );
}

```

If we use approximation II, change "*sigma(RUNLENGTH-1,X)*" to "*appsigma(X)*" and "*logaccprob(RUNLENGTH-1,X,Y)*" to "*applogaccprob(X,Y)*" in the part to generate Markov Chain and the function a(double);

1.1.2 C code to implement the adaptation algorithm and generate a Markov Chain (Example 4)

```

#include <stdio.h>
#include <stdlib.h>
#include <math.h>
#include <sys/time.h>

#define RUNLENGTH 10000
#define PRINTSP 100
#define PI 3.1415926536
#define N 10000
#define M 100000
#define B 10000
#define numsigma 100
#define left -5
#define right 5
#define bottom -5
#define top 5
#define gap 0.1

```

```

#define m0 0x100000000LL
#define c0 0xB16
#define a0 0x5DEECE66DLL

double alpha1, alpha2, bn, beta, C, ggamma;
double height, width;
double x[2][RUNLENGTH], xlist[2][M];
int accept[RUNLENGTH];
int addsign[RUNLENGTH];
double appg[numsigma][numsigma], appsig[numsigma][numsigma];

int main()
{
    int i, j, n, numacc;
    double X[2], Y[2], U;
    FILE *fpg, *fpx, *fpsig, *fpout, *fpulist;
    int graphsp, graphleft, graphright, graphtop, graphbottom;
    clock_t start, end;
    double time0, time1, time2, time3, time4;

    double normal();
    double logpi(double, double);
    double g(int, double, double), K(double);
    double sigma(int, double, double), logaccprob(int, double, double, double, double);
    void seedrand();
    double a(double[2]);
    double appsigma(double, double), applogaccprob(double, double, double, double);

    seedrand();
    start = clock();

    /* Initial values. */
    alpha1 = 1.0;
    alpha2 = 1.0;
    bn = 1.0;
    beta = 0.0;
    C = 0.01; /*one parameter in the second term of sigma*/
    ggamma = 10.0; /*one parameter in the second term of sigma*/
    height = 0.5;
    width = 0.5;
    X[0] = 0.0;
    X[1] = 0.0;
    numacc = 0;
    graphsp = 15;

```

```

graphleft = graphbottom = -30;
graphright = graphtop = 30;

printf("\nHere we go!\n\n");

/* Do the run. */
for (n=0; n<RUNLENGTH; n++) {
    Y[0] = X[0] + sigma(n,X[0],X[1]) * normal();
    Y[1] = X[1] + sigma(n,X[0],X[1]) * normal();
    U = drand48();
    if ( log(U) < logaccprob(n,X[0],X[1], Y[0], Y[1]) ) {
        X[0] = Y[0];
        X[1] = Y[1];
        accept[n] = 1;
        numacc++;
        beta = beta + 1.0/pow((n+5),0.5)*(1.0-0.234);
    }
    else {
        accept[n] = 0;
        beta = beta - 1.0/pow((n+5),0.5)*0.234;
    }
    if ( log(0.234) < logaccprob(n,X[0],X[1], Y[0], Y[1]) )
        addsign[n] = 1 /* *(1-0.234)*;
    else
        addsign[n] = -1 /* * 0.234*/;
    x[0][n] = X[0];
    x[1][n] = X[1];
    if (divides(PRINTSP,n)) {
        printf("n=%d, X=(%f,%f), Y=(%f,%f), beta=%f, accept=%d\n", n, X[0],X[1],
Y[0],Y[1], beta, accept[n]);
    }
    /*bn = 1/pow((n+1),0.2); *//*fixed or decreasing bandwidth*/
}
printf("Accepted %d out of %d (%.3f%%).\n", numacc,
RUNLENGTH,100.0*numacc/RUNLENGTH);
printf("final beta = %f\n\n", beta);
end = clock();
time0 = (double) (end - start)/CLOCKS_PER_SEC;

start = clock();
printf("computing g and sigma values.... ");
for(i=0;i<numsigma;i++){
    for(j=0;j<numsigma;j++){
        X[0] = left + i*gap;

```

```

        X[1] = bottom + j*gap;
        appg[i][j] = g((RUNLENGTH-1),X[0],X[1]);
        appsig[i][j] = sigma((RUNLENGTH-1),X[0],X[1]);
    }
}
end = clock();
time1 = (double) (end - start)/CLOCKS_PER_SEC;

/*Plot the resulting g values to a file ... */
printf("Writing gvals ... \n");
if ((fpg = fopen("gvals", "w")) == NULL) {
    fprintf(stderr, "Unable to open output file 'gvals'. \n");
    exit(1);
}
fprintf(fpg, "gvals = c(");
for (i=graphleft*graphsp; i<(graphright*graphsp-1); i++){
    for(j=graphbottom*graphsp;j<(graphtop*graphsp-1);j++){
        fprintf(fpg, "%f,\n", g(n, 1.0*i/graphsp, 1.0*j/graphsp));
    }
    fprintf(fpg, "%f,\n", g(n, 1.0*i/graphsp, 1.0*(j+1)/graphsp));
}
for(j=graphbottom*graphsp;j<(graphtop*graphsp-1);j++){
    fprintf(fpg, "%f,\n", g(n, 1.0*(i+1)/graphsp, 1.0*j/graphsp));
}
fprintf(fpg, "%f)\n", g(n, 1.0*i/graphsp, 1.0*(j+1)/graphsp));
fclose(fpg);

/*Plot the resulting sigma values to a file ... */
printf("Writing sigvals ... \n");
if ((fpsig = fopen("sigvals", "w")) == NULL) {
    fprintf(stderr, "Unable to open output file 'sigvals'. \n");
    exit(1);
}
fprintf(fpsig, "sigvals = c(");
for (i=graphleft*graphsp; i<(graphright*graphsp-1); i++){
    for(j=graphbottom*graphsp;j<(graphtop*graphsp-1);j++){
        fprintf(fpsig, "%f,\n", sigma(n, 1.0*i/graphsp, 1.0*j/graphsp));
    }
    fprintf(fpsig, "%f,\n", sigma(n, 1.0*i/graphsp, 1.0*(j+1)/graphsp));
}
for(j=graphbottom*graphsp;j<(graphtop*graphsp-1);j++){
    fprintf(fpsig, "%f,\n", sigma(n, 1.0*(i+1)/graphsp, 1.0*j/graphsp));
}
fprintf(fpsig, "%f)\n", sigma(n, 1.0*i/graphsp, 1.0*(j+1)/graphsp));

```

```

fclose(fpsig);
end = clock();
time2 = (double) (end - start)/CLOCKS_PER_SEC;

/*Plot the resulting X values to a file ... */
printf("Writing xvals ... \n");
if ((fpx = fopen("xvals", "w")) == NULL) {
fprintf(stderr, "Unable to open output file 'xvals'. \n");
exit(1);
}
fprintf(fpx, "xvals1 = c(");
for (i=0; i<n-1; i++)
    fprintf(fpx, "%f, \n", x[0][i]);
fprintf(fpx, "%f)\n\n", x[0][n-1]);
fprintf(fpx, "xvals2 = c(");
for (i=0; i<n-1; i++)
    fprintf(fpx, "%f, \n", x[1][i]);
fprintf(fpx, "%f)\n\n", x[1][n-1]);
fprintf(fpx, "plot(xvals1,xvals2)");
fclose(fpx);

/*generate a Markov chain with scale proposed by the algorithm */
start = clock();
printf("generating Markov Chain ... \n");
xlist[0][0] = drand48()*20;
xlist[1][0] = drand48()*20; /*starting point*/
numacc = 0;
for(i=1; i<M; i++){
    Y[0] = xlist[0][(i-1)] + appsigma(xlist[0][i-1], xlist[1][i-1]) * normal();
    Y[1] = xlist[1][(i-1)] + appsigma(xlist[0][i-1], xlist[1][i-1]) * normal();
    U = drand48();
    if ( log(U) < applogaccprob(xlist[0][i-1], xlist[1][i-1], Y[0], Y[1]) ) {
        xlist[0][i] = Y[0];
        xlist[1][i] = Y[1];
        numacc++;
    }
    else {
        xlist[0][i] = xlist[0][i-1];
        xlist[1][i] = xlist[1][i-1];
    }
}
printf("run the M-H algorithm for %d times, and acceptance rate is (%.3f%%).\n",
M, 100.0*numacc/M);

```

```

/*save the resulting xlist values to a file */
printf("Writing xlist vals ... \n");
if ((fpclist = fopen("xlist", "w")) == NULL) {
    fprintf(stderr, "Unable to open output file 'xlist'. \n");
    exit(1);
}
fprintf(fpclist, "xlist1=c(");
for (i=0; i<(M-1); i++) {
    fprintf(fpclist, "%f, \n", xlist[0][i]);
}
fprintf(fpclist, "%f \n \n", xlist[0][M-1]);
fprintf(fpclist, "xlist2=c(");
for (i=0; i<(M-1); i++) {
    fprintf(fpclist, "%f, \n", xlist[1][i]);
}
fprintf(fpclist, "%f \n \n", xlist[1][M-1]);
fprintf(fpclist, "\n \n");
fclose(fpclist);
end = clock();
time3 = (double) (end - start)/CLOCKS_PER_SEC;

/*test alpha(x) for some specific vector x*/
start = clock();
printf("testing alpha ... \n");
if ((fpout = fopen("out", "w")) == NULL) {
    fprintf(stderr, "Unable to open output file 'xout'. \n");
    exit(1);
}
X[0] = 0; X[1] = 0;
fprintf(fpout, "alpha(%f, %f) is about %f \n", X[0], X[1], a(X));
fprintf(fpout, "alpha(%f, %f) is about %f \n", X[0], X[1], a(X));
X[0] = 5; X[1] = 5;
fprintf(fpout, "alpha(%f, %f) is about %f \n", X[0], X[1], a(X));
X[0] = 10; X[1] = 10;
fprintf(fpout, "alpha(%f, %f) is about %f \n", X[0], X[1], a(X));
X[0] = 20; X[1] = 50;
fprintf(fpout, "alpha(%f, %f) is about %f \n", X[0], X[1], a(X));
end = clock();
time4 = (double) (end - start)/CLOCKS_PER_SEC;
fprintf(fpout, "it takes %f seconds to run the adaptation algorithm \n", time0);
fprintf(fpout, "it takes %f seconds to compute g and sigma \n", time1);
fprintf(fpout, "it takes %f seconds to plot g and sigma \n", time2);
fprintf(fpout, "it takes %f seconds to generate the Markov Chain \n", time3);
fprintf(fpout, "it takes %f seconds to test the local acceptance \n", time4);

```

```

    fclose(fpout);
    fclose(fpout);

    printf("Done.\n");
    return(0);
}

/* NORMAL: return a standard normal random number. */
double normal()
{
    double R, theta, drand48();
    R = -log(drand48());
    theta = 2 * PI * drand48();
    return( sqrt(2*R) * cos(theta));
}

/* SEEDRAND: SEED RANDOM NUMBER GENERATOR. */
void seedrand()
{
    int i, seed;
    struct timeval tmptv;
    gettimeofday (&tmptv, (struct timezone *)NULL);
    seed = (int) tmptv.tv_usec;
    srand48(seed);
    (void)drand48(); /* Spin it once. */
}

int divides(int aa, int bb)
{
    return( (bb/aa)*aa == bb );
}

double logpi(double xx, double yy)
{
    double sq(), val;
    return (-sq(xx)/2-sq(yy)/2);
}

double g(int nn, double xx1, double xx2)
{
    int ii;
    double eta(), K(), val, abdif;
    val = 0.0;
    for (ii=0; ii<nn; ii++) {

```



```

        abdif = pow(sq(xx1-x[0][ii])+sq(xx2-x[1][ii]), 0.5);
        val = (1.0 - eta(ii)) * val + eta(ii) * addsign[ii] / bn * K(abdif/bn);
    }
    return(val);
}

double K(double xx)
{
    double abdif = fabs(xx);
    /*the kernel function is the exponential function*/
    return
        /*( exp(-pow(abdif,alpha1)/alpha2) );*/
        /*you can try other kernel function like: */
        /*( 1.0 / (1.0 + alpha1*pow( abdif, alpha2 ))); */
        height*( 2*indicator(abdif<width) -indicator(abdif<2*width) );
        /* indicator((abdif>=width)&&(abdif<2*width)); */
}

double sigma(int nn, double xx1, double xx2)
{
    double g();
    return( exp(beta) * pow(1.0 + C*pow(sq(xx1)+sq(xx2),0.5), ggamma) *
    exp( g(nn,xx1,xx2) ));
}

double logaccprob(int nn, double xx1, double xx2, double yy1, double yy2)
{
    double sigma(), sq();
    return( logpi(yy1,yy2) - logpi(xx1,xx2) + log(sigma(nn,xx1,xx2)) - log(sigma(nn,yy1,yy2))
    + (sq(xx1-yy1)+sq(xx2-yy2)) * (0.5/sq(sigma(nn,xx1,xx2))-
    0.5/sq(sigma(nn,yy1,yy2))));
}

double eta(int nn)
{
    return (1.0/pow(nn+5,0.5));
    /*return (1.0/pow(nn+5,0.8)); */
}

double sq(double xx)
{
    return(xx*xx);
}

int indicator(int bb)

```

```

{
  if (bb==0)
    return(0);
  else

    return(1);
}

double a(double X[2])
{
  int ii;
  double Y[2], U, tmpval=0.0;
  double alphaproposal[N];
  for(ii=0;ii<N;ii++)
  {
    Y[0] = X[0] + appsigma(X[0],X[1]) * normal();
    Y[1] = X[1] + appsigma(X[0],X[1]) * normal();
    U = drand48();
    if(log(U)<applogaccprob(X[0],X[1], Y[0], Y[1]))
      tmpval = tmpval + 1;
  }
  tmpval = tmpval/N;
  return tmpval;
}

double appsigma(double xx1,double xx2)
{
  int ii,jj;
  double val;
  if( (abs(xx1)>right) || (abs(xx2)>right) || (abs(xx1)==right) || (abs(xx2)==right)
  )
    val = sigma((RUNLENGTH-1),xx1,xx2);
  for(ii=0;ii<numsigma;ii++){
    for(jj=0;jj<numsigma;jj++){
      if(((xx1>left+ii*gap)||xx1==left+ii*gap)&xx1<left+(ii+1)*gap)&
      ((xx2>bottom+jj*gap)||xx2==bottom+jj*gap)&xx2<bottom+(jj+1)*gap))
        val = appsig[ii][jj];
    }
  }
  return val;
}

double applogaccprob(double xx1,double xx2,double yy1,double yy2)

```

```

{
  double appsigma(), sq();
  return( logpi(yy1,yy2) - logpi(xx1,xx2) + log(appsigma(xx1,xx2)) -
log(appsigma(yy1,yy2))
+ (sq(xx1-yy1)+sq(xx2-yy2)) * (0.5/sq(appsigma(xx1,xx2))-
0.5/sq(appsigma(yy1,yy2))));
}

```

1.2 R code

1.2.1 R code to plot the final $g(X)$ and $\sigma(X)$

```

source("gvals")
source("sigvals")

L = length(gvals)
x = seq(-50,50,length = L)
M = 10^5
B = 10^4
varfact = function(xxx) { 2 * sum(acf(xxx, plot=FALSE)$acf) - 1 }
asjd = function(x){
val = 0
for(i in (B+1):M )
  val = val +(xlist[i]-xlist[i-1])^2
return (val/(M-B))
}
par(mfrow=c(1,2))
plot(x,gvals)
plot(x,sigvals)
pdf(file = ifelse(T, "plot.pdf", "plot%03d.pdf"),width=10,height=5,pointsize = 1/200)
par(mfrow=c(1,2))
plot(x,gvals)
plot(x,sigvals)
dev.off()

```

1.2 R code

1.2.1 R code to plot the final $g(X)$ and $\sigma(X)$ (Example 1~3)

```

source("gvals")
source("sigvals")

L = length(gvals)
x = seq(-50,50,length = L)

```

```

M = 10^5
B = 10^4
varfact = function(xxx) { 2 * sum(acf(xxx, plot=FALSE)$acf) - 1 }
asjd = function(x){
val = 0
for(i in (B+1):M)
  val = val +(xlist[i]-xlist[i-1])^2
return (val/(M-B))
}
par(mfrow=c(1,2))
plot(x,gvals)
plot(x,sigvals)
pdf(file = ifelse(T, "plot.pdf", "plot%03d.pdf"),width=10,height=5,pointsize = 1/200)
par(mfrow=c(1,2))
plot(x,gvals)
plot(x,sigvals)
dev.off()

```

1.2.2 R code to plot the final $g(X)$ and $\sigma(X)$ (Example 4)

```

source("gvals")
source("sigvals")
L = length(gvals)
L;sqrt(L);
x = seq(-30,30,length = sqrt(L))
M = 10^5
B = 10^4
varfact = function(xxx) { 2 * sum(acf(xxx, plot=FALSE)$acf) - 1 }

plot(x,gvals[(449*900+1):(450*900)],main="g(x, *)",ylab="g")
lines(x,gvals[((15*28)*900+1):((15*28+1)*900)],col="blue")
lines(x,gvals[((15*25)*900+1):((15*25+1)*900)],col="green")
lines(x,gvals[(300*900+1):(301*900)],col="yellow")
lines(x,gvals[1:900],col="red")

plot(x,sigvals[(449*900+1):(450*900)],ylim=c(0,50),main="sig(x, *)",ylab="sig")
lines(x,sigvals[(300*900+1):(301*900)],col="yellow")
lines(x,sigvals[((15*25)*900+1):((15*25+1)*900)],col="green")
lines(x,sigvals[((15*28)*900+1):((15*28+1)*900)],col="blue")
lines(x,sigvals[1:900],col="red")

pdf(file = ifelse(T, "plot.pdf", "plot%03d.pdf"),width=10,height=5,pointsize = 1/200)
par(mfrow=c(1,2))
plot(x,gvals[(449*900+1):(450*900)])

```

```

lines(x,gvals[(300*900+1):(301*900)],col="yellow")
lines(x,gvals[((15*25)*900+1):((15*25+1)*900)],col="green")
lines(x,gvals[((15*28)*900+1):((15*28+1)*900)],col="blue")
lines(x,gvals[1:900],col="red")
plot(x,sigvals[(449*900+1):(450*900)],ylim=c(0,50),main="sig(x,*)",ylab="sig")
lines(x,sigvals[(300*900+1):(301*900)],col="yellow")
lines(x,sigvals[((15*25)*900+1):((15*25+1)*900)],col="green")
lines(x,sigvals[((15*28)*900+1):((15*28+1)*900)],col="blue")
lines(x,sigvals[1:900],col="red")
dev.off()

```

1.2.3 R code to generate Markov Chain without adaption (Example 1)

```

logpi = function(x){
  return (- x^2/2);
}

```

```

M = 100000;

```

```

B = 10000;

```

```

xlist = rep(0.0,M);

```

```

num = 0;

```

```

X = runif(1);

```

```

sigma = 5.21;

```

```

for(i in 1:M){

```

```

  Y = X + sigma * rnorm(1);

```

```

  U = runif(1);

```

```

  logalpha = logpi(Y) - logpi(X);

```

```

  if (log(U) < logalpha) {

```

```

    X = Y;

```

```

    num = num + 1;

```

```

  }

```

```

  xlist[i] = X;

```

```

}

```

```

cat("ran Metropolis algorithm for", M, "iterations, with burn-in", B, "\n");

```

```

cat("acceptance rate =", num/M, "\n");

```

```

varfact <- function(xxx) { 2 * sum(acf(xxx, plot=FALSE)$acf) - 1 }

```

```

varf = varfact(xlist[(B+1):M]);

```

```

se = sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );

```

```

val = 0

```

```

for(i in (B+1):M)

```

```

  val = val +(xlist[i]-xlist[i-1])^2

```

```

asjd = val/(M-B)

```

```

varf;
se;
asjd;

a = function(x){
  tmpval = 0;
  for(i in 1:M){
    y = x + sigma * rnorm(1);
    u = runif(1);
    if (log(u) < (logpi(y)-logpi(x)))
      tmpval = tmpval + 1;
  }
  return (tmpval/M);
}

```

1.2.4 R code to generate Markov Chain without adaption (Example 2)

```

logpi = function(x){
  y = 0.0;
  if(x<=0) y = - x^2/2;
  if(x>=10) y = -(x-10)^2/2;
  if(x>0&&x<10) y = log(exp(- x^2/2)+exp(- (x-10)^2/2));
  return (y);
}
L = 10^4
x = seq(-30,30,length=L)
y = rep(0,L)
for(i in 1:L)
  y[i] = exp(logpi(x[i]))
plot(x,y)
M = 100000;
B = 10000;
xlist = rep(0.0,M);
num = 0;
X = runif(1);
sigma = 7.7;

for(i in 1:M){
  Y = X + sigma * rnorm(1);
  U = runif(1);
  logalpha = logpi(Y) - logpi(X);
  if (log(U) < logalpha) {
    X = Y;
    num = num + 1;
  }
}

```

```

    }
    xlist[j] = X;
}
varfact <- function(xxx) { 2 * sum(acf(xxx, plot=FALSE)$acf) - 1 }
varf = varfact(xlist[(B+1):M]);
se = sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );

val = 0
for(j in (B+1):M)
  val = val +(xlist[j]-xlist[j-1])^2
asjd = val/(M-B)
cat("ran Metropolis algorithm for", M, "iterations, with burn-in", B, "\n");
cat("acceptance rate =", num/M, "\n");

varf;
se;
asjd;

```

1.2.5 R code to generate Markov Chain without adaption (Example 3)

```

logpi = function(x){
  y = 0.0;
  if(x<=-12) y = log(0.3)-(x+10.0)^2/2.0;
  if(x>=12) y = log(0.3)-(x-10.0)^2/2.0;
  if(x>-12&& x<12) y = log(0.3*exp(-(x+10.0)^2/2)+0.4*exp(-x^2/2)+0.3*exp(-(x-10.0)^2/2));
  return (y);
}

M = 100000;
B = 10000;
xlist = rep(0.0,M);
num = 0;
X = runif(1);
sigma = 10.8;

for(i in 1:M){
  Y = X + sigma * rnorm(1);
  U = runif(1);
  logalpha = logpi(Y) - logpi(X);
  if (log(U) < logalpha) {
    X = Y;
    num = num + 1;
  }
  xlist[i] = X;
}

```

```

varfact <- function(xxx) { 2 * sum(acf(xxx, plot=FALSE)$acf) - 1 }
varf = varfact(xlist[(B+1):M]);
se = sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );

val = 0
for(i in (B+1):M)
  val = val +(xlist[i]-xlist[i-1])^2
asjd = val/(M-B)
cat("ran Metropolis algorithm for", M, "iterations, with burn-in", B, "\n");
cat("acceptance rate =", num/M, "\n");
cat("varfact is about", varf, "\n");
cat("standard error is about", se, "\n");
cat("average squared jump distance is about", asjd, "\n");
par(mfrow=c(1,2))
plot(xlist[(B+1):M], type="l");
plot(xlist[(B+1):M], type="p");

```

1.2.6 R code to generate Markov Chain without adaption (Example 4)

```

logpi = function(x,y){
return (-x^2/2-y^2/2);
}

```

```

M = 100000;
B = 10000;
xlist1 = xlist2 = rep(0.0,M);
num = 0;
X1 = runif(1);
X2 = runif(1);
sigma = 2.39;

for(j in 1:M){
  Y1 = X1 + sigma * rnorm(1);
  Y2 = X2 + sigma * rnorm(1);
  U = runif(1);
  if (log(U) < (logpi(Y1, Y2) - logpi(X1,X2))) {
    X1 = Y1;
    X2 = Y2;
    num = num + 1;
  }
  xlist1[j] = X1;
  xlist2[j] = X2;
}

```

```

varfact = function(xxx) { 2 * sum(acf(xxx, plot=FALSE)$acf) - 1 }

```



```

asjd = function(xlist){
  val = 0
  for(i in (B+1):M)
    val = val +(xlist[i]-xlist[i-1])^2
  return (val/(M-B));
}
cat("ran Metropolis algorithm for", M, "iterations, with burn-in", B, "\n");
cat("acceptance rate =", num/M, "\n");
cat("varfact is about", varfact(xlist1[(B+1):M]), "and", varfact(xlist2[(B+1):M]), "\n");
cat("standard error is about", (sd(xlist1[(B+1):M]) / sqrt(M-B) *
sqrt( varfact(xlist1[(B+1):M]))) , "and", (sd(xlist2[(B+1):M]) / sqrt(M-B) *
sqrt( varfact(xlist2[(B+1):M]))) , "\n");
cat("average squared jump distance is about", asjd(xlist1), "and", asjd(xlist2), "\n");
par(mfrow=c(2,2));
plot(xlist1[(B+1):M], type="l");
plot(xlist1[(B+1):M], type="p");
plot(xlist2[(B+1):M], type="l");
plot(xlist2[(B+1):M], type="p");
par(mfrow=c(1,2));
plot(xlist1[(B+1):M], xlist2[(B+1):M], type="p");
plot(xlist1[(B+1):M], xlist2[(B+1):M], type="l")

```

1.2.7 R code to compute different efficiency measures (Example 1~3)

```

par(mfrow=c(3,2))
source("xlist1");plot(xlist[(B+1):M], type="l");source("xlist2");plot(xlist[(B+1):M], type="l");
source("xlist3");plot(xlist[(B+1):M], type="l");source("xlist4");plot(xlist[(B+1):M], type="l");
source("xlist5");plot(xlist[(B+1):M], type="l");

pdf(file = ifelse(T, "trace plot.pdf", "trace plot%03d.pdf"), width=10, height=5, pointsize =
1/200)
par(mfrow=c(3,2))
source("xlist1");plot(xlist[(B+1):M], type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
source("xlist2");plot(xlist[(B+1):M], type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
source("xlist3");plot(xlist[(B+1):M], type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
source("xlist4");plot(xlist[(B+1):M], type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
source("xlist5");plot(xlist[(B+1):M], type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
dev.off()

```

1.2.8 R code to compute different efficiency measures (Example 4)

```

pdf(file = ifelse(T, "plot.pdf", "plot%03d.pdf"), width=10, height=5, pointsize = 1/200)
par(mfrow=c(1,2))
plot(x, gvals[(449*900+1):(450*900)])
lines(x, gvals[(300*900+1):(301*900)], col="yellow")
lines(x, gvals[((15*25)*900+1):((15*25+1)*900)], col="green")
lines(x, gvals[((15*28)*900+1):((15*28+1)*900)], col="blue")
lines(x, gvals[1:900], col="red")
plot(x, sigvals[(449*900+1):(450*900)], ylim=c(0, 50), main="sig(x, *)", ylab="sig")
lines(x, sigvals[(300*900+1):(301*900)], col="yellow")
lines(x, sigvals[((15*25)*900+1):((15*25+1)*900)], col="green")
lines(x, sigvals[((15*28)*900+1):((15*28+1)*900)], col="blue")
lines(x, sigvals[1:900], col="red")
dev.off()

```

1.2.9 R code to implement OLS in approximation of the final $\sigma(X)$

```
#####comparison#####
```

```

L = 10001
left = -50
right = 50
gap = 0.01

```

```

l1 = l2 = l3 = rep(0,L)
source("sigvals-11")
for(i in 1:L) l1[i] = sigvals[i]
source("sigvals-14")
for(i in 1:L) l2[i] = sigvals[i]
source("sigvals-16")
for(i in 1:L) l3[i] = sigvals[i]

```

```
x = seq(-50,50,length = L)
```

```

par(mfrow=c(1,3))
plot(x,l1)
plot(x,l2)
plot(x,l3)

```

```
#####OLS for CASE 14#####
```

```

left = -3
right = 3
L = 601
gap = 0.01

```

```

l = rep(0,L)
for(i in 1:L)
  l[i]=l2[i+4700]

c = 0.0;
exponnet = 1.0;
n = 200;
k = 120;
sse = matrix(rep(0.0,n*k),nrow=k);
rowindex = 1;
colindex = 1;

for(row in 1:k){
  exponent = 12*row/k;
  for(col in 1:n){
    c = 20*col/n;
    for(i in 1:L){
      X = left + (i-1)* gap;
      sse[row,col] = sse[row,col] + (l[i]-(c*abs(X)^exponent+l[(L-1)/2+1]))^2 ;
    }
    if( sse[rowindex,colindex]>sse[row,col] ) {
      rowindex = row;
      colindex = col;}}
}

c =20*colindex/n;
exponent = 12*rowindex/k;
c1=c;
e1=exponent;

app = rep(0.0,L);
for(i in 1:L) {
  X = left + (i-1)* gap;
  app[i] = c*abs(X)^exponent+l[(L-1)/2+1];
}
x = seq(left,right,length=L)
plot(x,app);
lines(x,l,col="red")

c1*abs(-3)^e1+l[(L-1)/2+1]

left = -50

```

```

right = -3
L = 4701
gap = 0.01

```

```

l = rep(0,L)
for(i in 1:L)
  l[i]=l2[i]

```

```

c = 0.0;
exponent = 0.0;
n = 200;
k = 100;
sse = matrix(rep(0.0,n*k),nrow=k);
rowindex = 1;
colindex = 1;

```

```

for(row in 1:k){
  exponent = row/k;
  for(col in 1:n){
    c = 20*col/n;
    for(i in 1:L){
      X = left + (i-1)* gap;
      sse[row,col] = sse[row,col] +
      (l[i]-(c*abs(X)^exponent+6.973254-3^exponent*c))^2 ;
    }
    if( sse[rowindex,colindex]>sse[row,col] ) {
      rowindex = row;
      colindex = col;}}
}

```

```

c = 20*colindex/n;
exponent = rowindex/k;
c;c2=c
exponent;e2=exponent

```

```

app = rep(0.0,L);
for(i in 1:L) {
  X = left + (i-1)* gap;
  app[i] = c*abs(X)^exponent+6.973254-3^exponent*c;
}

```

```

x = seq(left,right,length=L)
plot(x, app);

```

```
lines(x,l,col="red")
```

```
sigma = function(x){  
  if(abs(x)<3) y = c1*(abs(x))^e1 + 5.572407;  
  if(abs(x)==3||abs(x)>3) y = c2*(abs(x))^e2 + 6.973254-3^e2*c2;  
  return (y)  
}
```

```
x = seq(-50,50,length=10001)  
y = rep(0,10001)  
for( i in 1:10001)  
  y[i] = sigma(x[i])  
plot(x,l2)  
lines(x,y,col="red")
```

```
#### check ####  
logpi = function(x){  
  return (- x^2/2);  
}
```

```
f = function(x,y){  
  return  
  ( logpi(y)-logpi(x)+(x-y)^2*(1/sigma(x)^2-1/sigma(y)^2))+log(sigma(x))-log(sigma(y) );  
}
```

```
M = 1000  
x = c(30,50,80,150,200,300);  
z = rep(1,M)
```

```
par(mfrow=c(3,2))  
for(i in 1:6){  
  y = seq(x[i]-3*sigma(x[i]),x[i]+3*sigma(x[i]),length=M)  
  for(j in 1:M){  
    if(f(x[i],y[j])<0) z[j]= exp(f(x[i],y[j]));  
  }  
  plot(y,z,main=c("when x=",x[i]))  
}
```

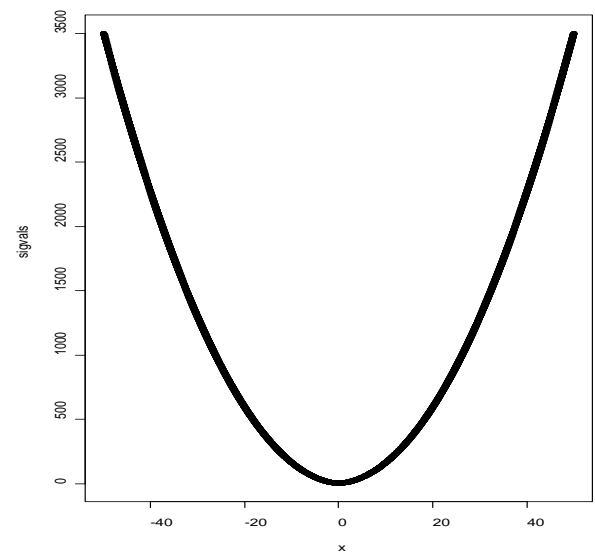
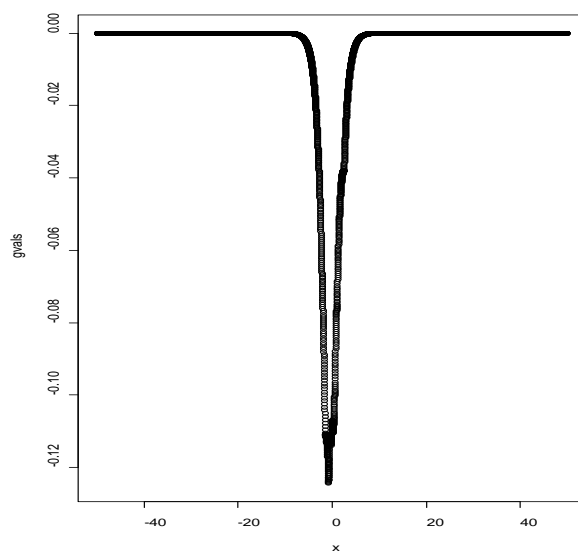

2. Output

2.1 Example 1: normal distribution in R^1

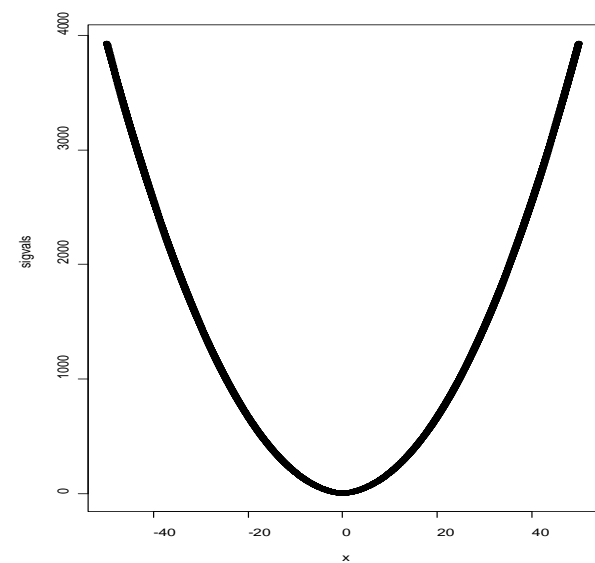
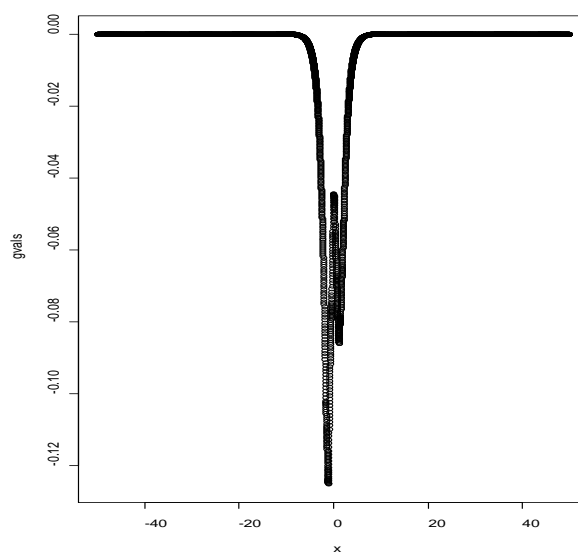
2.1.1 kernel function $K(x) = e^{-\frac{|x|^{\alpha_1}}{\alpha_2}}$

2.1.1.1 case 1 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$

Without approximation:



With approximation:



Accepted 22920 out of 100000 (22.920%).

final beta = 0.413548

alpha(0.000000) is 0.294400

alpha(2.000000) is 0.146900

alpha(5.000000) is 0.079300

alpha(10.000000) is 0.047600

alpha(20.000000) is 0.022500

alpha(50.000000) is 0.009100

alpha(100.000000) is 0.005800

alpha(150.000000) is 0.002600

it takes 233.63636 seconds to run the adaptation algorithm

it takes 95.5646 seconds to compute g and sigma

it takes 21.525 seconds to generate the first Markov Chain

it takes 25.2524 seconds to generate the second Markov Chain

it takes 23.8585 seconds to generate the third Markov Chain

it takes 21.156 seconds to generate the fourth Markov Chain

it takes 26.6363 seconds to generate the fifth Markov Chain

it takes 1564.99 seconds to test the local acceptance

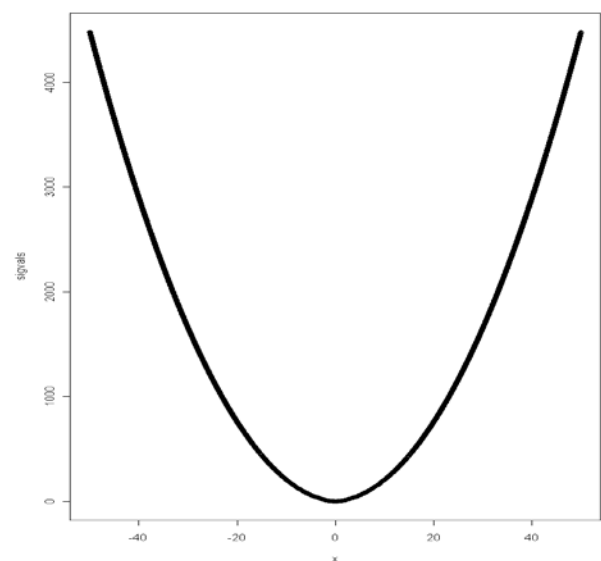
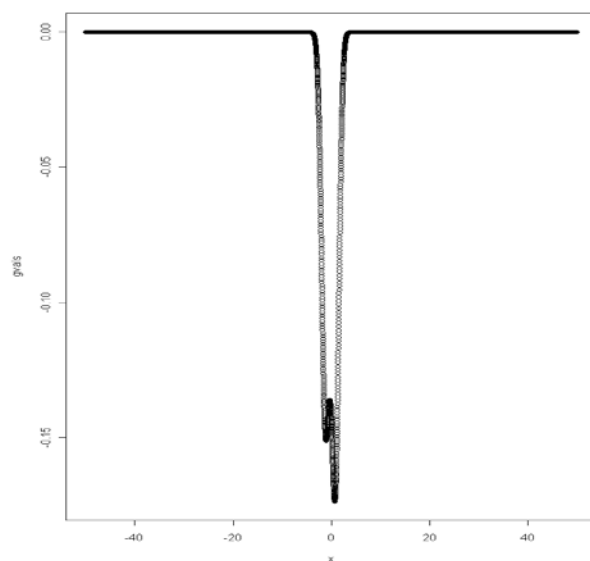
|


```

> source("xlist1");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 11.35909
[1] 0.01122983
[1] 0.33542
> source("xlist2");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 12.05121
[1] 0.01172226
[1] 0.3463196
> source("xlist3");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 11.45263
[1] 0.01136355
[1] 0.3383667
> source("xlist4");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 10.70036
[1] 0.01089844
[1] 0.3378794
> source("xlist5");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 10.27269
[1] 0.01078979
[1] 0.3482317

```

2.1.1.2 case 2 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 21393 out of 100000 (21.393%).

final beta = 0.543719

alpha(0.000000) is 0.275100

alpha(2.000000) is 0.123300

alpha(5.000000) is 0.065000

alpha(10.000000) is 0.036300

alpha(20.000000) is 0.020400

alpha(50.000000) is 0.008500

alpha(100.000000) is 0.003700

alpha(150.000000) is 0.004400

it takes 231.632000 seconds to run the adaptation algorithm

it takes 153.155000 seconds to compute g and sigma

it takes 22.924000 seconds to generate the first Markov Chain

it takes 23.594000 seconds to generate the second Markov Chain

it takes 23.285000 seconds to generate the third Markov Chain

it takes 21.130000 seconds to generate the fourth Markov Chain

it takes 21.698000 seconds to generate the fifth Markov Chain

it takes 1627.749000 seconds to test the local acceptance

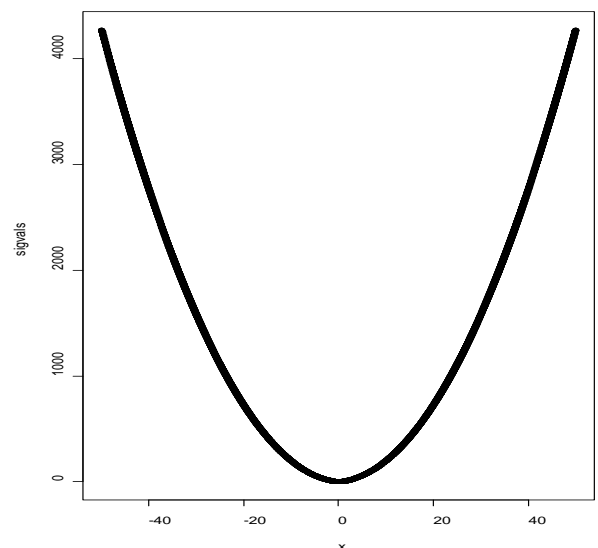
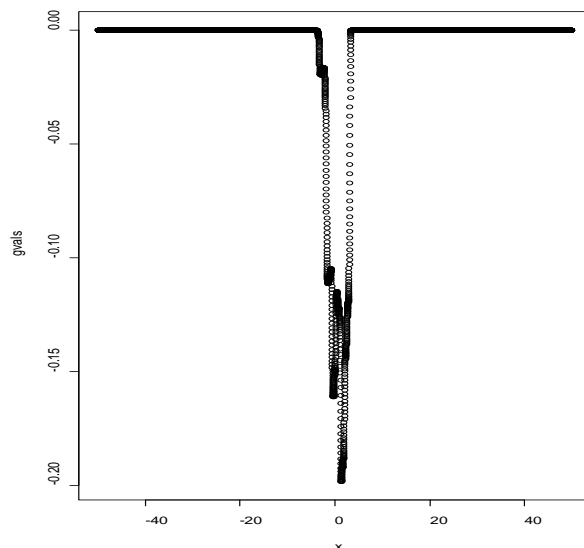


```

> source("xlist2");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 12.98504
[1] 0.01201336
[1] 0.3106892
> source("xlist3");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 13.36214
[1] 0.01222844
[1] 0.3051376
> source("xlist4");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 12.5798
[1] 0.01166746
[1] 0.3061098
> source("xlist5");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 11.6263
[1] 0.01115963
[1] 0.309262

```

2.1.1.3 case 3 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 22184 out of 100000 (22.184%).

final beta = 0.496175

alpha(0.000000) is 0.287000

alpha(2.000000) is 0.146700

alpha(5.000000) is 0.067300

alpha(10.000000) is 0.042100

alpha(20.000000) is 0.022000

alpha(50.000000) is 0.008600

alpha(100.000000) is 0.005500

alpha(150.000000) is 0.002500

it takes 482.924000 seconds to run the adaptation algorithm

it takes 231.983000 seconds to compute g and sigma

it takes 36.292000 seconds to generate the first Markov Chain

it takes 38.465000 seconds to generate the second Markov Chain

it takes 36.953000 seconds to generate the third Markov Chain

it takes 35.281000 seconds to generate the fourth Markov Chain

it takes 36.833000 seconds to generate the fifth Markov Chain

it takes 2345.843000 seconds to test the local acceptance

|

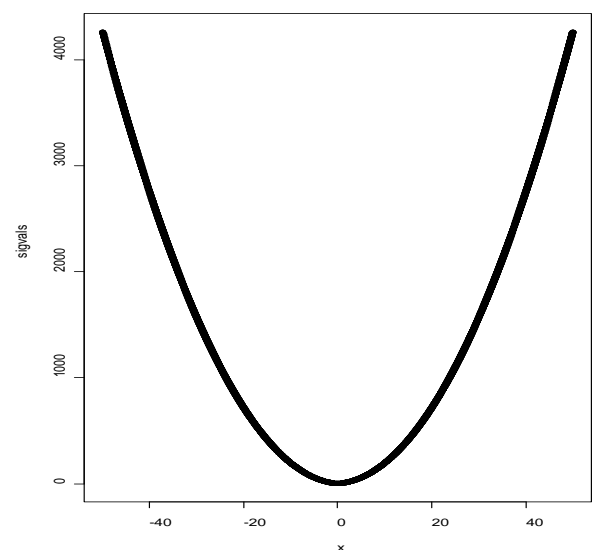
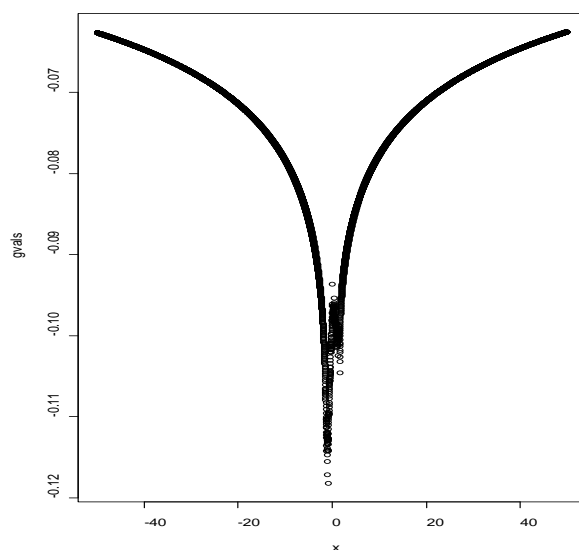
\

```

> source("xlist3");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 12.00902
[1] 0.0117056
[1] 0.3388592
> source("xlist4");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 11.17787
[1] 0.01105268
[1] 0.3208399
> source("xlist5");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 12.35328
[1] 0.01156459
[1] 0.3275879

```

2.1.1.4 case 4 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 20175 out of 100000 (20.175%).

final beta = 0.557074

alpha(0.000000) is 0.263300

alpha(2.000000) is 0.135800

alpha(5.000000) is 0.070300

alpha(10.000000) is 0.041900

alpha(20.000000) is 0.021200

alpha(50.000000) is 0.008200

alpha(100.000000) is 0.005600

alpha(150.000000) is 0.004000

it takes 436.537000 seconds to run the adaptation algorithm
it takes 191.065000 seconds to compute g and sigma
it takes 36.543000 seconds to generate the first Markov Chain
it takes 36.102000 seconds to generate the second Markov Chain
it takes 39.417000 seconds to generate the third Markov Chain
it takes 37.934000 seconds to generate the fourth Markov Chain
it takes 37.694000 seconds to generate the fifth Markov Chain
it takes 1960.229000 seconds to test the local acceptance

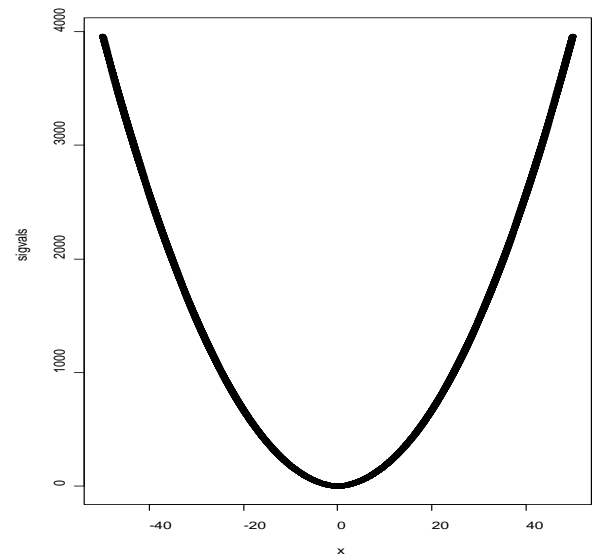
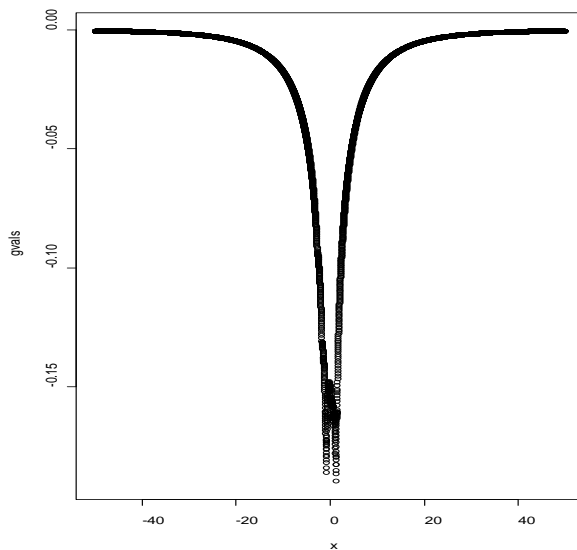
|

```

[1] 0.3049649
> source("xlist4");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 12.47907
[1] 0.01187855
[1] 0.3073156
> source("xlist5");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 13.20204
[1] 0.01218168
[1] 0.303518

```

2.1.1.5 case 5 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.5, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 24190 out of 100000 (24.190%).

final beta = 0.420755

alpha(0.000000) is 0.309200

alpha(2.000000) is 0.150900

alpha(5.000000) is 0.076500

alpha(10.000000) is 0.045300

alpha(20.000000) is 0.022600

alpha(50.000000) is 0.010200

alpha(100.000000) is 0.003300

alpha(150.000000) is 0.003400

it takes 458.670000 seconds to run the adaptation algorithm

it takes 208.940000 seconds to compute g and sigma

it takes 106.120000 seconds to generate the first Markov Chain

it takes 108.450000 seconds to generate the second Markov Chain

it takes 107.710000 seconds to generate the third Markov Chain

it takes 106.870000 seconds to generate the fourth Markov Chain
it takes 108.390000 seconds to generate the fifth Markov Chain
it takes 2139.130000 seconds to test the local acceptance

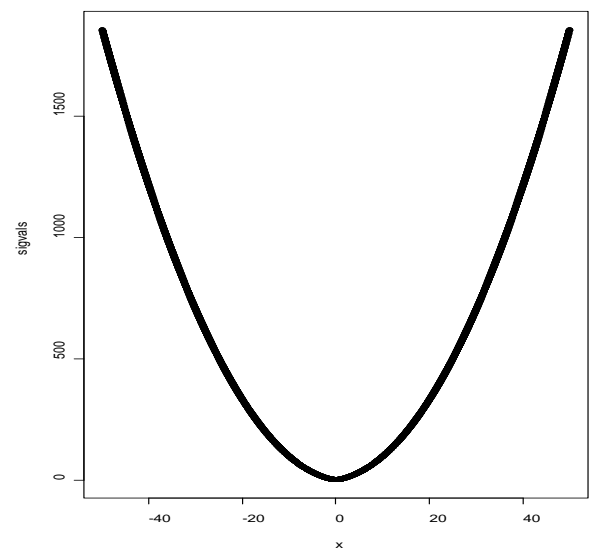
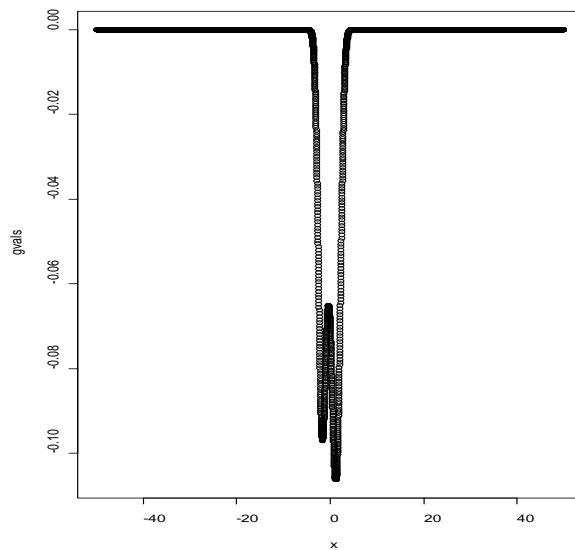
|


```

[1] 0.3406725
> source("xlist5");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 10.34777
[1] 0.01072979
[1] 0.3623652

```

2.1.1.6 case 6 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 2, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 21452 out of 100000 (21.452%).

final beta = -0.217726

alpha(0.000000) is 0.345100

alpha(2.000000) is 0.092500

alpha(5.000000) is 0.043700

alpha(10.000000) is 0.019400

alpha(20.000000) is 0.011800

alpha(50.000000) is 0.004900

alpha(100.000000) is 0.001900

alpha(150.000000) is 0.002400

it takes 453.780000 seconds to run the adaptation algorithm

it takes 325.460000 seconds to compute g and sigma

it takes 142.590000 seconds to generate the first Markov Chain

it takes 143.880000 seconds to generate the second Markov Chain

it takes 136.990000 seconds to generate the third Markov Chain

it takes 139.650000 seconds to generate the fourth Markov Chain

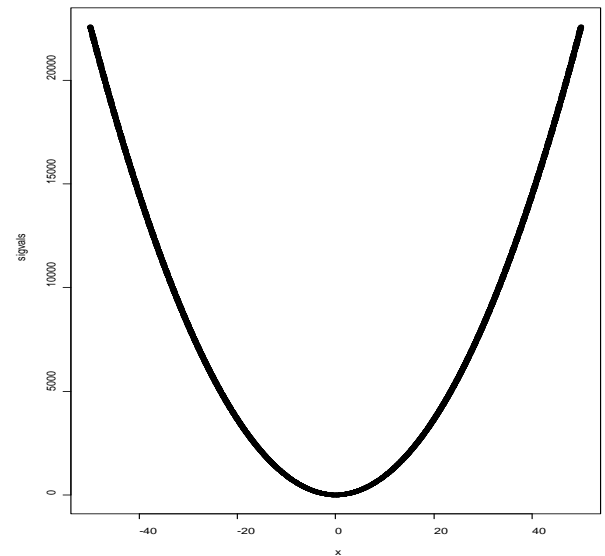
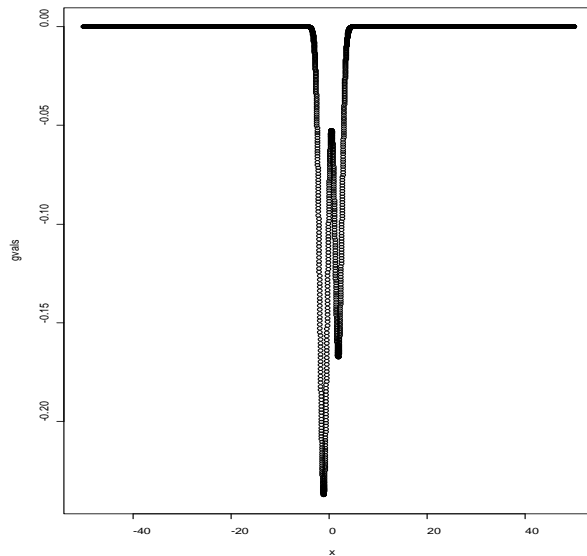
it takes 135.720000 seconds to generate the fifth Markov Chain

it takes -1420.447296 seconds to test the local acceptance

1

[1] 14.36675
[1] 0.01244616
[1] 0.2595380

2.1.1.7 case 7 $\alpha_1 = 2, \alpha_2 = 1, C = 10, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 23083 out of 100000 (23.083%).

final beta = -2.408190

alpha(0.000000) is 0.638400

alpha(2.000000) is 0.050600

alpha(5.000000) is 0.015100

alpha(10.000000) is 0.008200

alpha(20.000000) is 0.003700

alpha(50.000000) is 0.001800

alpha(100.000000) is 0.000600

alpha(150.000000) is 0.000300

it takes 464.760000 seconds to run the adaptation algorithm

it takes 320.620000 seconds to compute g and sigma

it takes 245.030000 seconds to generate the first Markov Chain

it takes 240.520000 seconds to generate the second Markov Chain

it takes 235.190000 seconds to generate the third Markov Chain

it takes 230.100000 seconds to generate the fourth Markov Chain

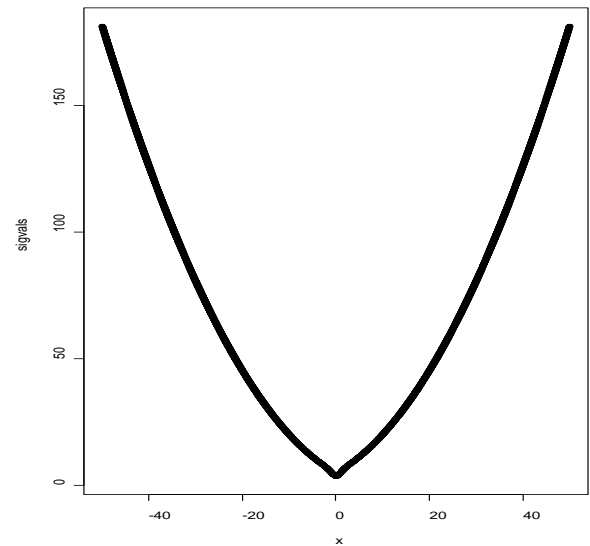
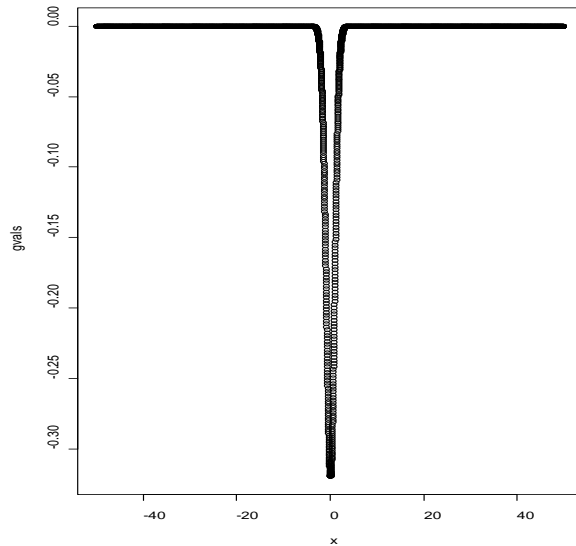
it takes 228.730000 seconds to generate the fifth Markov Chain

it takes -1298.167296 seconds to test the local acceptance

1

[1] 28.38106
[1] 0.01755109
[1] 0.1614916

2.1.1.8 case 8 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 23789 out of 100000 (23.789%).

final beta = 1.685565

alpha(0.000000) is 0.209326

alpha(2.000000) is 0.310810

alpha(5.000000) is 0.450666

alpha(10.000000) is 0.503885

alpha(20.000000) is 0.509007

alpha(50.000000) is 0.500492

alpha(100.000000) is 0.497852

alpha(150.000000) is 0.502459

alpha(200.000000) is 0.498544

alpha(300.000000) is 0.501603

it takes 219.483000 seconds to run the adaptation algorithm

it takes 144.400000 seconds to compute g and sigma

it takes 19.396000 seconds to generate the first Markov Chain

it takes 19.387000 seconds to generate the second Markov Chain

it takes 19.118000 seconds to generate the third Markov Chain

it takes 19.331000 seconds to generate the fourth Markov Chain

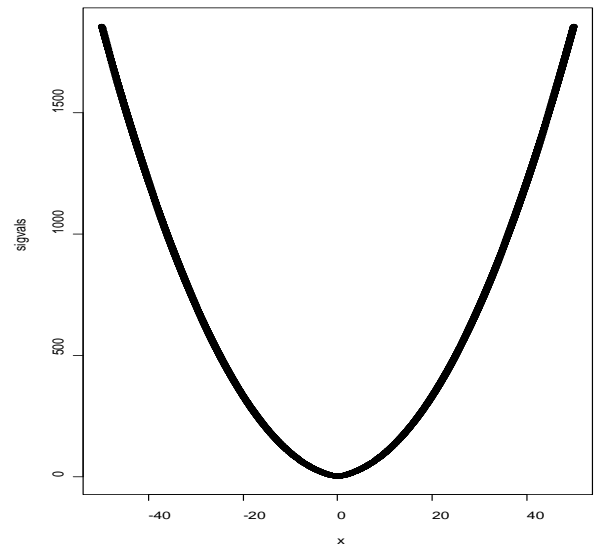
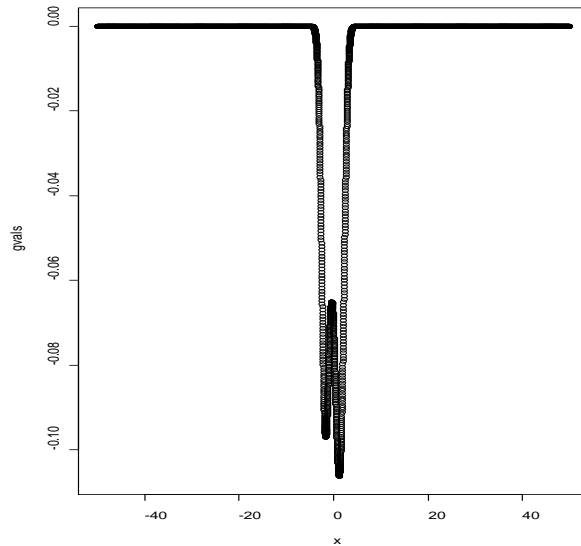
it takes 19.341000 seconds to generate the fifth Markov Chain

it takes 2855.818000 seconds to test the local acceptance

1

[1] 6.911154
[1] 0.008697184
[1] 0.5301068

2.1.1.9 case 9 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.5, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 21014 out of 100000 (21.014%).

final beta = 1.010674

alpha(0.000000) is 0.232100

alpha(2.000000) is 0.183200

alpha(5.000000) is 0.124800

alpha(10.000000) is 0.083000

alpha(20.000000) is 0.049300

alpha(50.000000) is 0.021500

alpha(100.000000) is 0.010600

alpha(150.000000) is 0.006200

it takes 441.064000 seconds to run the adaptation algorithm

it takes 244.381000 seconds to compute g and sigma

it takes 28.692000 seconds to generate the first Markov Chain

it takes 28.120000 seconds to generate the second Markov Chain

it takes 28.852000 seconds to generate the third Markov Chain

it takes 28.320000 seconds to generate the fourth Markov Chain

it takes 29.292000 seconds to generate the fifth Markov Chain

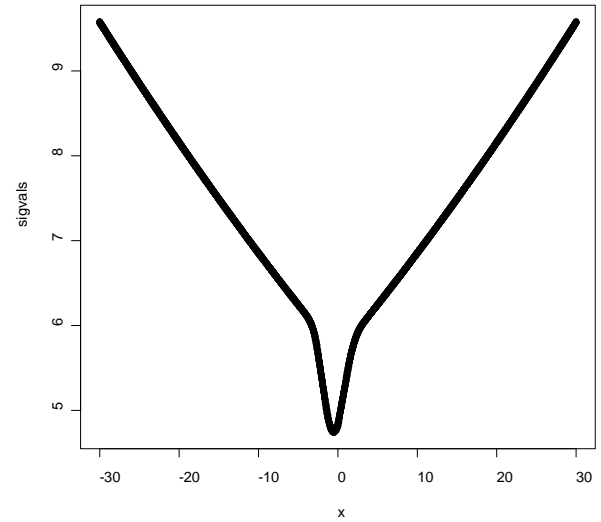
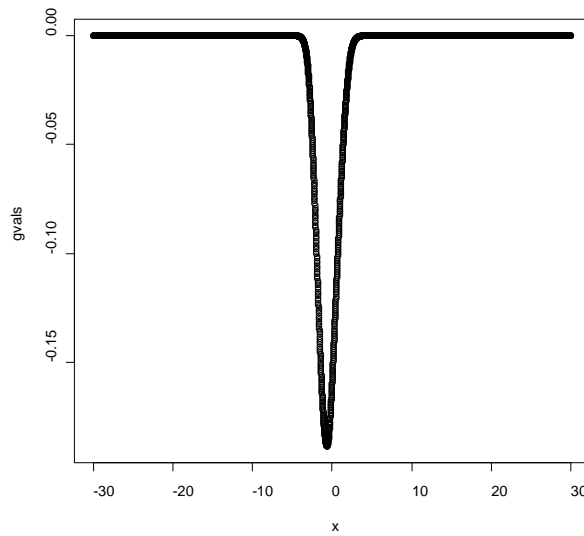
it takes 2695.236000 seconds to test the local acceptance

1

[1] 10.2363
[1] 0.01076473
[1] 0.3784802

2.1.1.10 case 10 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.01, \gamma = 2$ with fixed bandwidth

$b_n = 1$



Accepted 23515 out of 100000 (23.515%).

final beta = 1.734452

alpha(0.000000) is 0.197174

alpha(2.000000) is 0.303052

alpha(5.000000) is 0.461148

alpha(10.000000) is 0.507069

alpha(20.000000) is 0.504815

alpha(50.000000) is 0.501644

alpha(100.000000) is 0.500501

alpha(150.000000) is 0.496824

it takes 216.113000 seconds to run the adaptation algorithm

it takes 66.348000 seconds to compute g and sigma

it takes 11.710000 seconds to generate the first Markov Chain

it takes 11.877000 seconds to generate the second Markov Chain

it takes 11.680000 seconds to generate the third Markov Chain

it takes 11.616000 seconds to generate the fourth Markov Chain

it takes 11.568000 seconds to generate the fifth Markov Chain

it takes 1890.326000 seconds to test the local acceptance

1

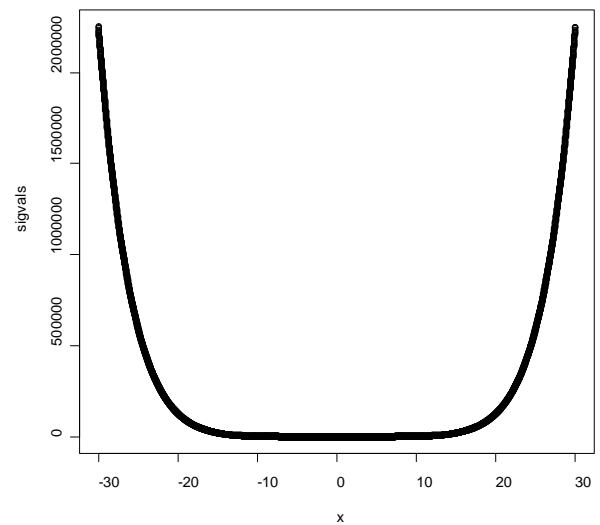
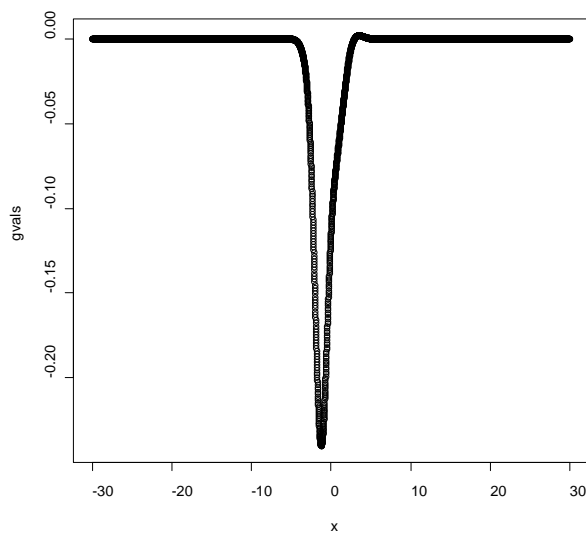
```

> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.008994134
> asjd(xlist)
[1] 0.5588261
>
> source("xlist4")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 5.971771
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.008119293
> asjd(xlist)
[1] 0.5441406
>
> source("xlist5")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 6.151567
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.008323233
> asjd(xlist)
[1] 0.5366647

```

2.1.1.11 case 11 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 10$ with fixed bandwidth

$b_n = 1$



Accepted 23997 out of 100000 (23.997%).

final beta = 0.765112

alpha(0.000000) is 0.283786
alpha(2.000000) is 0.143202
alpha(5.000000) is 0.030523
alpha(10.000000) is 0.002805
alpha(20.000000) is 0.000000
alpha(50.000000) is 0.000000
alpha(100.000000) is 0.000000
alpha(150.000000) is 0.000000
it takes 214.196000 seconds to run the adaptation algorithm
it takes 67.179000 seconds to compute g and sigma
it takes 23.495000 seconds to generate the first Markov Chain
it takes 20.797000 seconds to generate the second Markov Chain
it takes 21.091000 seconds to generate the third Markov Chain
it takes 27.039000 seconds to generate the fourth Markov Chain
it takes 19.527000 seconds to generate the fifth Markov Chain
it takes 2947.240000 seconds to test the local acceptance

|

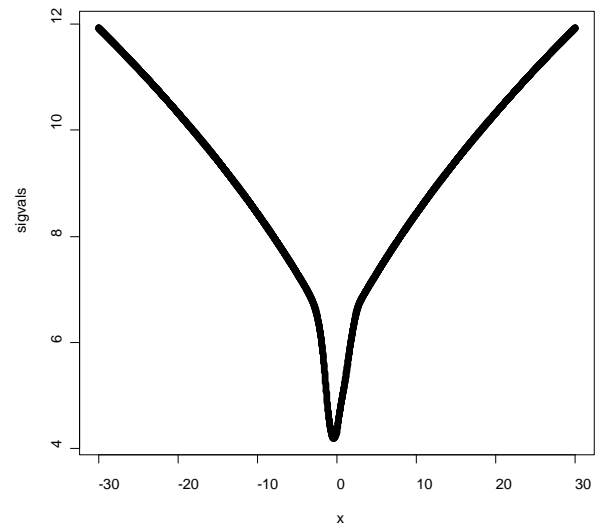
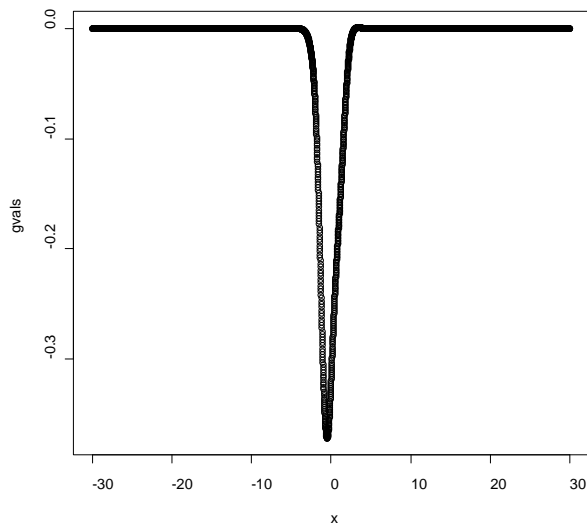
```

> asjd(xlist)
[1] 0.3507836
>
> source("xlist2")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 11.71392
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.01135253
> asjd(xlist)
[1] 0.355038
>
> source("xlist3")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 10.21051
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.01073888
> asjd(xlist)
[1] 0.3733516
>
> source("xlist4")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 10.77967
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.01113413
> asjd(xlist)
[1] 0.3672165
>
> source("xlist5")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 10.77254
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.01087192
> asjd(xlist)
[1] 0.3593188

```

2.1.1.12 case 12 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 0.5$ with fixed bandwidth

$$b_n = 1$$



Accepted 23701 out of 100000 (23.701%).

final beta = 1.785324

alpha(0.000000) is 0.206467

alpha(2.000000) is 0.285679

alpha(5.000000) is 0.432219

alpha(10.000000) is 0.494165

alpha(20.000000) is 0.491928

alpha(50.000000) is 0.505376

alpha(100.000000) is 0.495385

alpha(150.000000) is 0.497050

it takes 396.720000 seconds to run the adaptation algorithm

it takes 202.050000 seconds to compute g and sigma

it takes 118.802704 seconds to generate the first Markov Chain

it takes 120.982704 seconds to generate the second Markov Chain

it takes 120.712704 seconds to generate the third Markov Chain

it takes 118.832704 seconds to generate the fourth Markov Chain

it takes 121.202704 seconds to generate the fifth Markov Chain

it takes -1983.704592 seconds to test the local acceptance

1

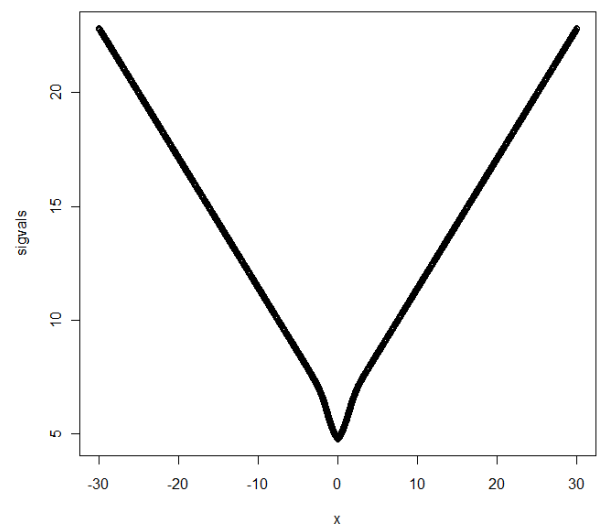
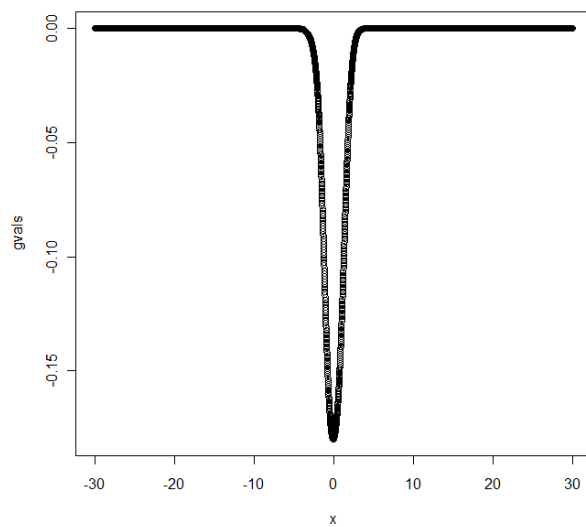
```

> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.008346926
> asjd(xlist)
[1] 0.5154546
>
> source("xlist4")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 6.739889
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.00864459
> asjd(xlist)
[1] 0.5293424
>
> source("xlist5")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 6.701922
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.00869634
> asjd(xlist)
[1] 0.5233073

```

2.1.1.13 case 13 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 1$ with fixed bandwidth

$b_n = 1$



Accepted 21399 out of 100000 (21.399%).

final beta = 1.741715

alpha(0.000000) is 0.187300

alpha(2.000000) is 0.261245

alpha(5.000000) is 0.379365

alpha(10.000000) is 0.467408

alpha(20.000000) is 0.486090

alpha(50.000000) is 0.496151

alpha(100.000000) is 0.498099

alpha(150.000000) is 0.494002

it takes 393.160000 seconds to run the adaptation algorithm

it takes 203.950000 seconds to compute g and sigma

it takes 93.012704 seconds to generate the first Markov Chain

it takes 94.202704 seconds to generate the second Markov Chain

it takes 90.432704 seconds to generate the third Markov Chain

it takes 88.402704 seconds to generate the fourth Markov Chain

it takes 88.382704 seconds to generate the fifth Markov Chain

it takes 1974.234592 seconds to test the local acceptance

|

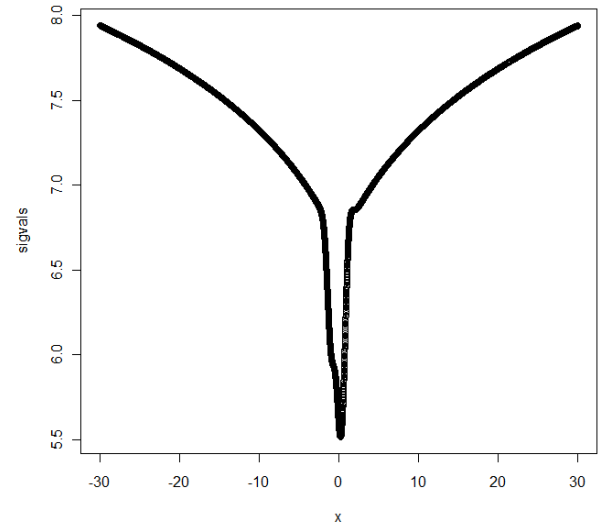
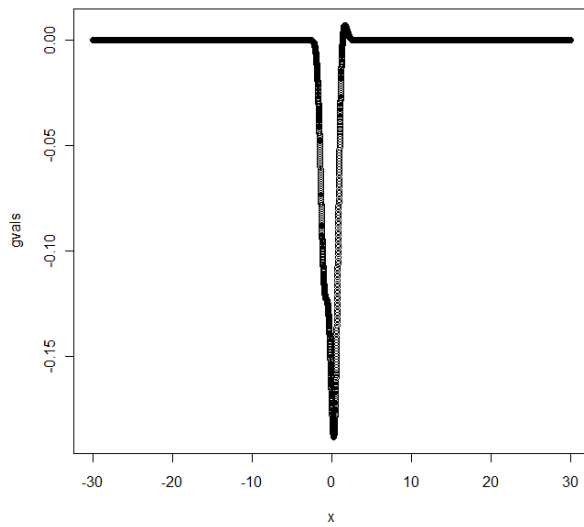
```

[1] 0.008915139
> asjd(xlist)
[1] 0.4866257
>
> source("xlist2")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 7.440486
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.009014073
> asjd(xlist)
[1] 0.4721054
>
> source("xlist3")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 7.480085
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.009195997
> asjd(xlist)
[1] 0.4982576
>
> source("xlist4")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 7.304401
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.009095373
> asjd(xlist)
[1] 0.4961344
>
> source("xlist5")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 8.057888
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.009576378
> asjd(xlist)
[1] 0.4929519

```

2.1.1.14 case 14 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 0.1$ with fixed bandwidth

$b_n = 1$



Accepted 20686 out of 100000 (20.686%).

final beta = 1.892872

alpha(0.000000) is 0.168239

alpha(2.000000) is 0.273334

alpha(5.000000) is 0.440324

alpha(10.000000) is 0.502495

alpha(20.000000) is 0.499843

alpha(50.000000) is 0.496880

alpha(100.000000) is 0.498992

alpha(150.000000) is 0.500321

it takes 148.470000 seconds to run the adaptation algorithm

it takes 121.910000 seconds to compute g and sigma

it takes 16.530000 seconds to generate the first Markov Chain

it takes 16.430000 seconds to generate the second Markov Chain

it takes 16.540000 seconds to generate the third Markov Chain

it takes 16.620000 seconds to generate the fourth Markov Chain

it takes 16.720000 seconds to generate the fifth Markov Chain

it takes 1005.607296 seconds to test the local acceptance

1

```

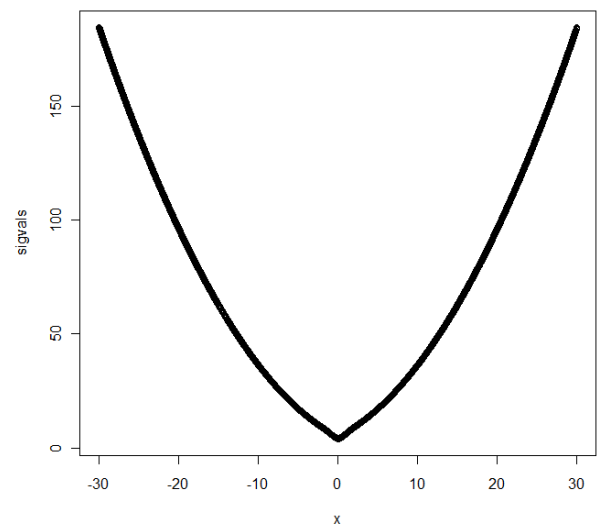
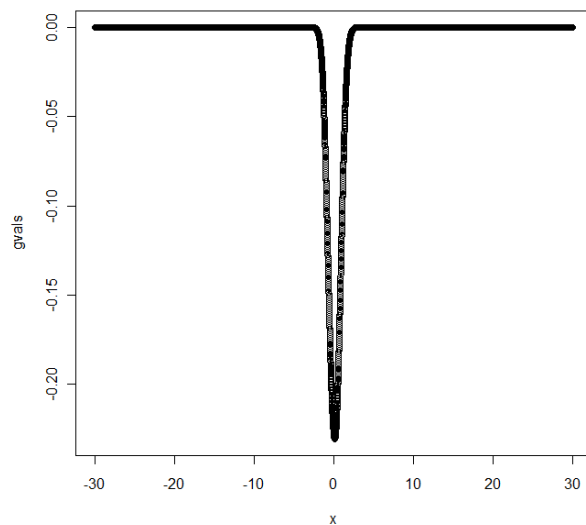
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.008678129
> asjd(xlist)
[1] 0.4830742
>
> source("xlist4")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 7.697511
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.009185244
> asjd(xlist)
[1] 0.4759112

>
> source("xlist5")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 7.061558
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.00885177
> asjd(xlist)
[1] 0.4897989

```

2.1.1.15 case 15 $\eta_n = \frac{1}{(n+5)^{0.8}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$$b_n = 1$$



Accepted 22330 out of 100000 (22.330%).

final beta = 1.633162
alpha(0.000000) is 0.202263
alpha(2.000000) is 0.267583
alpha(5.000000) is 0.311616
alpha(10.000000) is 0.334902
alpha(20.000000) is 0.306255
alpha(50.000000) is 0.206723
alpha(100.000000) is 0.125700
alpha(150.000000) is 0.088200
it takes 807.930000 seconds to run the adaptation algorithm
it takes 465.320000 seconds to compute g and sigma
it takes 168.840000 seconds to generate the first Markov Chain
it takes 168.350000 seconds to generate the second Markov Chain
it takes 168.410000 seconds to generate the third Markov Chain
it takes 168.490000 seconds to generate the fourth Markov Chain
it takes 168.340000 seconds to generate the fifth Markov Chain
it takes 1450.812704 seconds to test the local acceptance

|

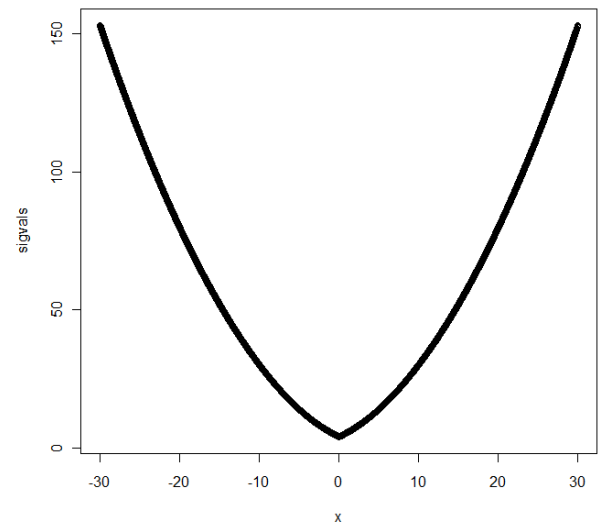
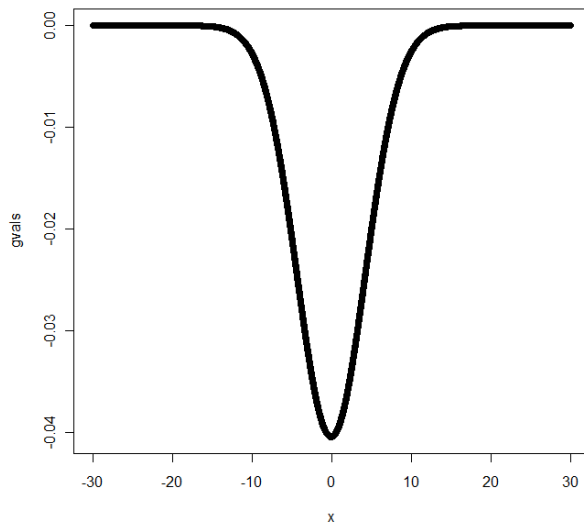
```

> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.008917038
> asjd(xlist)
[1] 0.4945916
>
> source("xlist2")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 7.612522
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.009193089
> asjd(xlist)
[1] 0.4812469
>
> source("xlist3")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 7.921151
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.009351136
> asjd(xlist)
[1] 0.4784871
>
> source("xlist4")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 7.508852
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.009159896
> asjd(xlist)
[1] 0.4711793
>
> source("xlist5")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 7.411572
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.009003102
> asjd(xlist)
[1] 0.4769998

```

2.1.1.16 case 16 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$b_n = 10$



Accepted 23891 out of 100000 (23.891%).

final beta = 1.447071

alpha(0.000000) is 0.212424

alpha(2.000000) is 0.299157

alpha(5.000000) is 0.375196

alpha(10.000000) is 0.394662

alpha(20.000000) is 0.350472

alpha(50.000000) is 0.243851

alpha(100.000000) is 0.150100

alpha(150.000000) is 0.109600

it takes 436.900000 seconds to run the adaptation algorithm

it takes 200.010000 seconds to compute g and sigma

it takes 168.410000 seconds to generate the first Markov Chain

it takes 168.390000 seconds to generate the second Markov Chain

it takes 168.310000 seconds to generate the third Markov Chain

it takes 168.250000 seconds to generate the fourth Markov Chain

it takes 168.680000 seconds to generate the fifth Markov Chain

it takes -1118.967296 seconds to test the local acceptance

1

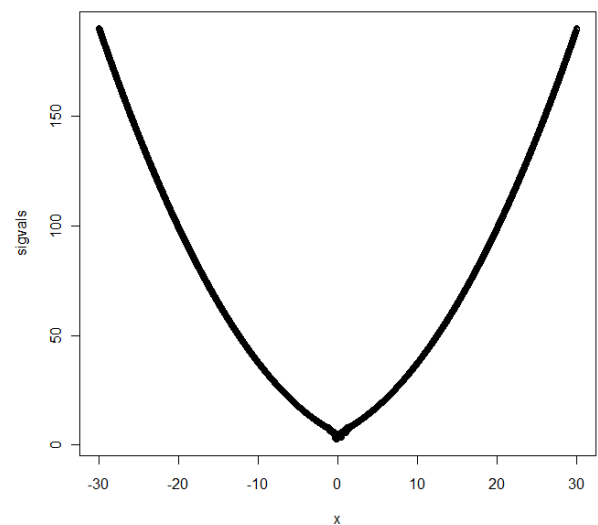
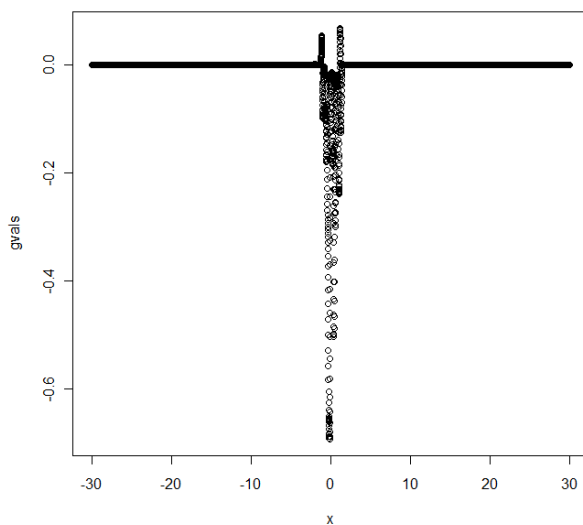
```

> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.008132099
> asjd(xlist)
[1] 0.5293508
>
> source("xlist4")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 6.549738
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.00844165
> asjd(xlist)
[1] 0.5197645
>
> source("xlist5")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 6.704092
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.008546772
> asjd(xlist)
[1] 0.5158363

```

2.1.1.17 case 17 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$b_n = 0.1$



Accepted 21377 out of 100000 (21.377%).

final beta = 1.664225

alpha(0.000000) is 0.180821

alpha(2.000000) is 0.232952

alpha(5.000000) is 0.308967

alpha(10.000000) is 0.331137

alpha(20.000000) is 0.304751

alpha(50.000000) is 0.198707

alpha(100.000000) is 0.112710

alpha(150.000000) is 0.084200

it takes 557.440000 seconds to run the adaptation algorithm

it takes 277.870000 seconds to compute g and sigma

it takes 168.700000 seconds to generate the first Markov Chain

it takes 168.520000 seconds to generate the second Markov Chain

it takes 168.430000 seconds to generate the third Markov Chain

it takes 168.420000 seconds to generate the fourth Markov Chain

it takes 168.310000 seconds to generate the fifth Markov Chain

it takes -559.027296 seconds to test the local acceptance

|

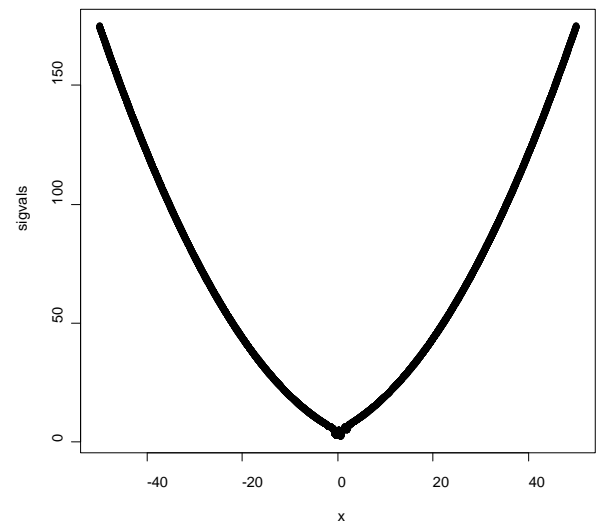
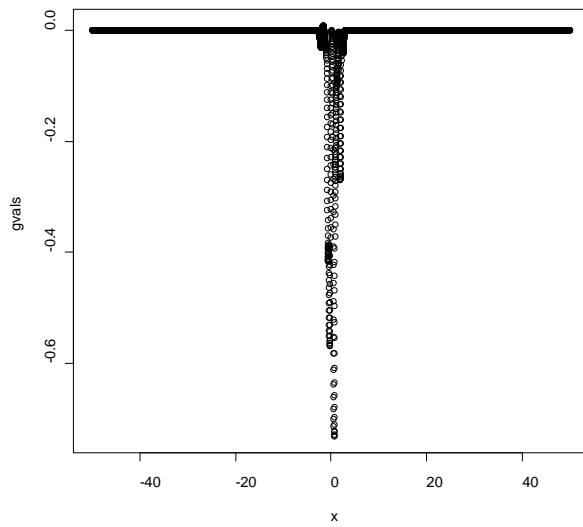
```

> asjd(xlist)
[1] 0.4587334
>
> source("xlist2")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 7.725935
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.009216995
> asjd(xlist)
[1] 0.4531863
>
> source("xlist3")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 8.350977
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.009555587
> asjd(xlist)
[1] 0.4569404
>
> source("xlist4")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 7.279248
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.008898774
> asjd(xlist)
[1] 0.4481364
>
> source("xlist5")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 7.577468
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.009148531
> asjd(xlist)
[1] 0.4577722

```

2.1.1.18 case 18 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with decreasing

bandwidth $b_n = \frac{1}{n^{0.2}}$



Accepted 23550 out of 100000 (23.550%).

final beta = 1.581161

alpha(0.000000) is 0.205731

alpha(2.000000) is 0.300010

alpha(5.000000) is 0.330864

alpha(10.000000) is 0.353506

alpha(20.000000) is 0.317601

alpha(50.000000) is 0.211646

alpha(100.000000) is 0.136600

alpha(150.000000) is 0.089400

it takes 248.510000 seconds to run the adaptation algorithm

it takes 155.567000 seconds to compute g and sigma

it takes 18.628000 seconds to generate the first Markov Chain

it takes 19.038000 seconds to generate the second Markov Chain

it takes 19.105000 seconds to generate the third Markov Chain

it takes 18.861000 seconds to generate the fourth Markov Chain

it takes 18.436000 seconds to generate the fifth Markov Chain

it takes 1793.310000 seconds to test the local acceptance

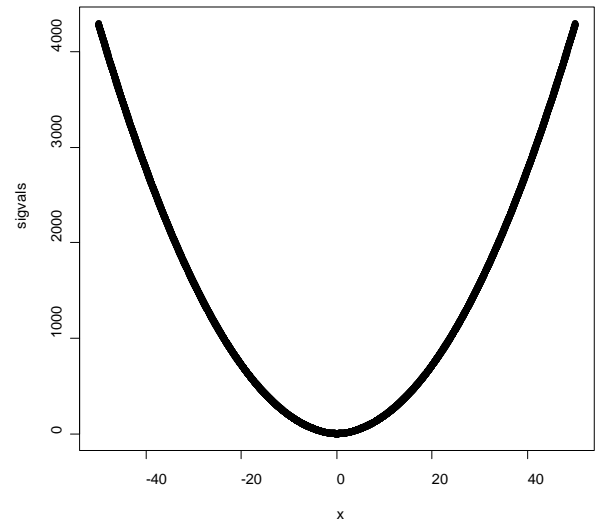
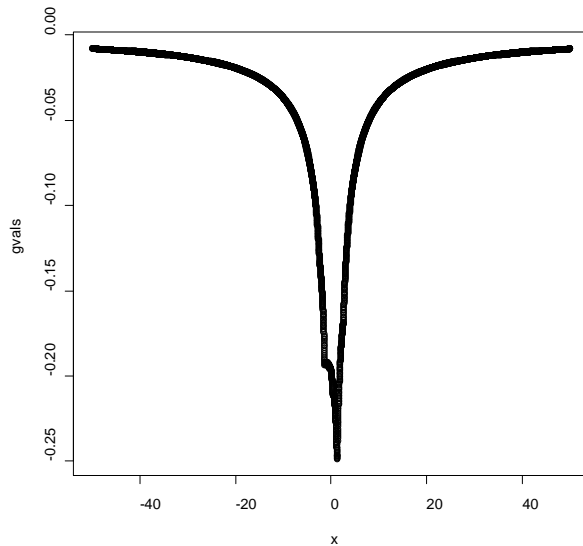
1

```
[1] 7.525139
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.009061946
> asjd(xlist)
[1] 0.4880344
>
> source("xlist4")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 7.189149
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.008921259
> asjd(xlist)
[1] 0.4885126
>
> source("xlist5")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 7.331579
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.008833732
> asjd(xlist)
[1] 0.4807859
```

```
>
```

2.1.2 kernel function $K(x) = \frac{1}{1 + \alpha_1 |x|^{\alpha_2}}$

2.1.2.1 case 19 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 23270 out of 100000 (23.270%).

final beta = 0.509653

alpha(0.000000) is 0.308718

alpha(2.000000) is 0.154510

alpha(5.000000) is 0.072492

alpha(10.000000) is 0.044654

alpha(20.000000) is 0.022523

alpha(50.000000) is 0.010300

alpha(100.000000) is 0.005800

alpha(150.000000) is 0.003400

it takes 182.254000 seconds to run the adaptation algorithm

it takes 79.529000 seconds to compute g and sigma

it takes 18.465000 seconds to generate the first Markov Chain

it takes 19.243000 seconds to generate the second Markov Chain

it takes 18.764000 seconds to generate the third Markov Chain

it takes 18.643000 seconds to generate the fourth Markov Chain

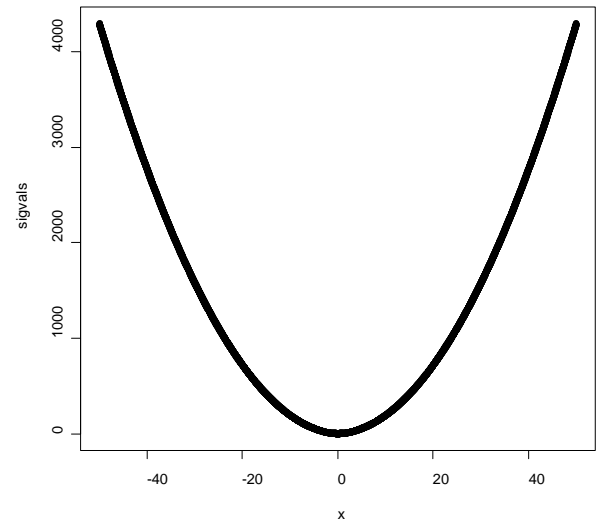
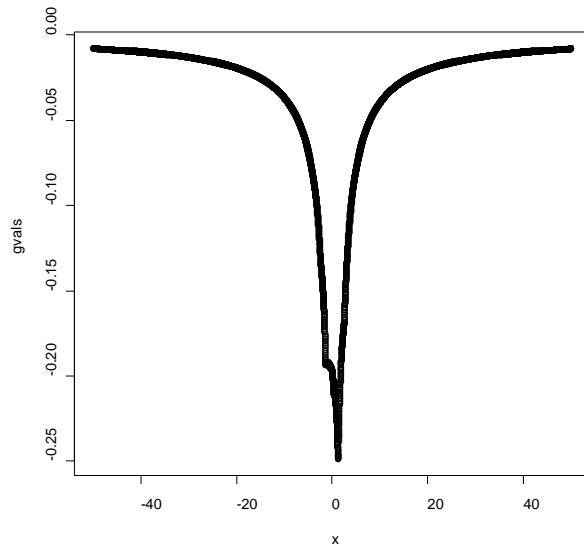
it takes 18.732000 seconds to generate the fifth Markov Chain

it takes 1417.510000 seconds to test the local acceptance

1

[1] 11.41702
[1] 0.01129308
[1] 0.3478964

2.1.2.2 case 20 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 23090 out of 100000 (23.090%).

final beta = 0.371945

alpha(0.000000) is 0.294688

alpha(2.000000) is 0.156616

alpha(5.000000) is 0.083929

alpha(10.000000) is 0.049232

alpha(20.000000) is 0.027440

alpha(50.000000) is 0.010606

alpha(100.000000) is 0.005000

alpha(150.000000) is 0.004300

it takes 182.737000 seconds to run the adaptation algorithm

it takes 79.860000 seconds to compute g and sigma

it takes 19.045000 seconds to generate the first Markov Chain

it takes 18.773000 seconds to generate the second Markov Chain

it takes 19.008000 seconds to generate the third Markov Chain

it takes 18.930000 seconds to generate the fourth Markov Chain

it takes 19.085000 seconds to generate the fifth Markov Chain

it takes 1412.770000 seconds to test the local acceptance

1

```
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M] ) );asjd(xlist[(B+1):M]);
```

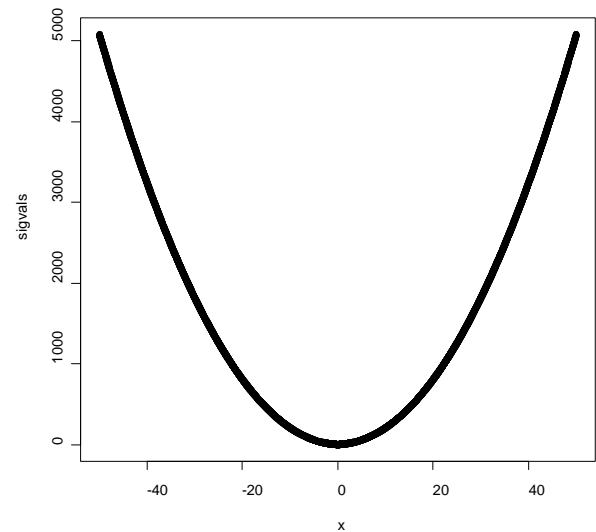
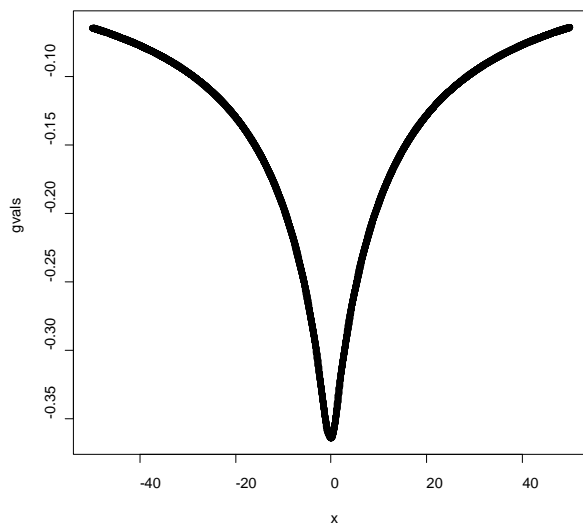
```
[1] 11.41702
```

```
[1] 0.01129308
```

```
[1] 0.3478964
```

2.1.2.3 case 21 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth

$b_n = 1$



Accepted 21634 out of 100000 (21.634%).

final beta = 0.733597

alpha(0.000000) is 0.283550

alpha(2.000000) is 0.132628

alpha(5.000000) is 0.071787

alpha(10.000000) is 0.038704

alpha(20.000000) is 0.018586

alpha(50.000000) is 0.008800

alpha(100.000000) is 0.003800

alpha(150.000000) is 0.002600

it takes 183.559000 seconds to run the adaptation algorithm

it takes 79.844000 seconds to compute g and sigma

it takes 20.529000 seconds to generate the first Markov Chain

it takes 21.000000 seconds to generate the second Markov Chain

it takes 19.672000 seconds to generate the third Markov Chain

it takes 19.536000 seconds to generate the fourth Markov Chain

it takes 19.809000 seconds to generate the fifth Markov Chain

it takes 1480.876000 seconds to test the local acceptance

1

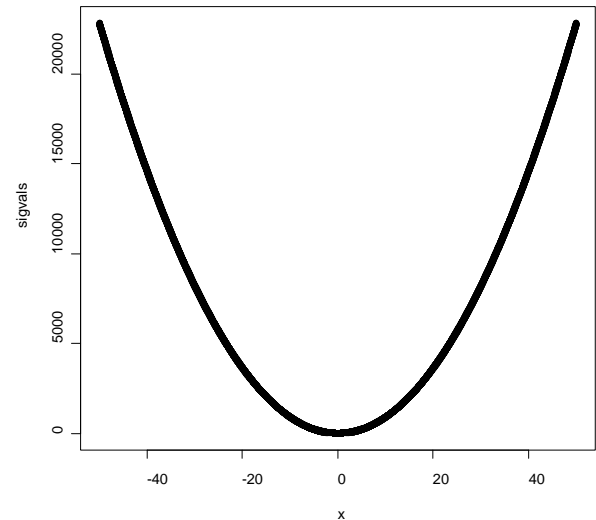
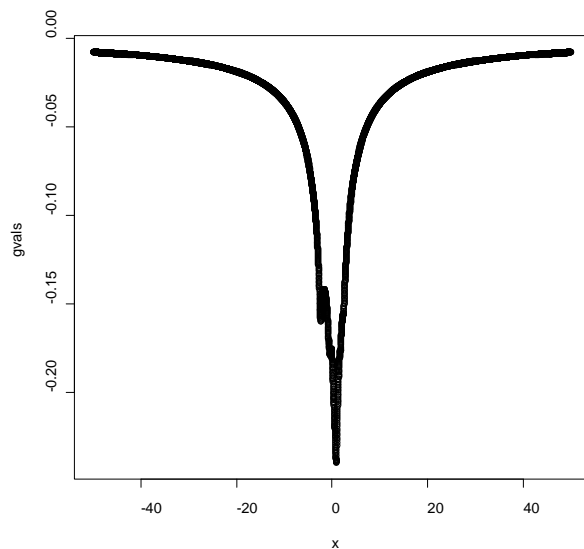
```
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
```

```
[1] 11.66403
```

```
[1] 0.01155291
```

```
[1] 0.3238721
```

2.1.2.4 case 22 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 10, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 23550 out of 100000 (23.550%).

final beta = -2.389302

alpha(0.000000) is 0.692987

alpha(2.000000) is 0.049448

alpha(5.000000) is 0.018691

alpha(10.000000) is 0.009739

alpha(20.000000) is 0.004700

alpha(50.000000) is 0.001200

alpha(100.000000) is 0.000700

alpha(150.000000) is 0.000400

it takes 189.708000 seconds to run the adaptation algorithm

it takes 82.037000 seconds to compute g and sigma

it takes 33.573000 seconds to generate the first Markov Chain

it takes 34.799000 seconds to generate the second Markov Chain

it takes 33.047000 seconds to generate the third Markov Chain

it takes 37.563000 seconds to generate the fourth Markov Chain

it takes 32.954000 seconds to generate the fifth Markov Chain

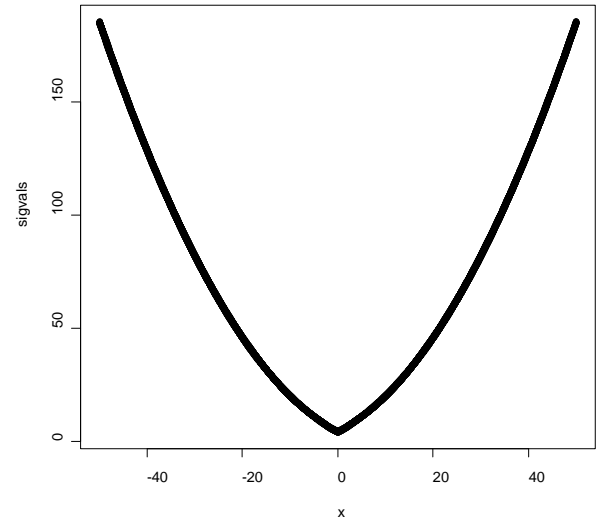
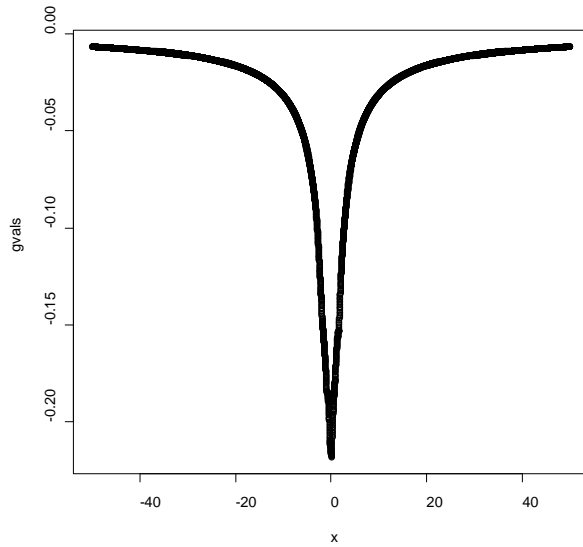
it takes 1589.008000 seconds to test the local acceptance

1

[1] 25.62197
[1] 0.01656713
[1] 0.1643911

2.1.2.5 case 23 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$b_n = 1$



Accepted 22407 out of 100000 (22.407%).

final beta = 1.644476

alpha(0.000000) is 0.194444

alpha(2.000000) is 0.275256

alpha(5.000000) is 0.325757

alpha(10.000000) is 0.347718

alpha(20.000000) is 0.304018

alpha(50.000000) is 0.199149

alpha(100.000000) is 0.123500

alpha(150.000000) is 0.093000

it takes 185.075000 seconds to run the adaptation algorithm

it takes 81.005000 seconds to compute g and sigma

it takes 18.974000 seconds to generate the first Markov Chain

it takes 19.055000 seconds to generate the second Markov Chain

it takes 19.158000 seconds to generate the third Markov Chain

it takes 19.246000 seconds to generate the fourth Markov Chain

it takes 19.145000 seconds to generate the fifth Markov Chain

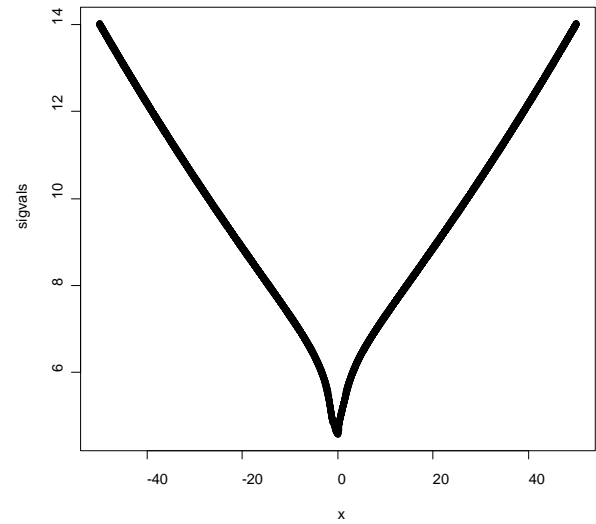
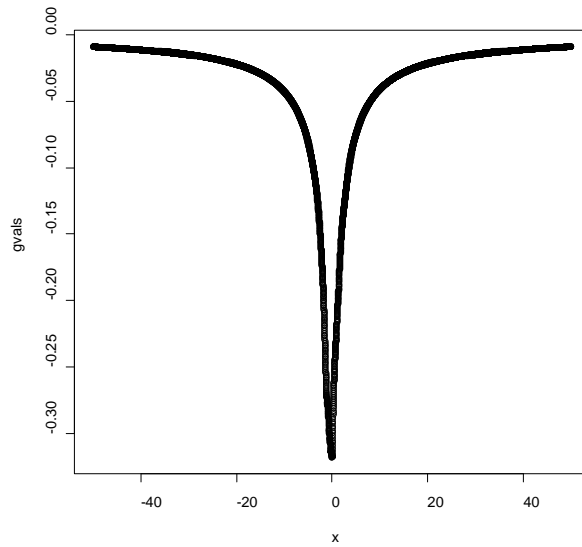
it takes 1080.022000 seconds to test the local acceptance

1

[1] 6.847748
[1] 0.008521907
[1] 0.4765741

2.1.2.6 case 24 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.01, \gamma = 2$ with fixed bandwidth

$b_n = 1$



Accepted 23657 out of 100000 (23.657%).

final beta = 1.838878

alpha(0.000000) is 0.200781

alpha(2.000000) is 0.309067

alpha(5.000000) is 0.451643

alpha(10.000000) is 0.498835

alpha(20.000000) is 0.495384

alpha(50.000000) is 0.492733

alpha(100.000000) is 0.499651

alpha(150.000000) is 0.505605

it takes 185.098000 seconds to run the adaptation algorithm

it takes 81.129000 seconds to compute g and sigma

it takes 19.323000 seconds to generate the first Markov Chain

it takes 19.333000 seconds to generate the second Markov Chain

it takes 19.919000 seconds to generate the third Markov Chain

it takes 19.601000 seconds to generate the fourth Markov Chain

it takes 19.271000 seconds to generate the fifth Markov Chain

it takes 822.868000 seconds to test the local acceptance

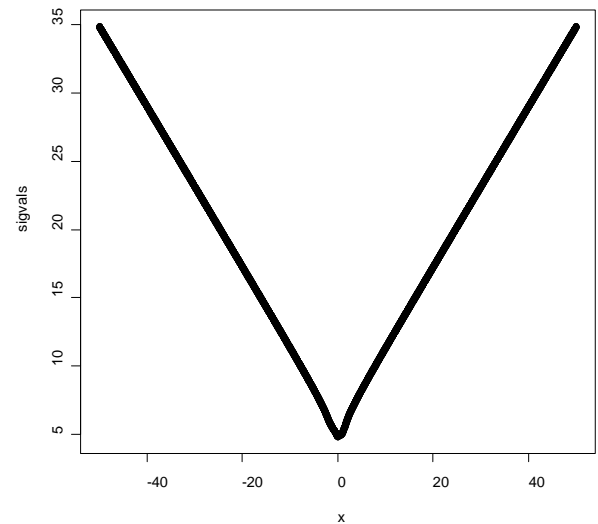
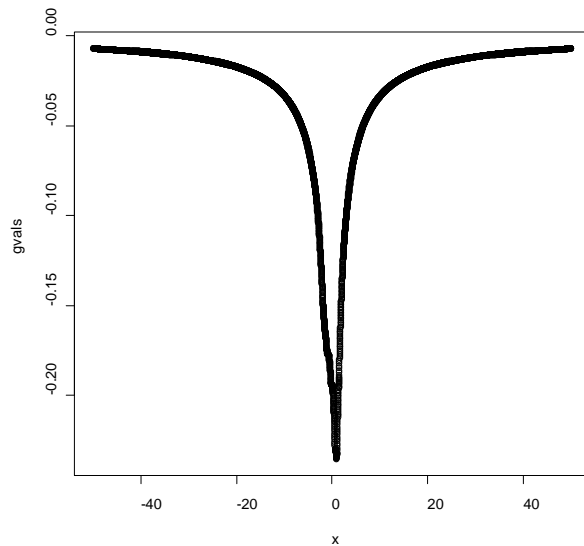
|

[1] 6.463722

[1] 0.008421049

[1] 0.5429365

2.1.2.7 case 25 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 1$ with fixed bandwidth $b_n = 1$



Accepted 22607 out of 100000 (22.607%).

final beta = 1.766949

alpha(0.000000) is 0.193104

alpha(2.000000) is 0.291302

alpha(5.000000) is 0.412738

alpha(10.000000) is 0.463710

alpha(20.000000) is 0.499346

alpha(50.000000) is 0.496252

alpha(100.000000) is 0.493020

alpha(150.000000) is 0.499200

it takes 188.056000 seconds to run the adaptation algorithm

it takes 81.384000 seconds to compute g and sigma

it takes 19.928000 seconds to generate the first Markov Chain

it takes 20.102000 seconds to generate the second Markov Chain

it takes 19.930000 seconds to generate the third Markov Chain

it takes 19.622000 seconds to generate the fourth Markov Chain

it takes 19.886000 seconds to generate the fifth Markov Chain

it takes 810.732000 seconds to test the local acceptance

1

```
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M] ));asjd(xlist[(B+1):M]);
```

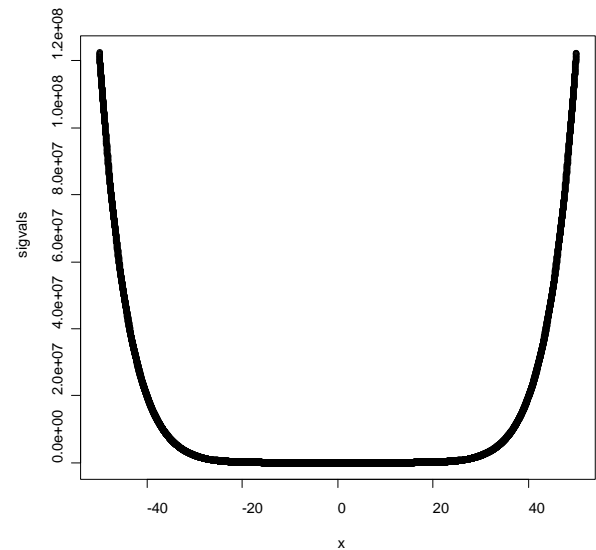
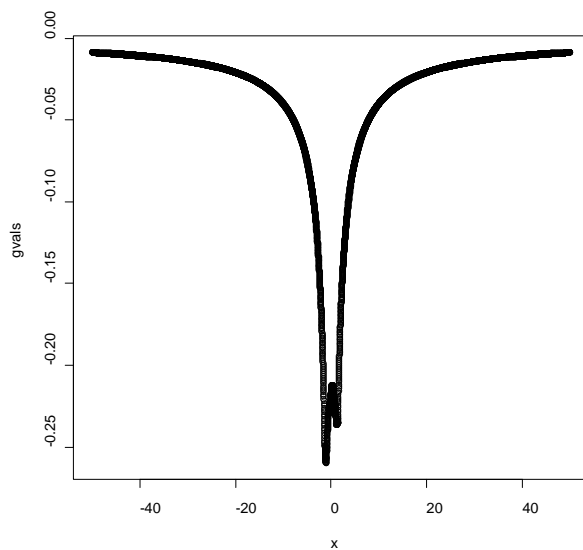
```
[1] 7.156546
```

```
[1] 0.009006958
```

```
[1] 0.5071021
```

2.1.2.8 case 26 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 10$ with fixed bandwidth

$b_n = 1$



Accepted 27588 out of 100000 (27.588%).

final beta = 0.714842

alpha(0.000000) is 0.323469

alpha(2.000000) is 0.179157

alpha(5.000000) is 0.038691

alpha(10.000000) is 0.004204

alpha(20.000000) is 0.000200

alpha(50.000000) is 0.000000

alpha(100.000000) is 0.000000

alpha(150.000000) is 0.000000

it takes 185.402000 seconds to run the adaptation algorithm

it takes 80.801000 seconds to compute g and sigma

it takes 20.724000 seconds to generate the first Markov Chain

it takes 28.117000 seconds to generate the second Markov Chain

it takes 20.586000 seconds to generate the third Markov Chain

it takes 20.432000 seconds to generate the fourth Markov Chain

it takes 20.293000 seconds to generate the fifth Markov Chain

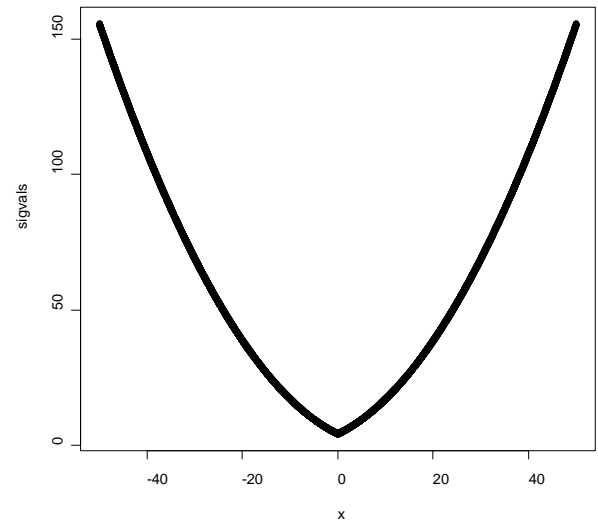
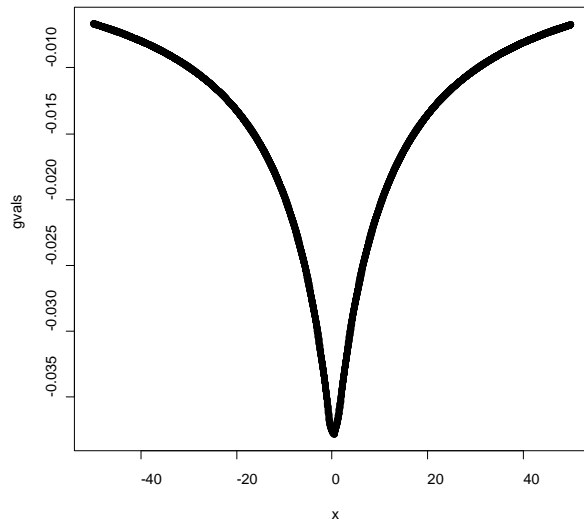
it takes 1514.924000 seconds to test the local acceptance

1

[1] 10.26327
[1] 0.01055025
[1] 0.3960828

2.1.2.9 case 27 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$b_n = 10$



Accepted 23321 out of 100000 (23.321%).

final beta = 1.470430

alpha(0.000000) is 0.201310

alpha(2.000000) is 0.301568

alpha(5.000000) is 0.366086

alpha(10.000000) is 0.380836

alpha(20.000000) is 0.352299

alpha(50.000000) is 0.239894

alpha(100.000000) is 0.155501

alpha(150.000000) is 0.105800

it takes 185.475000 seconds to run the adaptation algorithm

it takes 82.646000 seconds to compute g and sigma

it takes 18.919000 seconds to generate the first Markov Chain

it takes 18.652000 seconds to generate the second Markov Chain

it takes 18.690000 seconds to generate the third Markov Chain

it takes 18.640000 seconds to generate the fourth Markov Chain

it takes 18.789000 seconds to generate the fifth Markov Chain

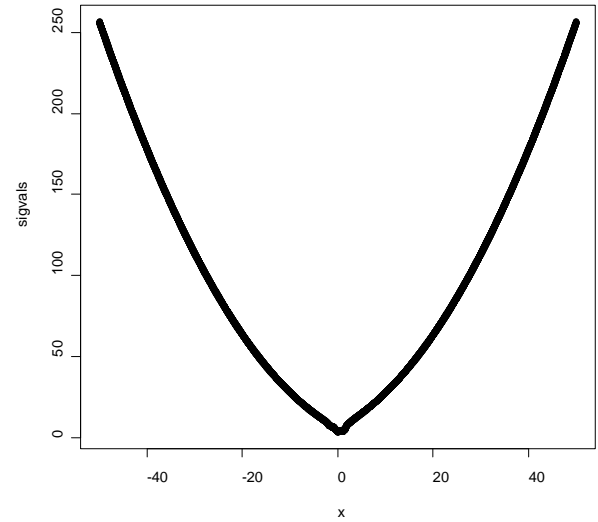
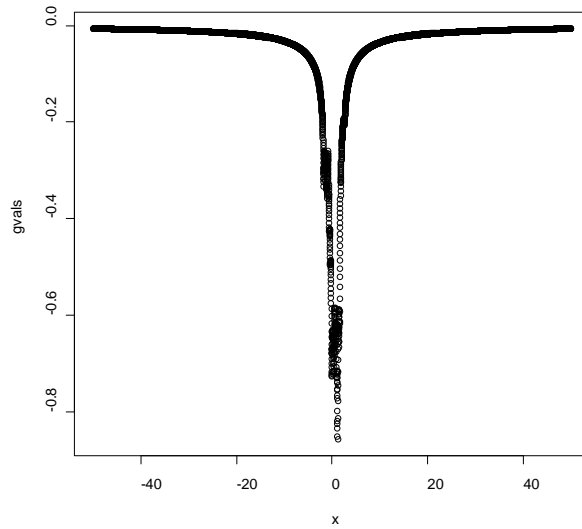
it takes 1089.644000 seconds to test the local acceptance

1

[1] 7.028814
[1] 0.008970417
[1] 0.5260427

2.1.2.10 case 28 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$b_n = 0.1$



Accepted 21876 out of 100000 (21.876%).

final beta = 1.970691

alpha(0.000000) is 0.202246

alpha(2.000000) is 0.235476

alpha(5.000000) is 0.255892

alpha(10.000000) is 0.268970

alpha(20.000000) is 0.234585

alpha(50.000000) is 0.152896

alpha(100.000000) is 0.091300

alpha(150.000000) is 0.063500

it takes 195.322000 seconds to run the adaptation algorithm

it takes 86.348000 seconds to compute g and sigma

it takes 25.162000 seconds to generate the first Markov Chain

it takes 25.307000 seconds to generate the second Markov Chain

it takes 25.162000 seconds to generate the third Markov Chain

it takes 24.111000 seconds to generate the fourth Markov Chain

it takes 22.829000 seconds to generate the fifth Markov Chain

it takes 1155.381000 seconds to test the local acceptance

1

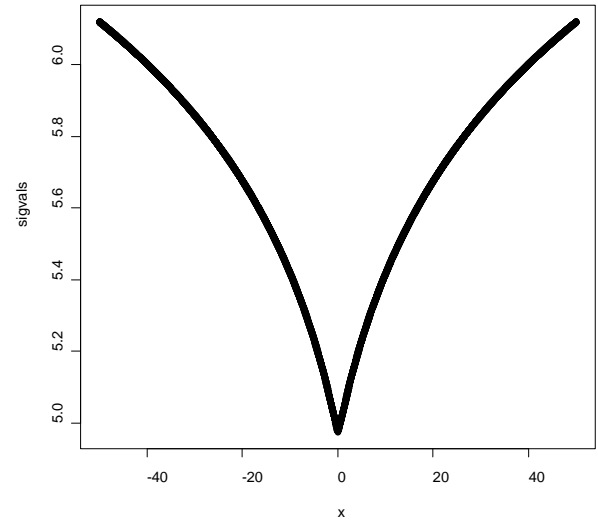
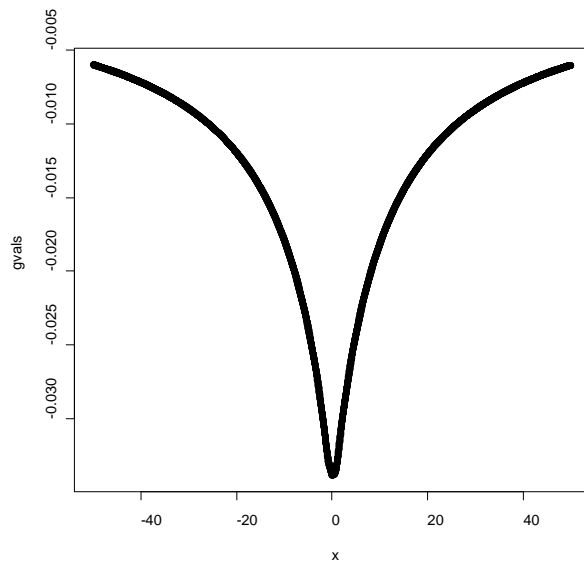
[1] 8.145908

[1] 0.009549854

[1] 0.4514627

2.1.2.11 case 29 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 0.1$ with fixed bandwidth

$b_n = 10$



Accepted 24039 out of 100000 (24.039%).

final beta = 1.638337

alpha(0.000000) is 0.194215

alpha(2.000000) is 0.331993

alpha(5.000000) is 0.488551

alpha(10.000000) is 0.496526

alpha(20.000000) is 0.499359

alpha(50.000000) is 0.505963

alpha(100.000000) is 0.508336

alpha(150.000000) is 0.507511

it takes 186.879000 seconds to run the adaptation algorithm

it takes 83.355000 seconds to compute g and sigma

it takes 20.056000 seconds to generate the first Markov Chain

it takes 19.361000 seconds to generate the second Markov Chain

it takes 19.535000 seconds to generate the third Markov Chain

it takes 19.817000 seconds to generate the fourth Markov Chain

it takes 19.696000 seconds to generate the fifth Markov Chain

it takes 858.514000 seconds to test the local acceptance

1

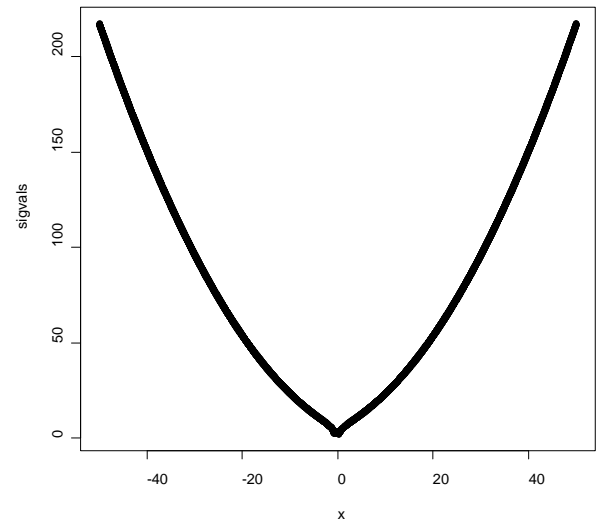
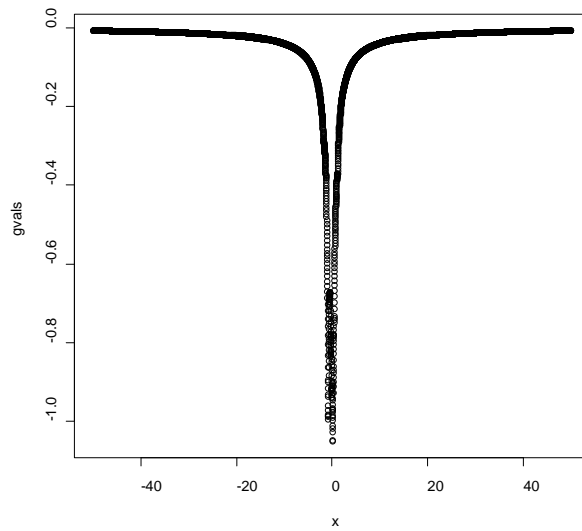
[1] 6.165894

[1] 0.008328171

[1] 0.5697796

2.1.2.12 case 30 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 2$ with decreasing bandwidth

$$b_n = \frac{1}{n^{0.2}}$$



Accepted 26457 out of 100000 (26.457%).

final beta = 1.805474

alpha(0.000000) is 0.269674

alpha(2.000000) is 0.249986

alpha(5.000000) is 0.293759

alpha(10.000000) is 0.307941

alpha(20.000000) is 0.279936

alpha(50.000000) is 0.176204

alpha(100.000000) is 0.109100

alpha(150.000000) is 0.075300

it takes 194.183000 seconds to run the adaptation algorithm

it takes 86.661000 seconds to compute g and sigma

it takes 24.157000 seconds to generate the first Markov Chain

it takes 23.538000 seconds to generate the second Markov Chain

it takes 23.525000 seconds to generate the third Markov Chain

it takes 23.575000 seconds to generate the fourth Markov Chain

it takes 23.875000 seconds to generate the fifth Markov Chain

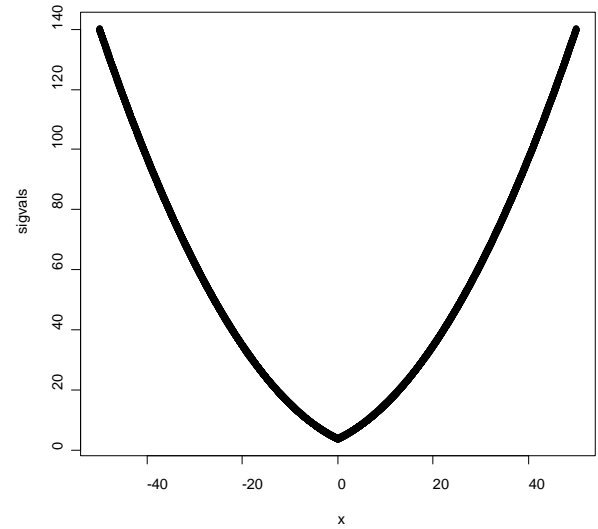
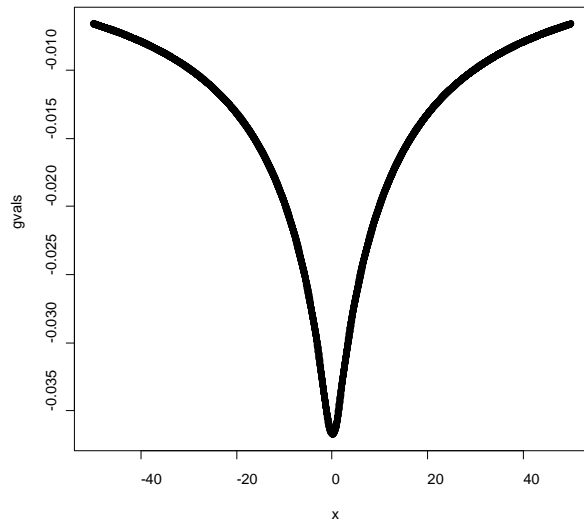
it takes 1177.590000 seconds to test the local acceptance

1

[1] 6.940457
[1] 0.008799531
[1] 0.4994858

2.1.2.13 case 31 $\eta_n = \frac{1}{(n+5)^{0.8}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$b_n = 10$



Accepted 25724 out of 100000 (25.724%).

final beta = 1.365579

alpha(0.000000) is 0.221199

alpha(2.000000) is 0.320933

alpha(5.000000) is 0.391188

alpha(10.000000) is 0.401987

alpha(20.000000) is 0.378950

alpha(50.000000) is 0.264811

alpha(100.000000) is 0.163500

alpha(150.000000) is 0.120201

it takes 195.386000 seconds to run the adaptation algorithm

it takes 87.578000 seconds to compute g and sigma

it takes 24.496000 seconds to generate the first Markov Chain

it takes 24.224000 seconds to generate the second Markov Chain

it takes 24.354000 seconds to generate the third Markov Chain

it takes 24.327000 seconds to generate the fourth Markov Chain

it takes 24.485000 seconds to generate the fifth Markov Chain

it takes 1079.685000 seconds to test the local acceptance

1

[1] 6.246366

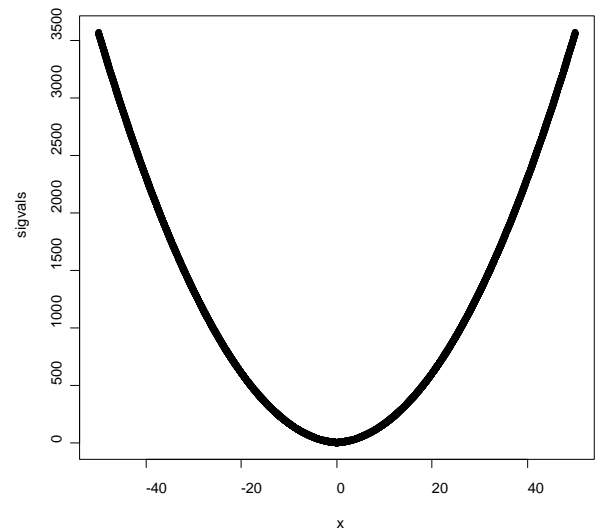
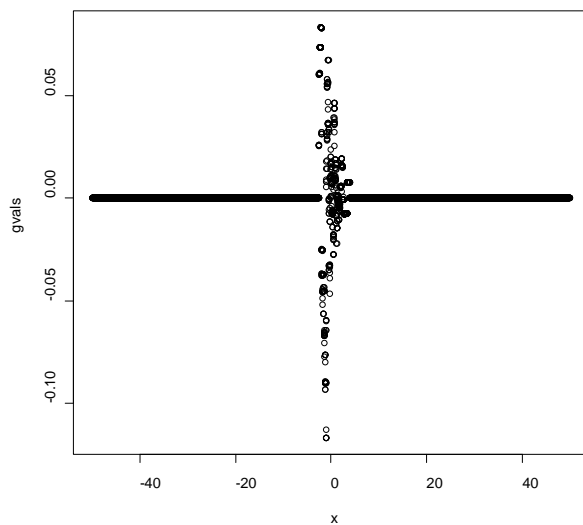
[1] 0.008281501

[1] 0.5653669

2.1.3 kernel function
$$K(x) = \begin{cases} 0, & |x| \geq 2 * width \\ -1 * height, & width < |x| < 2 * width \\ 1 * height, & |x| \leq width \end{cases}$$

2.1.3.1 case 32 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $height = 0.5$, $width = 0.5$, $C = 1$, $\gamma = 2$ with fixed

bandwidth $b_n = 1$



Accepted 23241 out of 100000 (23.241%).

final beta = 0.317424

alpha(0.000000) is 0.294893

alpha(2.000000) is 0.148025

alpha(5.000000) is 0.085389

alpha(10.000000) is 0.049931

alpha(20.000000) is 0.026705

alpha(50.000000) is 0.012373

alpha(100.000000) is 0.006300

alpha(150.000000) is 0.003200

it takes 124.035000 seconds to run the adaptation algorithm

it takes 54.897000 seconds to compute g and sigma

it takes 18.362000 seconds to generate the first Markov Chain

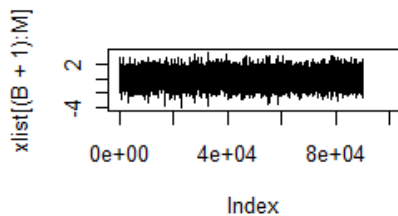
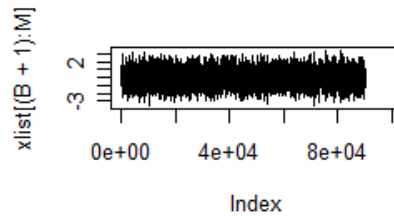
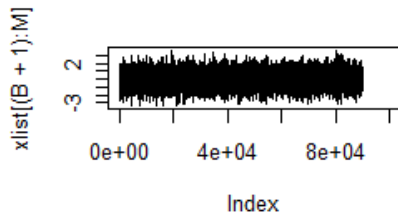
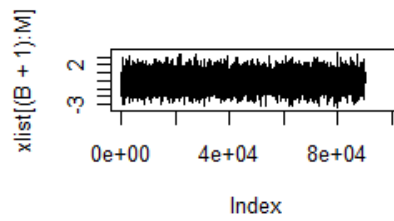
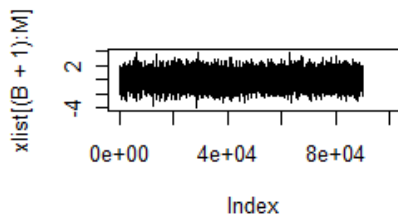
it takes 18.330000 seconds to generate the second Markov Chain

it takes 18.314000 seconds to generate the third Markov Chain

it takes 18.892000 seconds to generate the fourth Markov Chain

it takes 18.439000 seconds to generate the fifth Markov Chain

it takes 972.911000 seconds to test the local acceptance



```

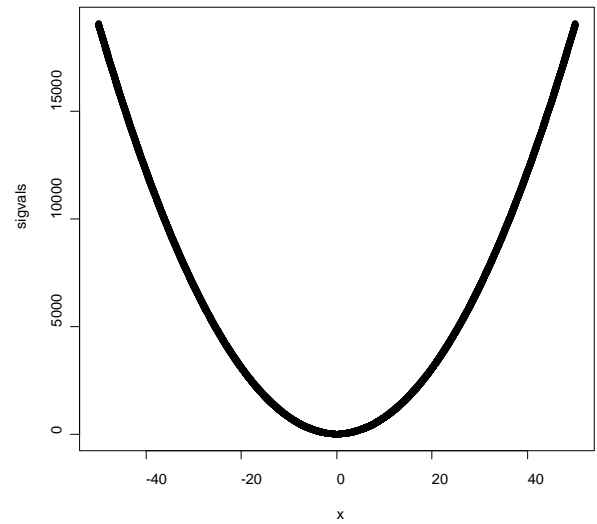
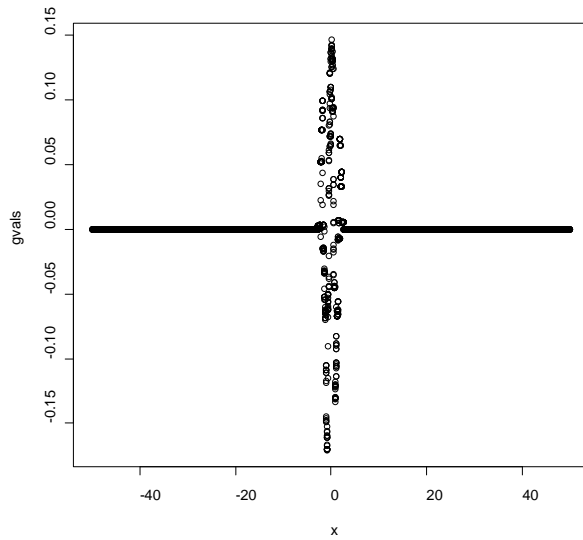
> source("xlist1");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 11.21697
[1] 0.01119531
[1] 0.3480791
> source("xlist2");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 11.01346
[1] 0.01102779
[1] 0.3393188
> source("xlist3");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 10.73923
[1] 0.01097638
[1] 0.3521589
> source("xlist4");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 11.00212
[1] 0.01111038
[1] 0.3414209
> source("xlist5");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);

```

[1] 10.74114
 [1] 0.01082565
 [1] 0.3407953

2.1.3.2 case 33 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.5, width = 0.5, C = 10, $\gamma = 2$ with fixed

bandwidth $b_n = 1$



Accepted 23196 out of 100000 (23.196%).

final beta = -2.577837

alpha(0.000000) is 0.648993

alpha(2.000000) is 0.050936

alpha(5.000000) is 0.019636

alpha(10.000000) is 0.012347

alpha(20.000000) is 0.004800

alpha(50.000000) is 0.002700

alpha(100.000000) is 0.001300

alpha(150.000000) is 0.000500

it takes 128.638000 seconds to run the adaptation algorithm

it takes 56.695000 seconds to compute g and sigma

it takes 29.910000 seconds to generate the first Markov Chain

it takes 30.054000 seconds to generate the second Markov Chain

it takes 28.054000 seconds to generate the third Markov Chain

it takes 29.111000 seconds to generate the fourth Markov Chain

it takes 32.262000 seconds to generate the fifth Markov Chain

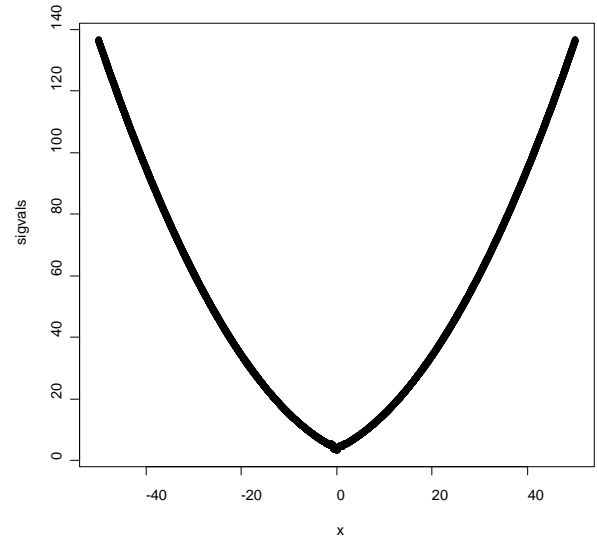
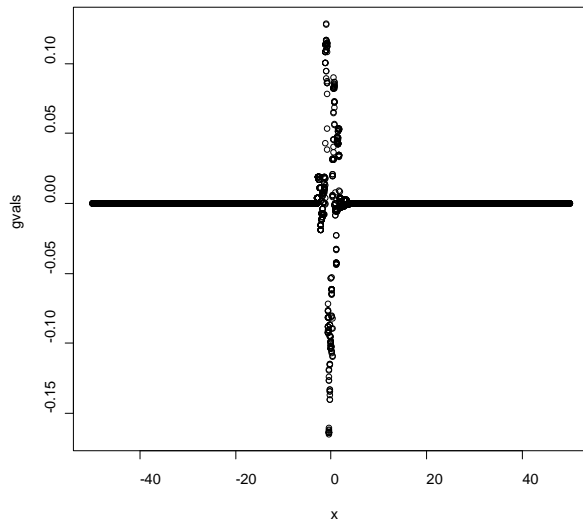
it takes 1103.764000 seconds to test the local acceptance

1

[1] 27.30234
[1] 0.01750065
[1] 0.1734251

2.1.3.3 case 34 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $height = 0.5$, $width = 0.5$, $C = 0.1$, $\gamma = 2$ with fixed

bandwidth $b_n = 1$



Accepted 25450 out of 100000 (25.450%).

final beta = 1.333309

alpha(0.000000) is 0.230635

alpha(2.000000) is 0.321085

alpha(5.000000) is 0.392833

alpha(10.000000) is 0.407148

alpha(20.000000) is 0.374904

alpha(50.000000) is 0.263909

alpha(100.000000) is 0.164500

alpha(150.000000) is 0.118700

it takes 129.268000 seconds to run the adaptation algorithm

it takes 56.751000 seconds to compute g and sigma

it takes 19.518000 seconds to generate the first Markov Chain

it takes 19.386000 seconds to generate the second Markov Chain

it takes 19.124000 seconds to generate the third Markov Chain

it takes 19.121000 seconds to generate the fourth Markov Chain

it takes 19.110000 seconds to generate the fifth Markov Chain

it takes 724.909000 seconds to test the local acceptance

1

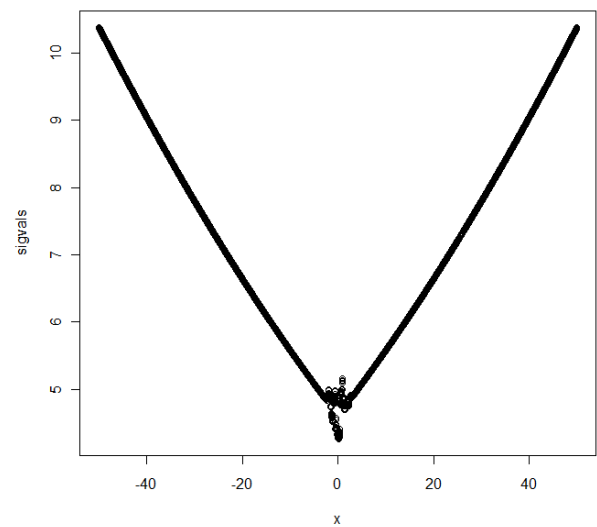
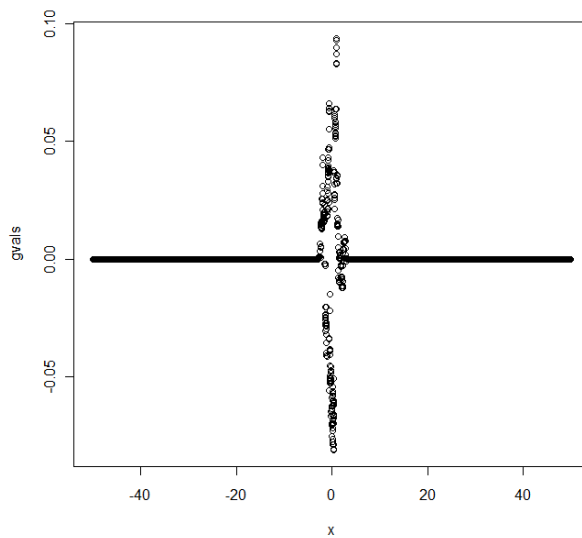

```

[1] 6.348009
[1] 0.008311205
[1] 0.5478521
> source("xlist5");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 6.251577
[1] 0.008308611
[1] 0.5388973

```

2.1.3.4 case 35 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $height = 0.5$, $width = 0.5$, $C = 0.01$, $\gamma = 2$ with fixed

bandwidth $b_n = 1$



Accepted 25285 out of 100000 (25.285%).

final beta = 1.528678

alpha(0.000000) is 0.211206

alpha(2.000000) is 0.355405

alpha(5.000000) is 0.499102

alpha(10.000000) is 0.505651

alpha(20.000000) is 0.502005

alpha(50.000000) is 0.502010

alpha(100.000000) is 0.497914

alpha(150.000000) is 0.508727

it takes 129.425000 seconds to run the adaptation algorithm

it takes 57.572000 seconds to compute g and sigma

it takes 19.149000 seconds to generate the first Markov Chain

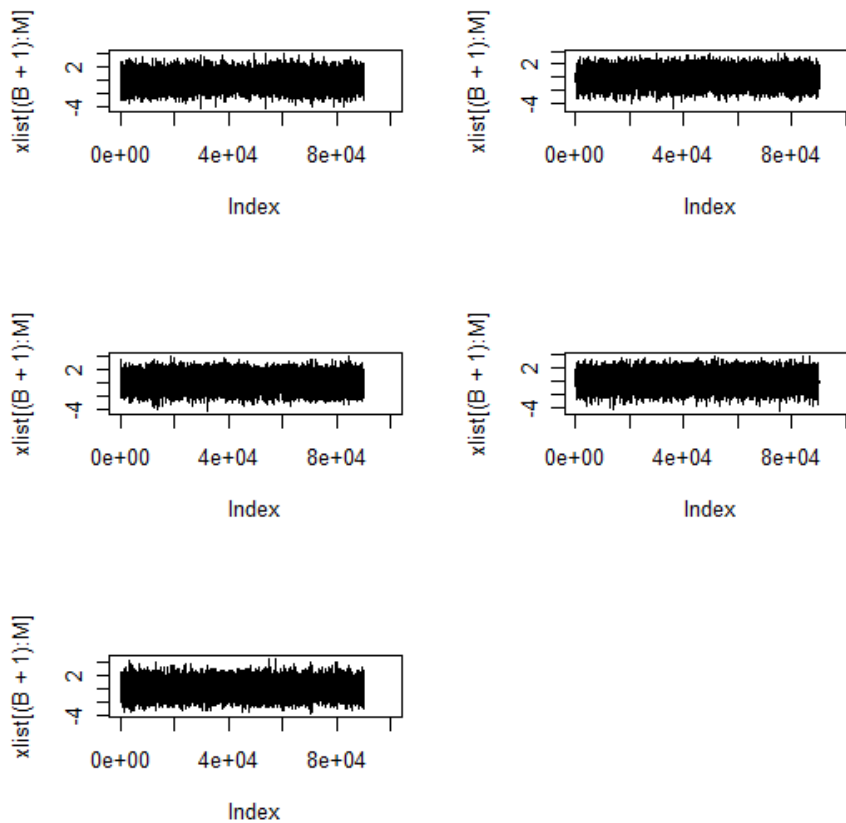
it takes 18.673000 seconds to generate the second Markov Chain

it takes 19.200000 seconds to generate the third Markov Chain

it takes 18.676000 seconds to generate the fourth Markov Chain

it takes 18.608000 seconds to generate the fifth Markov Chain

it takes 586.823000 seconds to test the local acceptance



```
> source("xlist1");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /  
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);  
[1] 5.714605  
[1] 0.007964564  
[1] 0.5832376  
> source("xlist2");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /  
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);  
[1] 6.093879  
[1] 0.008183764  
[1] 0.5765046  
> source("xlist3");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /  
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);  
[1] 6.027745  
[1] 0.008146571  
[1] 0.5731739  
> source("xlist4");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /  
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);  
[1] 5.876299  
[1] 0.008100663  
[1] 0.5905011
```

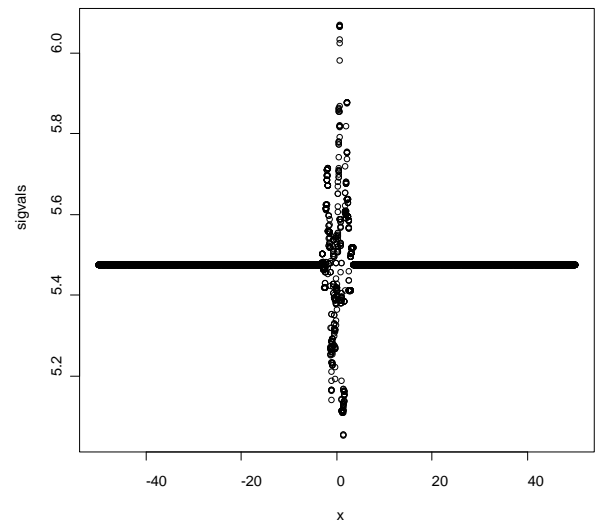
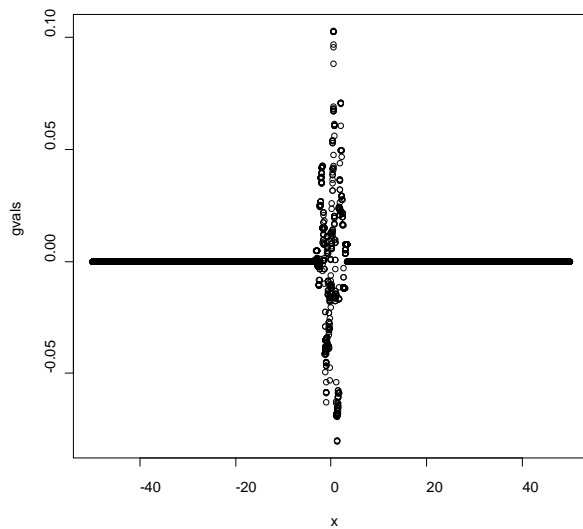
```

> source("xlist5");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 6.161878
[1] 0.008257061
[1] 0.5782485

```

2.1.3.5 case 36 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $height = 0.5$, $width = 0.5$, $C = 0$, $\gamma = 2$ with fixed

bandwidth $b_n = 1$



Accepted 22366 out of 100000 (22.366%).

final beta = 1.700274

alpha(0.000000) is 0.180320

alpha(2.000000) is 0.318118

alpha(5.000000) is 0.483259

alpha(10.000000) is 0.498034

alpha(20.000000) is 0.502090

alpha(50.000000) is 0.506030

alpha(100.000000) is 0.508454

alpha(150.000000) is 0.500686

it takes 127.853000 seconds to run the adaptation algorithm

it takes 56.083000 seconds to compute g and sigma

it takes 19.049000 seconds to generate the first Markov Chain

it takes 18.718000 seconds to generate the second Markov Chain

it takes 18.813000 seconds to generate the third Markov Chain

it takes 18.679000 seconds to generate the fourth Markov Chain

it takes 18.793000 seconds to generate the fifth Markov Chain

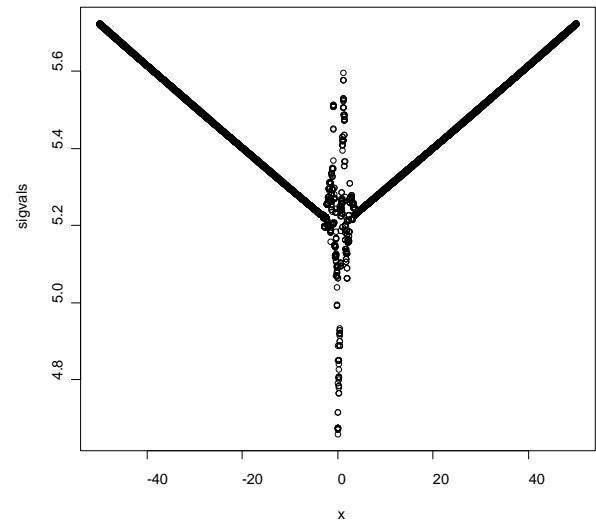
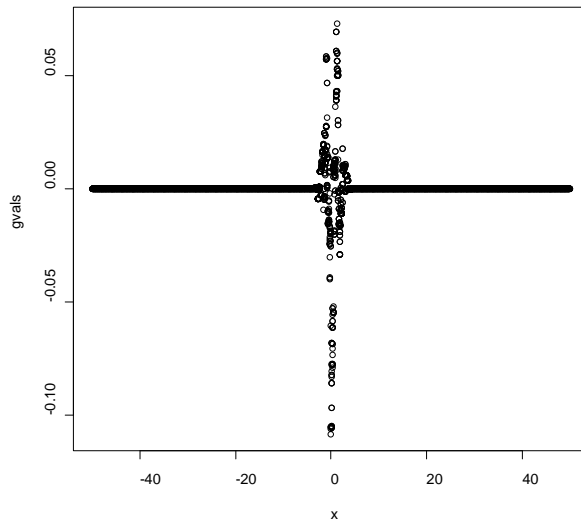
it takes 584.083000 seconds to test the local acceptance

1

[1] 6.861094
[1] 0.008786732
[1] 0.5409318

2.1.3.6 case 37 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $height = 0.5$, $width = 0.5$, $C = 0.001$, $\gamma = 2$ with fixed

bandwidth $b_n = 1$



Accepted 23124 out of 100000 (23.124%).

final beta = 1.646878

alpha(0.000000) is 0.194871

alpha(2.000000) is 0.334081

alpha(5.000000) is 0.494616

alpha(10.000000) is 0.501907

alpha(20.000000) is 0.503077

alpha(50.000000) is 0.499887

alpha(100.000000) is 0.495402

alpha(150.000000) is 0.496685

it takes 127.753000 seconds to run the adaptation algorithm

it takes 56.661000 seconds to compute g and sigma

it takes 19.610000 seconds to generate the first Markov Chain

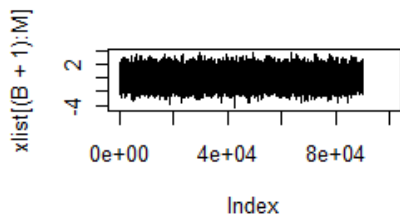
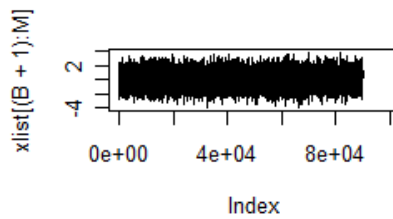
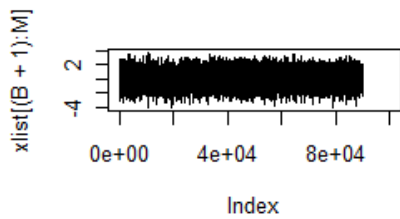
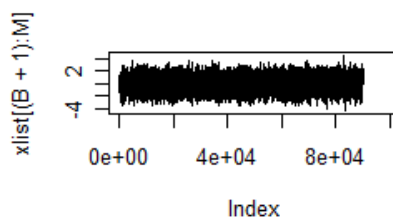
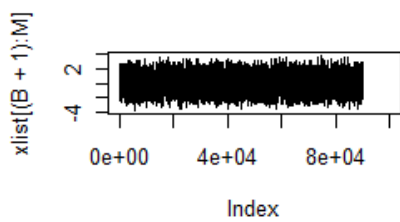
it takes 19.572000 seconds to generate the second Markov Chain

it takes 19.451000 seconds to generate the third Markov Chain

it takes 20.123000 seconds to generate the fourth Markov Chain

it takes 19.345000 seconds to generate the fifth Markov Chain

it takes 589.808000 seconds to test the local acceptance



```

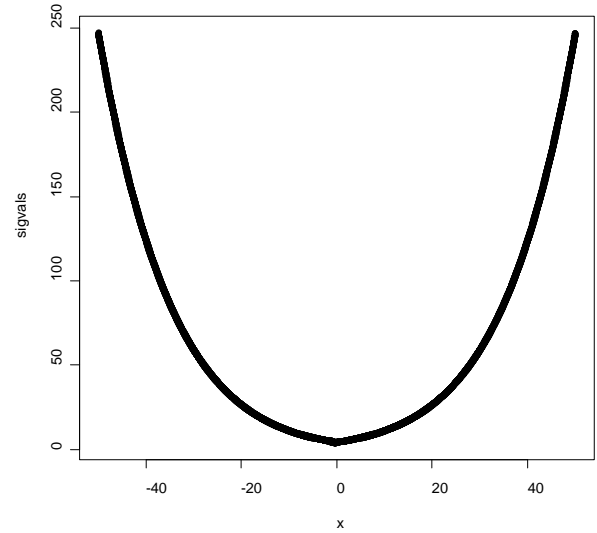
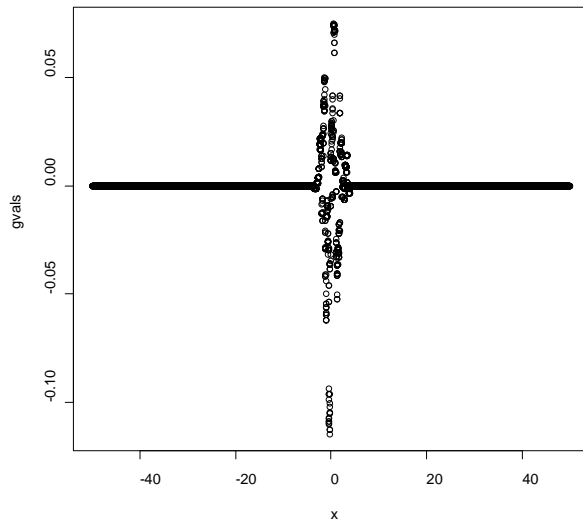
> source("xlist1");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 6.480792
[1] 0.008498191
[1] 0.5554767
> source("xlist2");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 6.665416
[1] 0.008673713
[1] 0.5492348
> source("xlist3");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 6.420364
[1] 0.008417142
[1] 0.5508303
> source("xlist4");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 6.372943
[1] 0.008327294
[1] 0.5473217
> source("xlist5");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);

```

[1] 6.769786
[1] 0.008624476
[1] 0.5400489

2.1.3.7 case 38 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $height = 0.5$, $width = 0.5$, $C = 0.001$, $\gamma = 10$ with fixed

bandwidth $b_n = 1$



Accepted 25144 out of 100000 (25.144%).

final beta = 1.454878

alpha(0.000000) is 0.211201

alpha(2.000000) is 0.331006

alpha(5.000000) is 0.434881

alpha(10.000000) is 0.469318

alpha(20.000000) is 0.432653

alpha(50.000000) is 0.158708

alpha(100.000000) is 0.018400

alpha(150.000000) is 0.002500

it takes 131.014000 seconds to run the adaptation algorithm

it takes 58.790000 seconds to compute g and sigma

it takes 21.423000 seconds to generate the first Markov Chain

it takes 19.720000 seconds to generate the second Markov Chain

it takes 19.325000 seconds to generate the third Markov Chain

it takes 19.330000 seconds to generate the fourth Markov Chain

it takes 20.172000 seconds to generate the fifth Markov Chain

it takes 794.188000 seconds to test the local acceptance

1

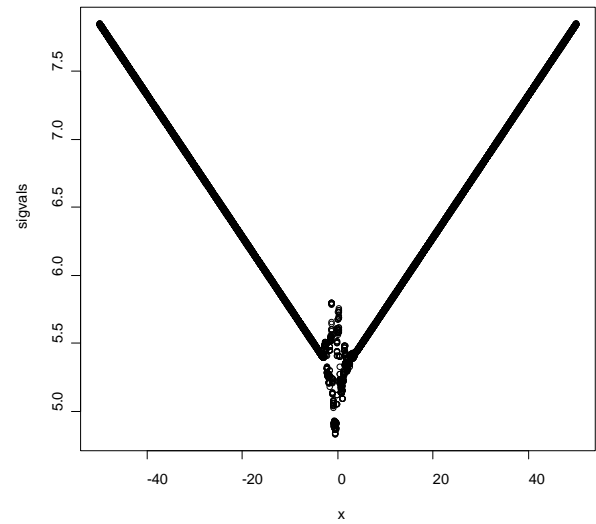
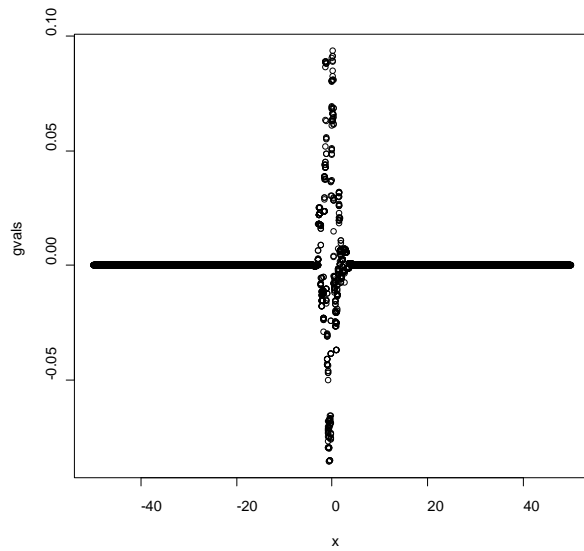
[1] 6.5259

[1] 0.008477031

[1] 0.55597

2.1.3.8 case 39 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $height = 0.5$, $width = 0.5$, $C = 0.001$, $\gamma = 1$ with fixed

bandwidth $b_n = 1$



Accepted 23332 out of 100000 (23.332%).

final beta = 1.655068

alpha(0.000000) is 0.188214

alpha(2.000000) is 0.329689

alpha(5.000000) is 0.483880

alpha(10.000000) is 0.511928

alpha(20.000000) is 0.509062

alpha(50.000000) is 0.497378

alpha(100.000000) is 0.497785

alpha(150.000000) is 0.505373

it takes 127.757000 seconds to run the adaptation algorithm

it takes 56.383000 seconds to compute g and sigma

it takes 19.888000 seconds to generate the first Markov Chain

it takes 19.055000 seconds to generate the second Markov Chain

it takes 18.871000 seconds to generate the third Markov Chain

it takes 19.311000 seconds to generate the fourth Markov Chain

it takes 19.177000 seconds to generate the fifth Markov Chain

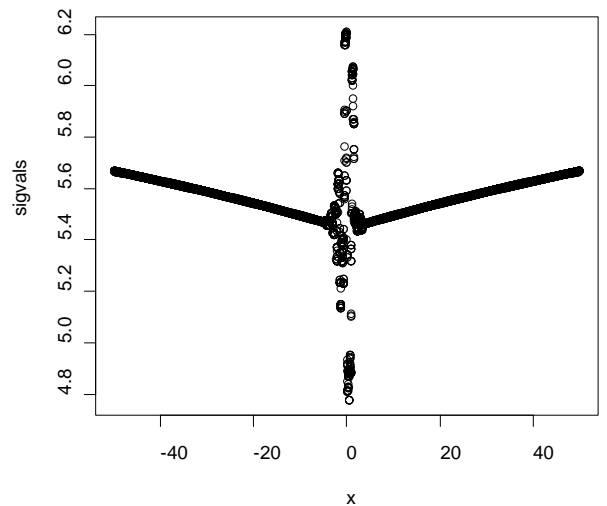
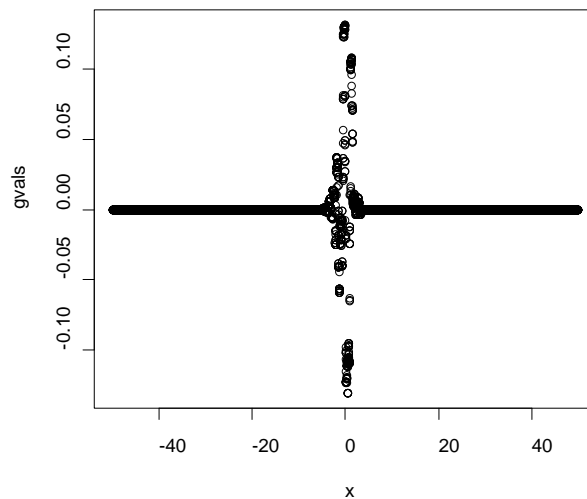
it takes 584.332000 seconds to test the local acceptance

1

[1] 6.692964
[1] 0.008586954
[1] 0.5457672

2.1.3.9 case 40 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $height = 0.5$, $width = 0.5$, $C = 0.001$, $\gamma = 0.1$ with fixed

bandwidth $b_n = 1$



Accepted 22634 out of 100000 (22.634%).

final beta = 1.694196

alpha(0.000000) is 0.175360

alpha(2.000000) is 0.328895

alpha(5.000000) is 0.477720

alpha(10.000000) is 0.503992

alpha(20.000000) is 0.499353

alpha(50.000000) is 0.508652

alpha(100.000000) is 0.512111

alpha(150.000000) is 0.501107

it takes 129.093000 seconds to run the adaptation algorithm

it takes 60.973000 seconds to compute g and sigma

it takes 19.711000 seconds to generate the first Markov Chain

it takes 19.439000 seconds to generate the second Markov Chain

it takes 19.064000 seconds to generate the third Markov Chain

it takes 19.393000 seconds to generate the fourth Markov Chain

it takes 19.296000 seconds to generate the fifth Markov Chain

it takes 585.210000 seconds to test the local acceptance

1

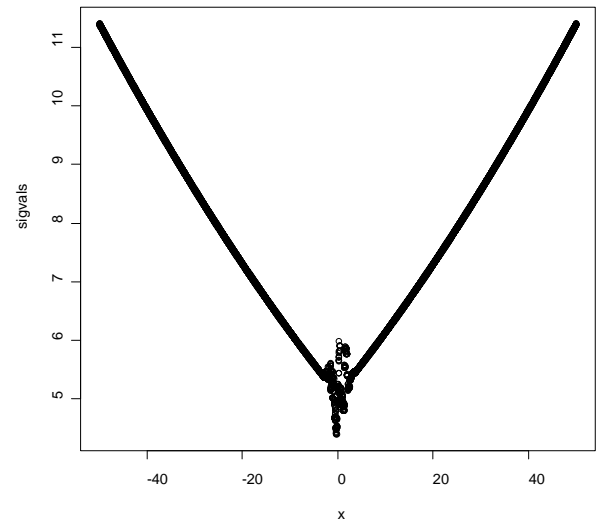
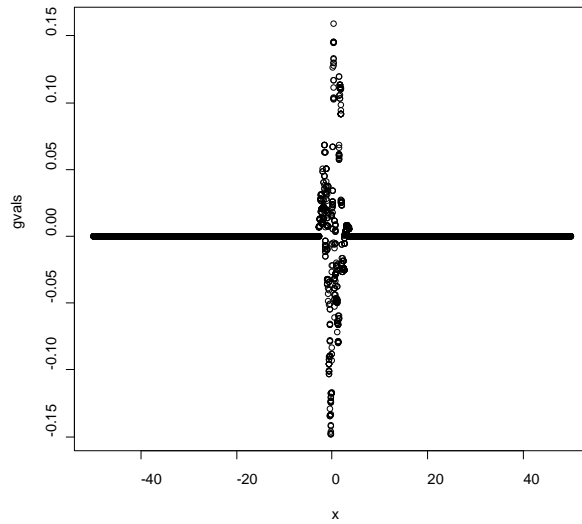
[1] 6.49034

[1] 0.008560577

[1] 0.5352067

2.1.3.10 case 41 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $height = 1$, $width = 0.5$, $C = 0.01$, $\gamma = 2$ with fixed

bandwidth $b_n = 1$



Accepted 23484 out of 100000 (23.484%).

final beta = 1.623149

alpha(0.000000) is 0.187799

alpha(2.000000) is 0.320460

alpha(5.000000) is 0.476159

alpha(10.000000) is 0.510392

alpha(20.000000) is 0.499119

alpha(50.000000) is 0.498086

alpha(100.000000) is 0.494173

alpha(150.000000) is 0.499675

it takes 128.783000 seconds to run the adaptation algorithm

it takes 56.547000 seconds to compute g and sigma

it takes 19.107000 seconds to generate the first Markov Chain

it takes 19.310000 seconds to generate the second Markov Chain

it takes 18.989000 seconds to generate the third Markov Chain

it takes 19.172000 seconds to generate the fourth Markov Chain

it takes 19.425000 seconds to generate the fifth Markov Chain

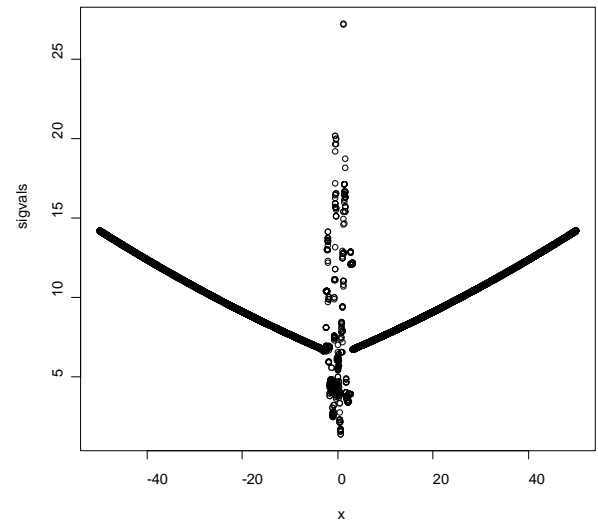
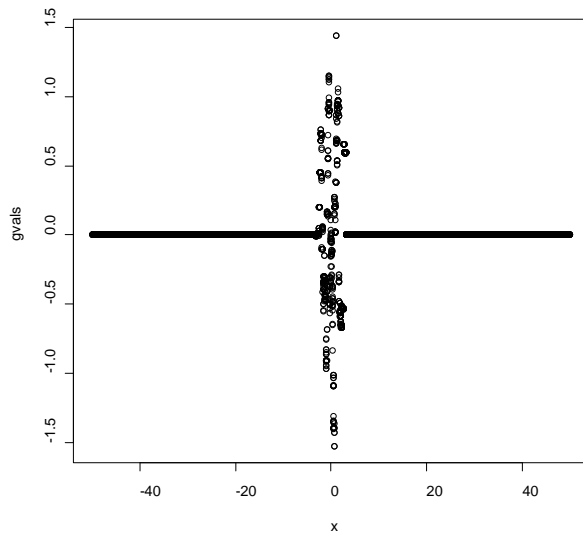
it takes 586.787000 seconds to test the local acceptance

1

[1] 6.555601
[1] 0.008636471
[1] 0.5541553

2.1.3.11 case 42 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $height = 10$, $width = 0.5$, $C = 0.01$, $\gamma = 2$ with fixed

bandwidth $b_n = 1$



Accepted 18745 out of 100000 (18.745%).

final beta = 1.842263

alpha(0.000000) is 0.161404

alpha(2.000000) is 0.399803

alpha(5.000000) is 0.440082

alpha(10.000000) is 0.507989

alpha(20.000000) is 0.491224

alpha(50.000000) is 0.503609

alpha(100.000000) is 0.500292

alpha(150.000000) is 0.502577

it takes 129.356000 seconds to run the adaptation algorithm

it takes 57.235000 seconds to compute g and sigma

it takes 20.125000 seconds to generate the first Markov Chain

it takes 19.813000 seconds to generate the second Markov Chain

it takes 19.562000 seconds to generate the third Markov Chain

it takes 19.695000 seconds to generate the fourth Markov Chain

it takes 20.045000 seconds to generate the fifth Markov Chain

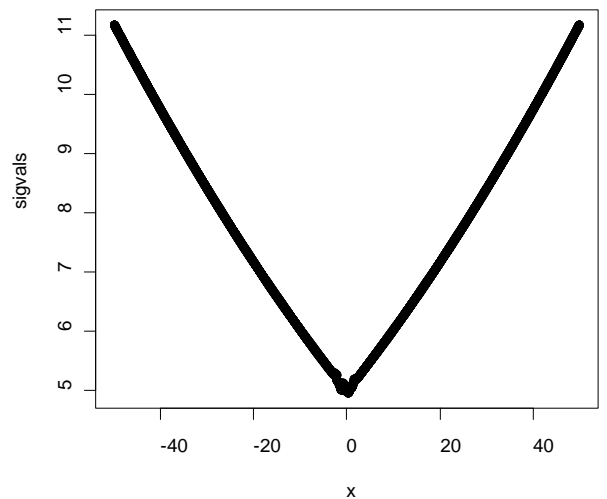
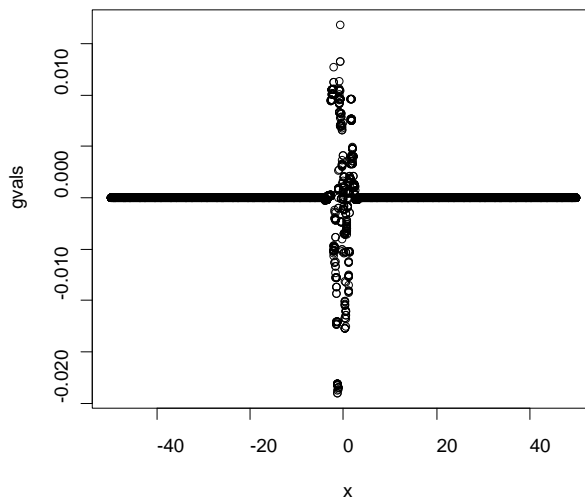
it takes 585.469000 seconds to test the local acceptance

1

[1] 9.308285
[1] 0.01020134
[1] 0.4585032

2.1.3.12 case 43 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $height = 0.1$, $width = 0.5$, $C = 0.01$, $\gamma = 2$ with fixed

bandwidth $b_n = 1$



Accepted 23679 out of 100000 (23.679%).

final beta = 1.603976

alpha(0.000000) is 0.188531

alpha(2.000000) is 0.337021

alpha(5.000000) is 0.483636

alpha(10.000000) is 0.499772

alpha(20.000000) is 0.499243

alpha(50.000000) is 0.506060

alpha(100.000000) is 0.504384

alpha(150.000000) is 0.504052

it takes 130.732000 seconds to run the adaptation algorithm

it takes 57.978000 seconds to compute g and sigma

it takes 18.671000 seconds to generate the first Markov Chain

it takes 18.633000 seconds to generate the second Markov Chain

it takes 18.680000 seconds to generate the third Markov Chain

it takes 18.546000 seconds to generate the fourth Markov Chain

it takes 18.661000 seconds to generate the fifth Markov Chain

it takes 578.604000 seconds to test the local acceptance

1

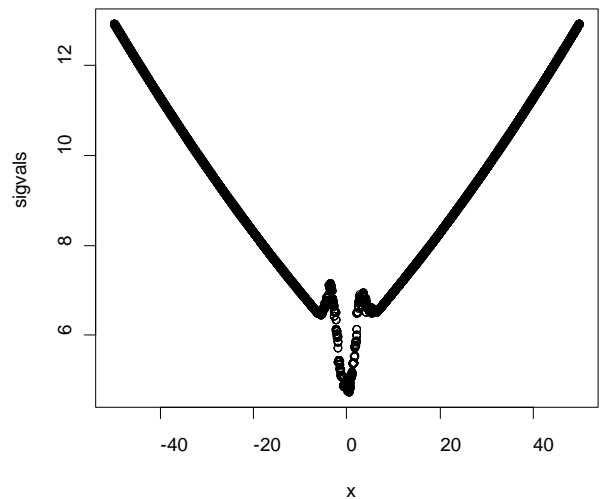
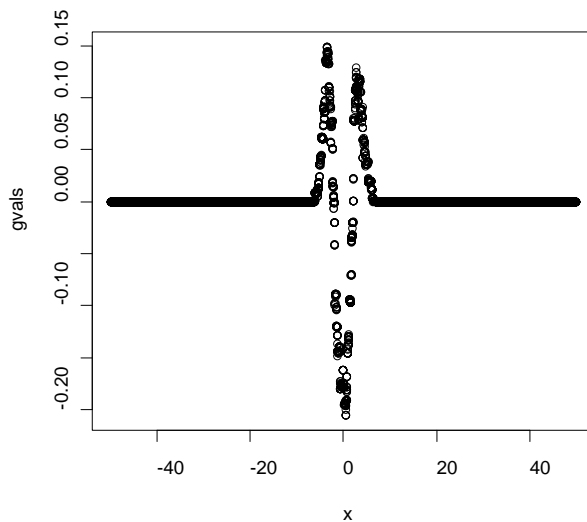
```

[1] 6.726921
[1] 0.008570708
[1] 0.5399683
> source("xlist5");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 6.362033
[1] 0.008291113
[1] 0.5503619

```

2.1.3.13 case 44 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $height = 0.5$, $width = 2$, $C = 0.01$, $\gamma = 2$ with fixed

bandwidth $b_n = 1$



Accepted 23426 out of 100000 (23.426%).

final beta = 1.749096

alpha(0.000000) is 0.192279

alpha(2.000000) is 0.300504

alpha(5.000000) is 0.453942

alpha(10.000000) is 0.503413

alpha(20.000000) is 0.495909

alpha(50.000000) is 0.507192

alpha(100.000000) is 0.495004

alpha(150.000000) is 0.503508

it takes 129.124000 seconds to run the adaptation algorithm

it takes 57.509000 seconds to compute g and sigma

it takes 18.836000 seconds to generate the first Markov Chain

it takes 19.084000 seconds to generate the second Markov Chain

it takes 20.564000 seconds to generate the third Markov Chain

it takes 18.880000 seconds to generate the fourth Markov Chain

it takes 20.031000 seconds to generate the fifth Markov Chain
it takes 594.385000 seconds to test the local acceptance

|

[1] 0.5300015

```
> source("xlist5");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /  
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
```

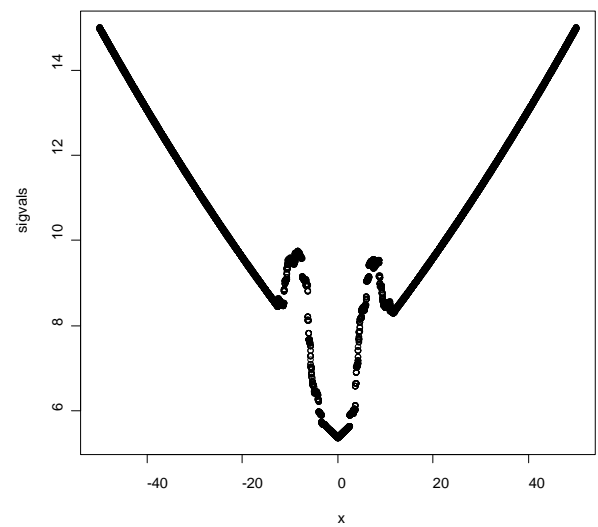
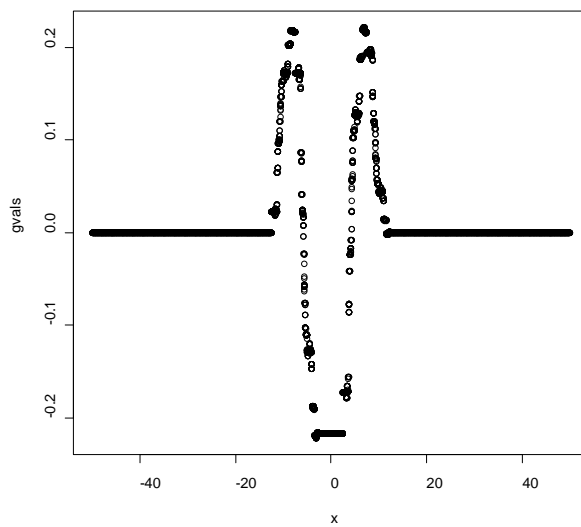
[1] 7.392876

[1] 0.009022338

[1] 0.5201393

2.1.3.14 case 45 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $height = 0.5$, $width = 5$, $C = 0.01$, $\gamma = 2$ with fixed

bandwidth $b_n = 1$



Accepted 21954 out of 100000 (21.954%).

final beta = 1.896775

alpha(0.000000) is 0.182106

alpha(2.000000) is 0.324927

alpha(5.000000) is 0.394897

alpha(10.000000) is 0.492385

alpha(20.000000) is 0.502033

alpha(50.000000) is 0.493569

alpha(100.000000) is 0.500820

alpha(150.000000) is 0.501123

it takes 130.563000 seconds to run the adaptation algorithm

it takes 57.790000 seconds to compute g and sigma

it takes 19.697000 seconds to generate the first Markov Chain

it takes 19.753000 seconds to generate the second Markov Chain

it takes 19.598000 seconds to generate the third Markov Chain

it takes 19.523000 seconds to generate the fourth Markov Chain

it takes 19.212000 seconds to generate the fifth Markov Chain

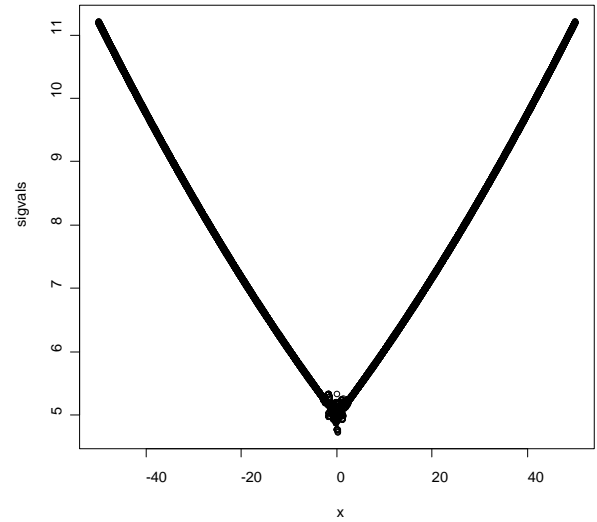
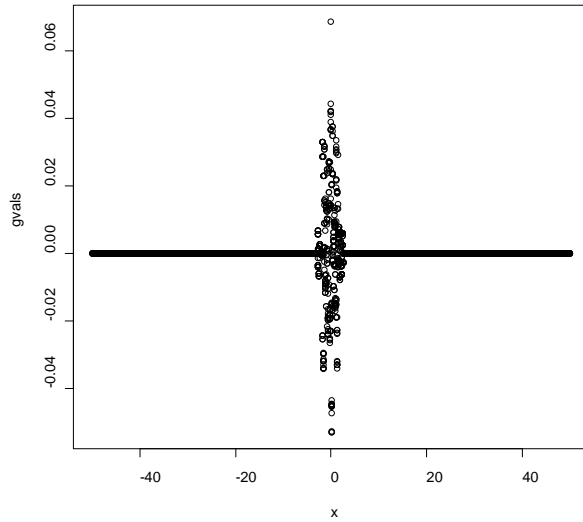
it takes 603.258000 seconds to test the local acceptance

1

[1] 6.854895
[1] 0.008702906
[1] 0.5164709

2.1.3.15 case 46 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $height = 0.5$, $width = 0.1$, $C = 0.01$, $\gamma = 2$ with fixed

bandwidth $b_n = 1$



Accepted 23642 out of 100000 (23.642%).

final beta = 1.605517

alpha(0.000000) is 0.192827

alpha(2.000000) is 0.325493

alpha(5.000000) is 0.478442

alpha(10.000000) is 0.512192

alpha(20.000000) is 0.499076

alpha(50.000000) is 0.493956

alpha(100.000000) is 0.503451

alpha(150.000000) is 0.504400

it takes 131.982000 seconds to run the adaptation algorithm

it takes 58.176000 seconds to compute g and sigma

it takes 20.263000 seconds to generate the first Markov Chain

it takes 20.133000 seconds to generate the second Markov Chain

it takes 20.427000 seconds to generate the third Markov Chain

it takes 20.049000 seconds to generate the fourth Markov Chain

it takes 20.327000 seconds to generate the fifth Markov Chain

it takes 605.936000 seconds to test the local acceptance

1

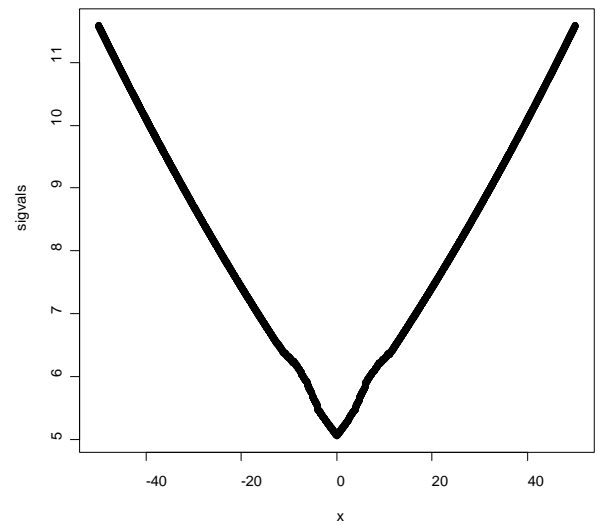
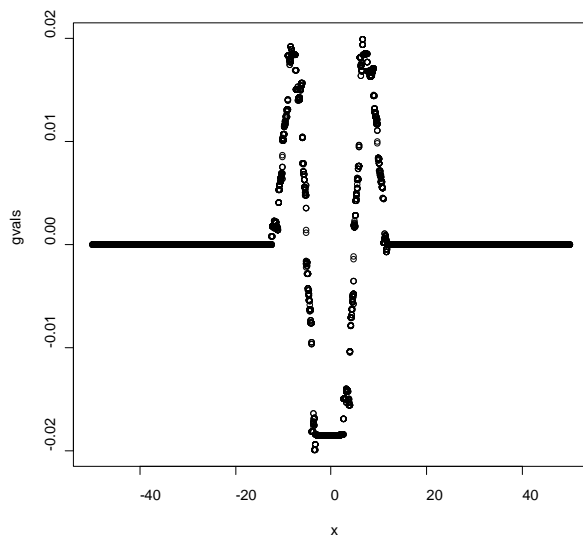
[1] 6.081314

[1] 0.008252063

[1] 0.5518468

2.1.3.16 case 47 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $height = 0.5$, $width = 0.5$, $C = 0.01$, $\gamma = 2$ with fixed

bandwidth $b_n = 10$



Accepted 23590 out of 100000 (23.590%).

final beta = 1.639301

alpha(0.000000) is 0.191540

alpha(2.000000) is 0.335518

alpha(5.000000) is 0.479633

alpha(10.000000) is 0.498527

alpha(20.000000) is 0.500063

alpha(50.000000) is 0.505558

alpha(100.000000) is 0.500621

alpha(150.000000) is 0.493689

it takes 133.815000 seconds to run the adaptation algorithm

it takes 59.140000 seconds to compute g and sigma

it takes 18.822000 seconds to generate the first Markov Chain

it takes 19.763000 seconds to generate the second Markov Chain

it takes 19.456000 seconds to generate the third Markov Chain

it takes 18.831000 seconds to generate the fourth Markov Chain

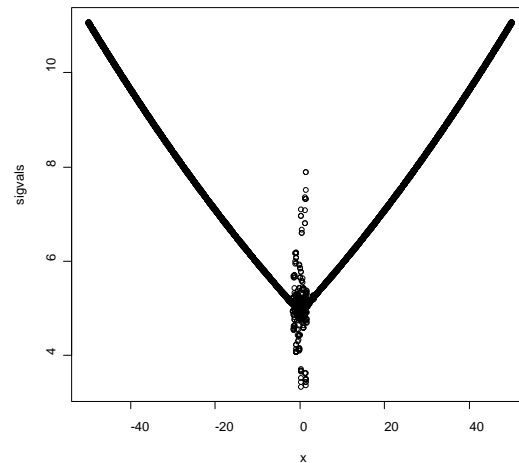
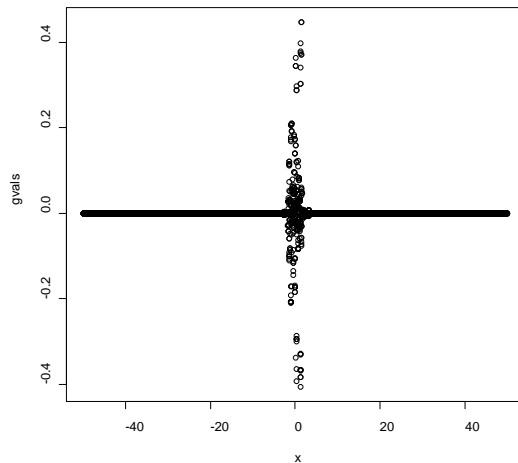
it takes 19.578000 seconds to generate the fifth Markov Chain

it takes 600.070000 seconds to test the local acceptance

1

[1] 6.359084
[1] 0.00842308
[1] 0.554771

2.1.3.17 case 48 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $height = 0.5$, $width = 0.5$, $C = 0.01$, $\gamma = 2$ with fixed
bandwidth $b_n = 0.1$



Accepted 24144 out of 100000 (24.144%).

final beta = 1.592917

alpha(0.000000) is 0.198912

alpha(2.000000) is 0.328186

alpha(5.000000) is 0.474185

alpha(10.000000) is 0.494897

alpha(20.000000) is 0.509700

alpha(50.000000) is 0.493201

alpha(100.000000) is 0.508407

alpha(150.000000) is 0.497111

it takes 132.193000 seconds to run the adaptation algorithm

it takes 58.991000 seconds to compute g and sigma

it takes 20.215000 seconds to generate the first Markov Chain

it takes 19.654000 seconds to generate the second Markov Chain

it takes 19.407000 seconds to generate the third Markov Chain

it takes 19.431000 seconds to generate the fourth Markov Chain

it takes 19.357000 seconds to generate the fifth Markov Chain

it takes 609.803000 seconds to test the local acceptance

1

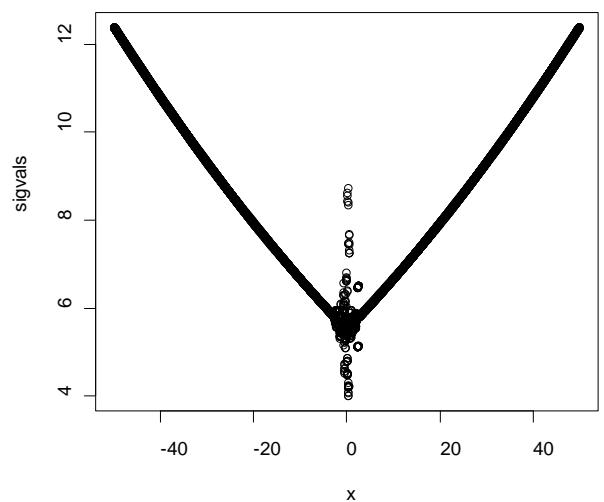
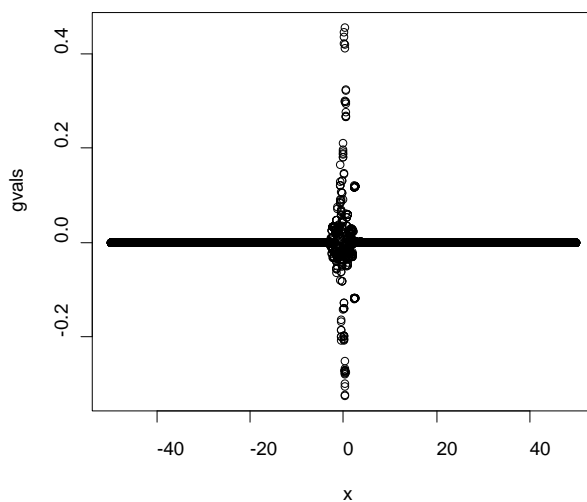
```

> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.008251732
> asjd(xlist)
[1] 0.543797
>
> source("xlist4")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 6.212332
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.008317304
> asjd(xlist)
[1] 0.5649309
>
> source("xlist5")
> plot(xlist[(B+1):M],type="l")
> varfact(xlist[(B+1):M]);
[1] 6.130305
> sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
[1] 0.008166715
> asjd(xlist)
[1] 0.5469031

```

2.1.3.18 case 49 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $height = 0.5$, $width = 0.5$, $C = 0.01$, $\gamma = 2$ with

decreasing bandwidth $b_n = \frac{1}{n^{0.2}}$



Accepted 21609 out of 100000 (21.609%).
 final beta = 1.705975

alpha(0.000000) is 0.168346

alpha(2.000000) is 0.303514

alpha(5.000000) is 0.473132

alpha(10.000000) is 0.508745

alpha(20.000000) is 0.500702

alpha(50.000000) is 0.502543

alpha(100.000000) is 0.501443

alpha(150.000000) is 0.500437

it takes 132.324000 seconds to run the adaptation algorithm

it takes 58.739000 seconds to compute g and sigma

it takes 19.708000 seconds to generate the first Markov Chain

it takes 19.571000 seconds to generate the second Markov Chain

it takes 19.439000 seconds to generate the third Markov Chain

it takes 19.542000 seconds to generate the fourth Markov Chain

it takes 19.544000 seconds to generate the fifth Markov Chain

it takes 599.769000 seconds to test the local acceptance

|

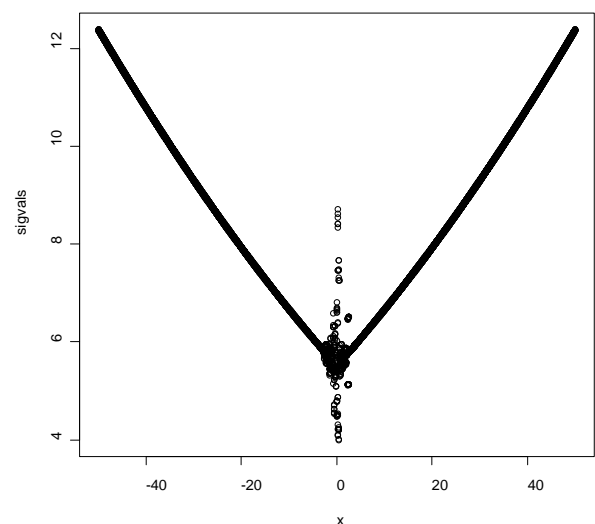
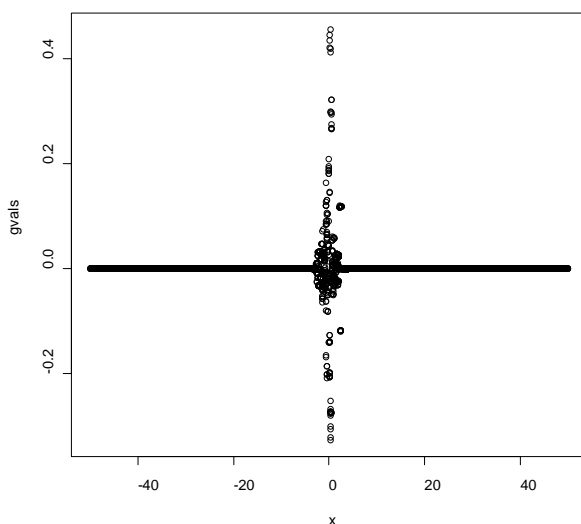
```

sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 7.150534
[1] 0.008775849
[1] 0.5047632
> source("xlist3");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 7.179354
[1] 0.008915502
[1] 0.5114743
> source("xlist4");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 7.156782
[1] 0.008810378
[1] 0.5108781
> source("xlist5");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 7.01146
[1] 0.008889637
[1] 0.5306071

```

2.1.3.19 case 50 $\eta_n = \frac{1}{(n+5)^{0.8}}$, $height = 0.5$, $width = 0.5$, $C = 0.01$, $\gamma = 2$ with fixed

bandwidth $b_n = 1$



Accepted 21609 out of 100000 (21.609%).

final beta = 1.705975

alpha(0.000000) is 0.168346

alpha(2.000000) is 0.303514

alpha(5.000000) is 0.473132

alpha(10.000000) is 0.508745

alpha(20.000000) is 0.500702

alpha(50.000000) is 0.502543

alpha(100.000000) is 0.501443

alpha(150.000000) is 0.500437

it takes 132.324000 seconds to run the adaptation algorithm

it takes 58.739000 seconds to compute g and sigma

it takes 19.708000 seconds to generate the first Markov Chain

it takes 19.571000 seconds to generate the second Markov Chain

it takes 19.439000 seconds to generate the third Markov Chain

it takes 19.542000 seconds to generate the fourth Markov Chain

it takes 19.544000 seconds to generate the fifth Markov Chain

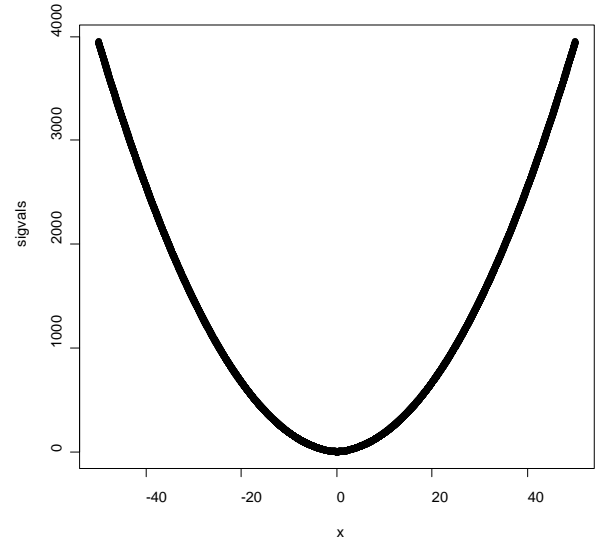
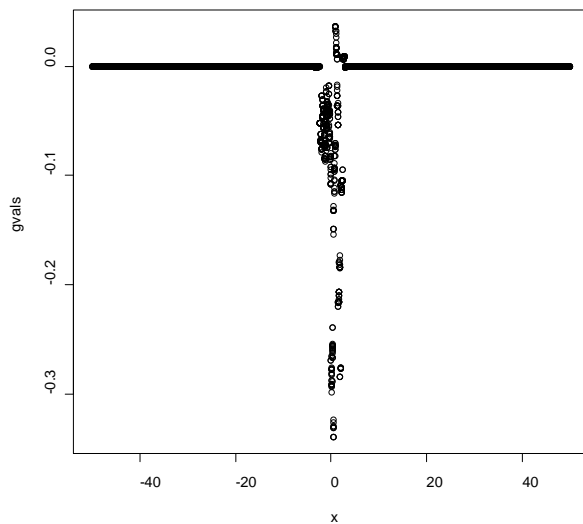
it takes 599.769000 seconds to test the local acceptance

|


```
[1] 0.5047632
> source("xlist3");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 7.179354
[1] 0.008915502
[1] 0.5114743
> source("xlist4");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 7.156782
[1] 0.008810378
[1] 0.5108781
> source("xlist5");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 7.01146
[1] 0.008889637
[1] 0.5306071
```

2.1.4 kernel function $K(x) = \begin{cases} 0, & |x| \geq 2 * width \text{ or } |x| \leq width \\ 1, & width < |x| < 2 * width \end{cases}$

2.1.4.1 case 51 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, C = 1, $\gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 23009 out of 100000 (23.009%).

final beta = 0.417902

alpha(0.000000) is 0.310259

alpha(2.000000) is 0.143592

alpha(5.000000) is 0.076589

alpha(10.000000) is 0.041575

alpha(20.000000) is 0.022942

alpha(50.000000) is 0.009200

alpha(100.000000) is 0.005400

alpha(150.000000) is 0.004200

it takes 125.540000 seconds to run the adaptation algorithm

it takes 55.805000 seconds to compute g and sigma

it takes 19.754000 seconds to generate the first Markov Chain

it takes 21.302000 seconds to generate the second Markov Chain

it takes 22.193000 seconds to generate the third Markov Chain

it takes 20.612000 seconds to generate the fourth Markov Chain

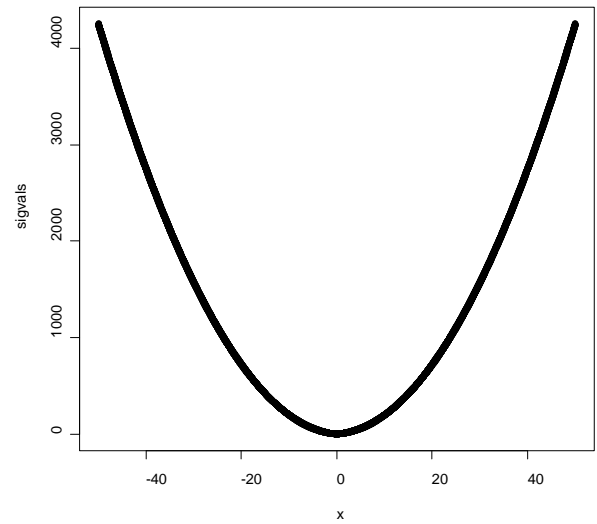
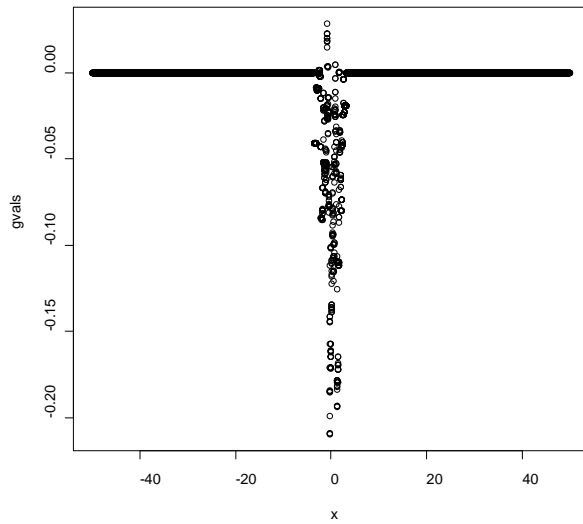
it takes 20.616000 seconds to generate the fifth Markov Chain

it takes 974.826000 seconds to test the local acceptance

1

[1] 11.34705
[1] 0.01121087
[1] 0.3325641

2.1.4.2 case 52 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C = 10$, $\gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 20742 out of 100000 (20.742%).

final beta = 0.491977

alpha(0.000000) is 0.275429

alpha(2.000000) is 0.134558

alpha(5.000000) is 0.065966

alpha(10.000000) is 0.044212

alpha(20.000000) is 0.024001

alpha(50.000000) is 0.009100

alpha(100.000000) is 0.004300

alpha(150.000000) is 0.003400

it takes 128.005000 seconds to run the adaptation algorithm

it takes 56.269000 seconds to compute g and sigma

it takes 19.186000 seconds to generate the first Markov Chain

it takes 19.712000 seconds to generate the second Markov Chain

it takes 20.762000 seconds to generate the third Markov Chain

it takes 21.651000 seconds to generate the fourth Markov Chain

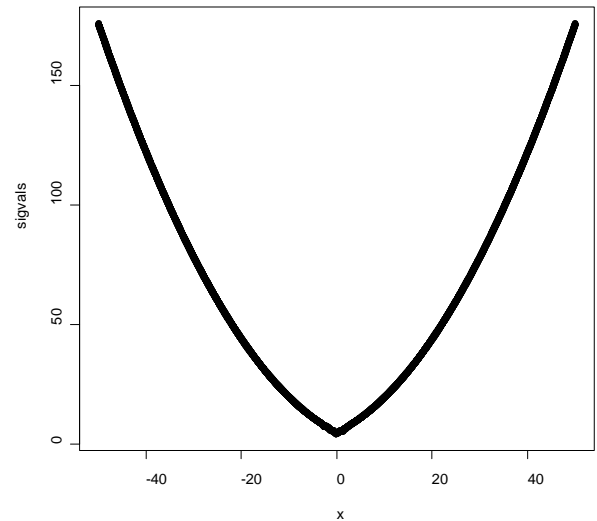
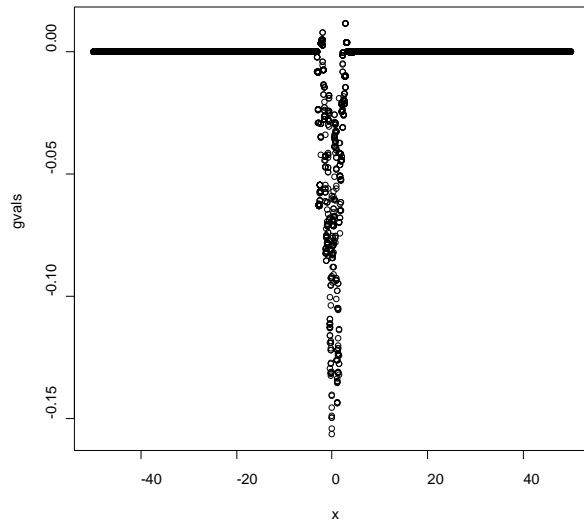
it takes 20.180000 seconds to generate the fifth Markov Chain

it takes 1010.090000 seconds to test the local acceptance

1

[1] 12.73849
[1] 0.01200023
[1] 0.3157405

2.1.4.3 case 53 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C = 0.1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 21407 out of 100000 (21.407%).

final beta = 1.586745

alpha(0.000000) is 0.186088

alpha(2.000000) is 0.255791

alpha(5.000000) is 0.322271

alpha(10.000000) is 0.361781

alpha(20.000000) is 0.319420

alpha(50.000000) is 0.215913

alpha(100.000000) is 0.130600

alpha(150.000000) is 0.098400

it takes 133.242000 seconds to run the adaptation algorithm

it takes 59.019000 seconds to compute g and sigma

it takes 22.075000 seconds to generate the first Markov Chain

it takes 21.186000 seconds to generate the second Markov Chain

it takes 20.902000 seconds to generate the third Markov Chain

it takes 20.804000 seconds to generate the fourth Markov Chain

it takes 22.036000 seconds to generate the fifth Markov Chain

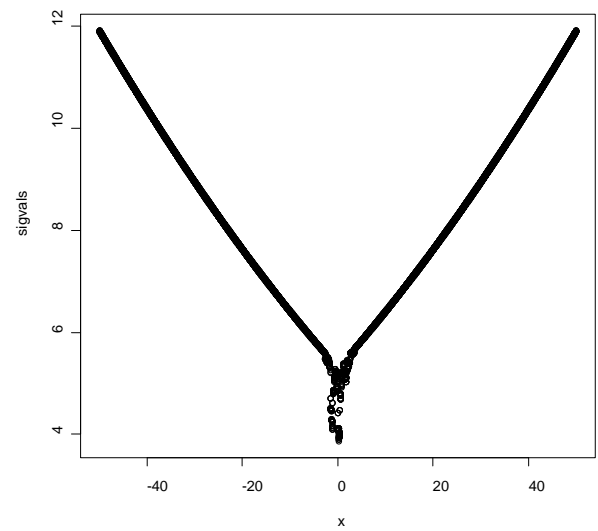
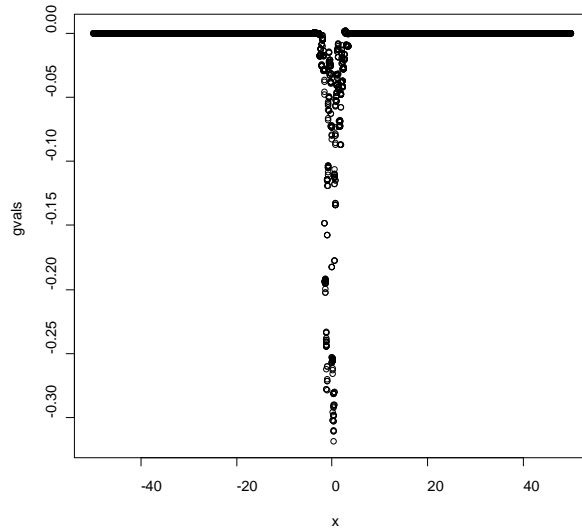
it takes 774.597000 seconds to test the local acceptance

1

[1] 7.425369
[1] 0.00926486
[1] 0.4934043

2.1.4.4 case 54 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C = 0.01, \gamma = 2$ with fixed bandwidth

$b_n = 1$



Accepted 24563 out of 100000 (24.563%).

final beta = 1.666639

alpha(0.000000) is 0.204343

alpha(2.000000) is 0.324662

alpha(5.000000) is 0.465485

alpha(10.000000) is 0.501068

alpha(20.000000) is 0.505233

alpha(50.000000) is 0.498960

alpha(100.000000) is 0.511536

alpha(150.000000) is 0.503191

it takes 126.672000 seconds to run the adaptation algorithm

it takes 55.830000 seconds to compute g and sigma

it takes 20.221000 seconds to generate the first Markov Chain

it takes 19.321000 seconds to generate the second Markov Chain

it takes 19.575000 seconds to generate the third Markov Chain

it takes 19.669000 seconds to generate the fourth Markov Chain

it takes 19.634000 seconds to generate the fifth Markov Chain

it takes 576.363000 seconds to test the local acceptance

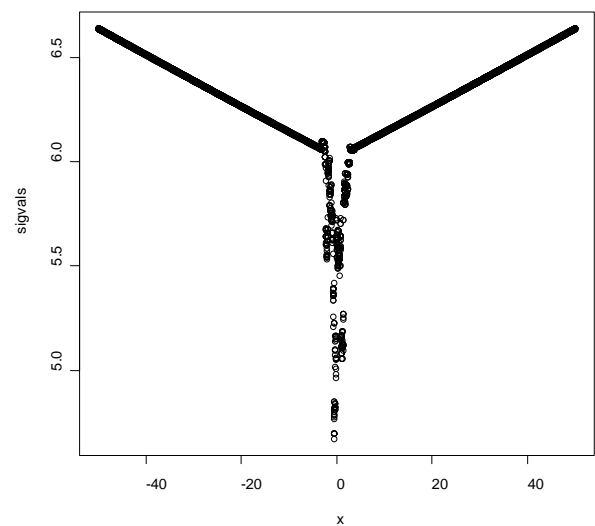
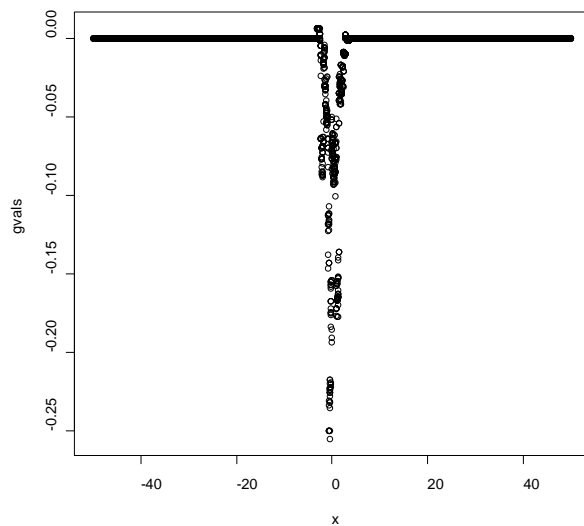
1

[1] 6.352072

[1] 0.008441499

[1] 0.5698832

2.1.4.5 case 55 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 1, $C = 0.001$, $\gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 21862 out of 100000 (21.862%).

final beta = 1.795190

alpha(0.000000) is 0.178309

alpha(2.000000) is 0.313602

alpha(5.000000) is 0.465026

alpha(10.000000) is 0.507124

alpha(20.000000) is 0.504982

alpha(50.000000) is 0.506570

alpha(100.000000) is 0.500667

alpha(150.000000) is 0.491467

it takes 126.739000 seconds to run the adaptation algorithm

it takes 55.053000 seconds to compute g and sigma

it takes 19.893000 seconds to generate the first Markov Chain

it takes 19.991000 seconds to generate the second Markov Chain

it takes 20.178000 seconds to generate the third Markov Chain

it takes 20.074000 seconds to generate the fourth Markov Chain

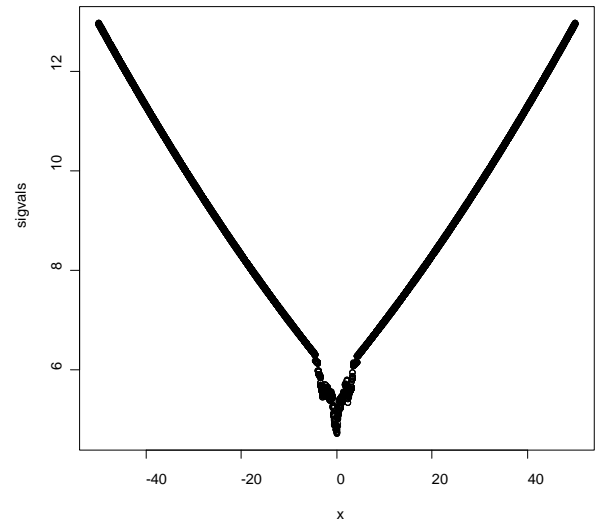
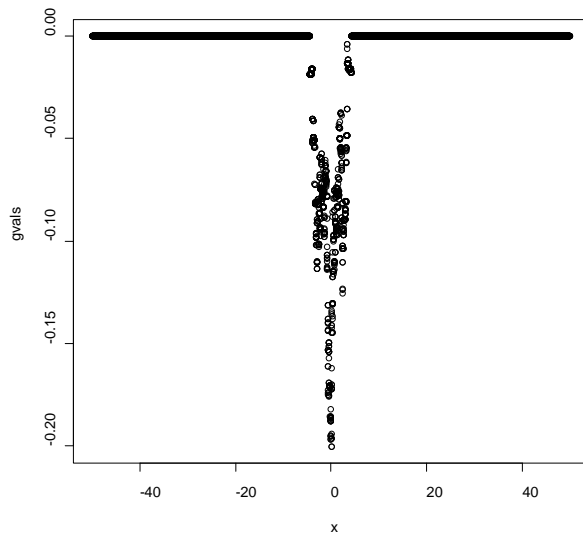
it takes 20.152000 seconds to generate the fifth Markov Chain

it takes 580.130000 seconds to test the local acceptance

1

[1] 7.055358
 [1] 0.008838765
 [1] 0.5103956

2.1.4.6 case 56 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 1, $C = 0.01, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 22481 out of 100000 (22.481%).

final beta = 1.752170

alpha(0.000000) is 0.189223

alpha(2.000000) is 0.310525

alpha(5.000000) is 0.459372

alpha(10.000000) is 0.497289

alpha(20.000000) is 0.503854

alpha(50.000000) is 0.495202

alpha(100.000000) is 0.494385

alpha(150.000000) is 0.509056

it takes 128.270000 seconds to run the adaptation algorithm

it takes 56.474000 seconds to compute g and sigma

it takes 19.944000 seconds to generate the first Markov Chain

it takes 19.749000 seconds to generate the second Markov Chain

it takes 21.216000 seconds to generate the third Markov Chain

it takes 20.799000 seconds to generate the fourth Markov Chain

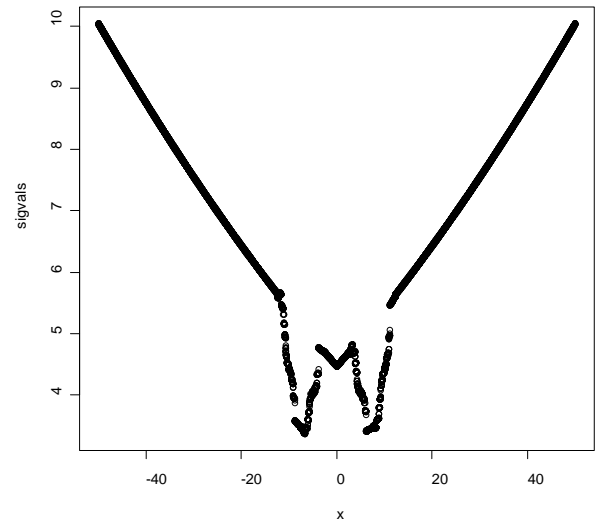
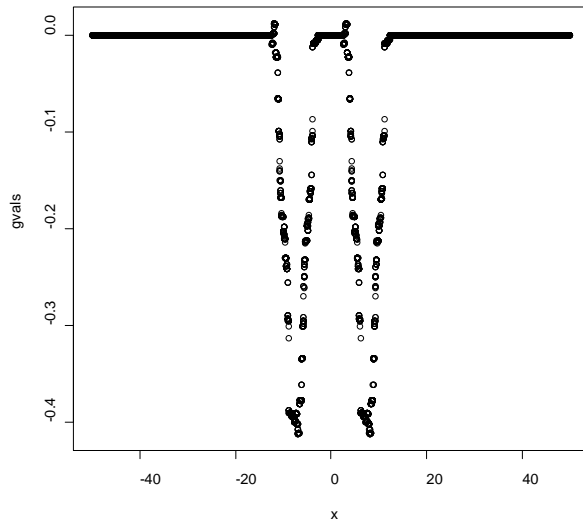
it takes 20.124000 seconds to generate the fifth Markov Chain

it takes 582.432000 seconds to test the local acceptance

1

[1] 7.293104
 [1] 0.008969298
 [1] 0.5260217

2.1.4.7 case 57 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 5, $C = 0.01$, $\gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 26365 out of 100000 (26.365%).

final beta = 1.496543

alpha(0.000000) is 0.216441

alpha(2.000000) is 0.368902

alpha(5.000000) is 0.500734

alpha(10.000000) is 0.507066

alpha(20.000000) is 0.502065

alpha(50.000000) is 0.502358

alpha(100.000000) is 0.495112

alpha(150.000000) is 0.503168

it takes 124.340000 seconds to run the adaptation algorithm

it takes 56.677000 seconds to compute g and sigma

it takes 21.173000 seconds to generate the first Markov Chain

it takes 20.264000 seconds to generate the second Markov Chain

it takes 19.534000 seconds to generate the third Markov Chain

it takes 19.489000 seconds to generate the fourth Markov Chain

it takes 18.931000 seconds to generate the fifth Markov Chain

it takes 569.717000 seconds to test the local acceptance

1

```
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M] ) );asjd(xlist[(B+1):M]);
```

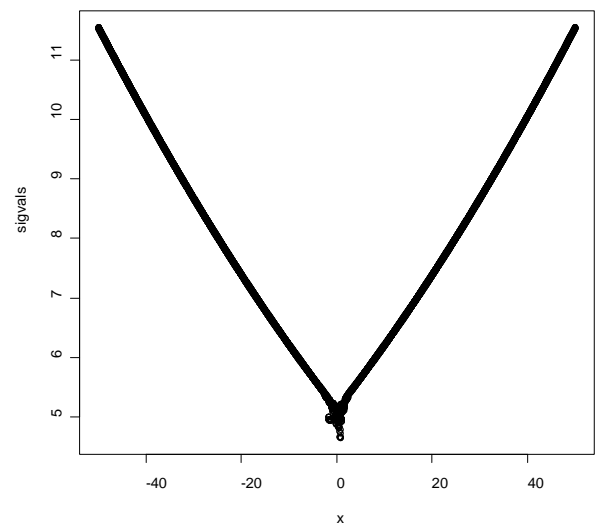
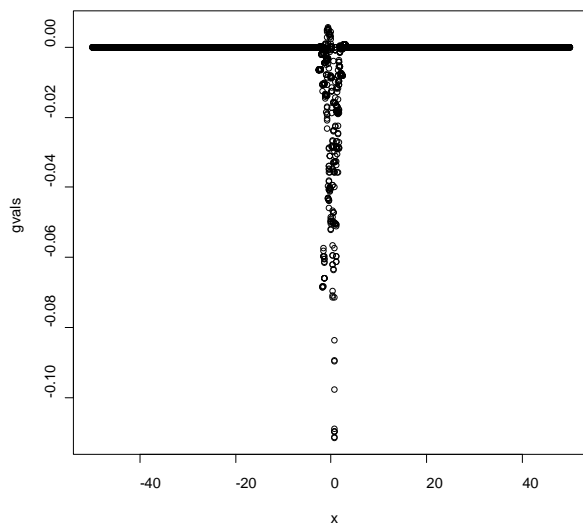
```
[1] 5.500506
```

```
[1] 0.007780254
```

```
[1] 0.5968249
```

2.1.4.8 case 58 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.1, $C = 0.01$, $\gamma = 2$ with fixed bandwidth

$b_n = 1$



Accepted 23471 out of 100000 (23.471%).

final beta = 1.635035

alpha(0.000000) is 0.196509

alpha(2.000000) is 0.329970

alpha(5.000000) is 0.479467

alpha(10.000000) is 0.512654

alpha(20.000000) is 0.507827

alpha(50.000000) is 0.496350

alpha(100.000000) is 0.489645

alpha(150.000000) is 0.503596

it takes 128.387000 seconds to run the adaptation algorithm

it takes 57.261000 seconds to compute g and sigma

it takes 22.145000 seconds to generate the first Markov Chain

it takes 21.970000 seconds to generate the second Markov Chain

it takes 21.670000 seconds to generate the third Markov Chain

it takes 22.460000 seconds to generate the fourth Markov Chain

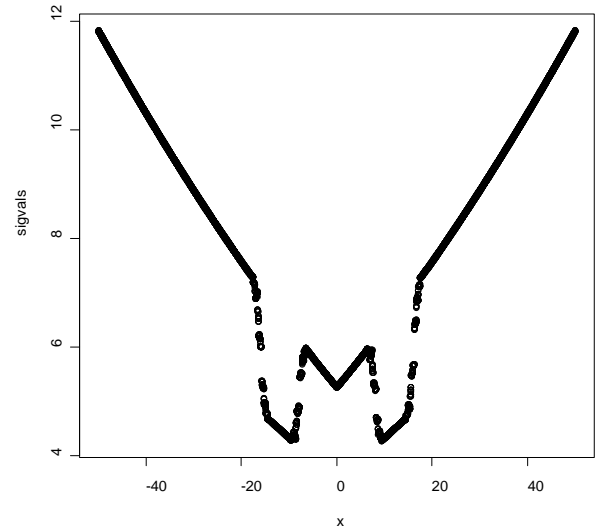
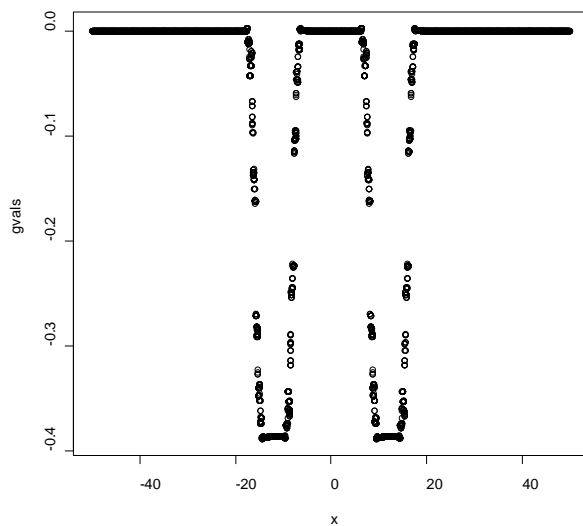
it takes 22.477000 seconds to generate the fifth Markov Chain

it takes 589.629000 seconds to test the local acceptance

1

[1] 6.456669
[1] 0.008401081
[1] 0.5444502

2.1.4.9 case 59 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 8, $C = 0.01$, $\gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 22642 out of 100000 (22.642%).

final beta = 1.660210

alpha(0.000000) is 0.182785

alpha(2.000000) is 0.313792

alpha(5.000000) is 0.478720

alpha(10.000000) is 0.516151

alpha(20.000000) is 0.495757

alpha(50.000000) is 0.495627

alpha(100.000000) is 0.510013

alpha(150.000000) is 0.506006

it takes 123.308000 seconds to run the adaptation algorithm

it takes 54.821000 seconds to compute g and sigma

it takes 19.924000 seconds to generate the first Markov Chain

it takes 19.878000 seconds to generate the second Markov Chain

it takes 19.394000 seconds to generate the third Markov Chain

it takes 19.481000 seconds to generate the fourth Markov Chain

it takes 20.128000 seconds to generate the fifth Markov Chain

it takes 574.279000 seconds to test the local acceptance

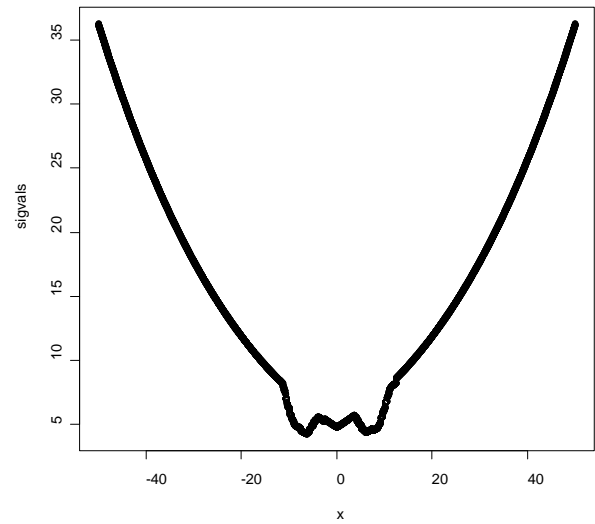
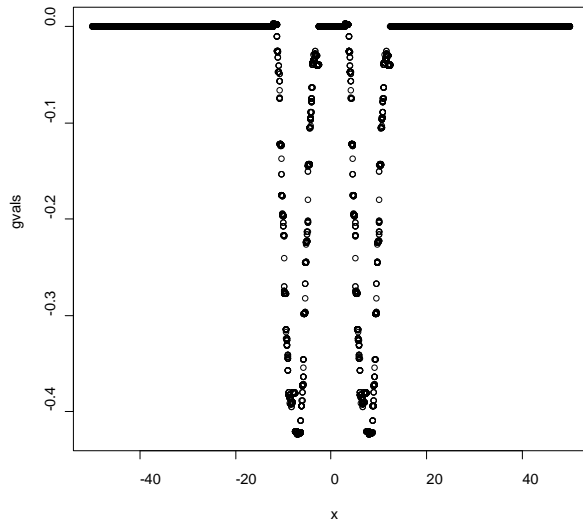
1

```

> source("xlist5");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 6.965559
[1] 0.008812787
[1] 0.5334517

```

2.1.4.10 case 60 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 5, $C = 0.01$, $\gamma = 5$ with fixed bandwidth $b_n = 1$



Accepted 23976 out of 100000 (23.976%).

final beta = 1.563580

alpha(0.000000) is 0.199347

alpha(2.000000) is 0.334377

alpha(5.000000) is 0.500748

alpha(10.000000) is 0.507236

alpha(20.000000) is 0.505732

alpha(50.000000) is 0.493323

alpha(100.000000) is 0.399116

alpha(150.000000) is 0.235500

it takes 124.660000 seconds to run the adaptation algorithm

it takes 55.283000 seconds to compute g and sigma

it takes 19.535000 seconds to generate the first Markov Chain

it takes 19.427000 seconds to generate the second Markov Chain

it takes 19.173000 seconds to generate the third Markov Chain

it takes 19.934000 seconds to generate the fourth Markov Chain

it takes 20.513000 seconds to generate the fifth Markov Chain

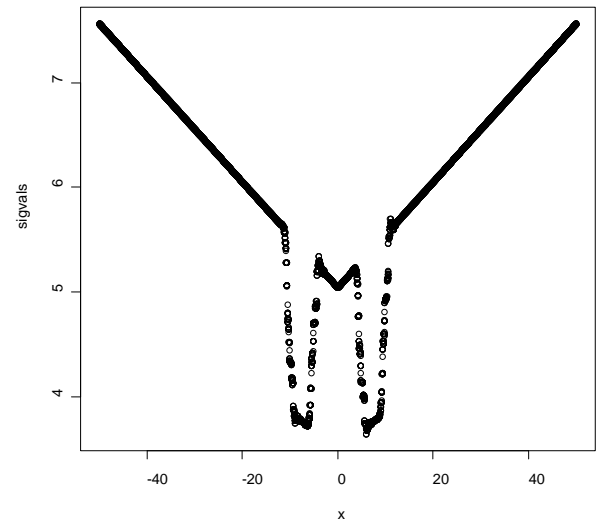
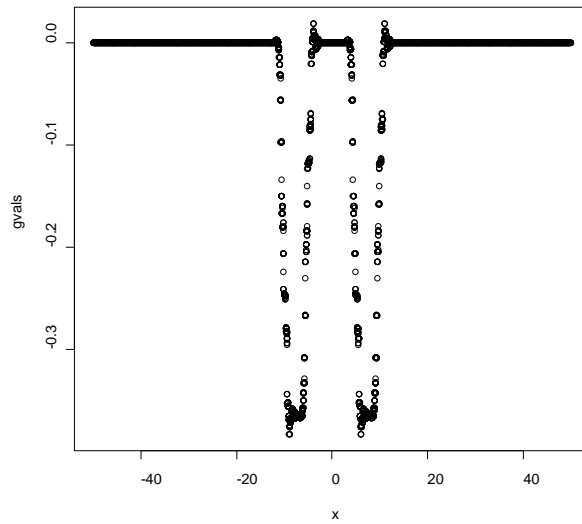
it takes 594.727000 seconds to test the local acceptance

1

[1] 6.651483
[1] 0.008605778
[1] 0.5450531

2.1.4.11 case 61 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 5, $C = 0.01$, $\gamma = 1$ with fixed bandwidth

$b_n = 1$



Accepted 23675 out of 100000 (23.675%).

final beta = 1.617569

alpha(0.000000) is 0.197561

alpha(2.000000) is 0.334814

alpha(5.000000) is 0.509056

alpha(10.000000) is 0.508438

alpha(20.000000) is 0.499158

alpha(50.000000) is 0.497928

alpha(100.000000) is 0.501279

alpha(150.000000) is 0.493803

it takes 125.480000 seconds to run the adaptation algorithm

it takes 56.040000 seconds to compute g and sigma

it takes 19.422000 seconds to generate the first Markov Chain

it takes 19.479000 seconds to generate the second Markov Chain

it takes 19.599000 seconds to generate the third Markov Chain

it takes 20.212000 seconds to generate the fourth Markov Chain

it takes 19.031000 seconds to generate the fifth Markov Chain

it takes 590.678000 seconds to test the local acceptance

1

```
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
```

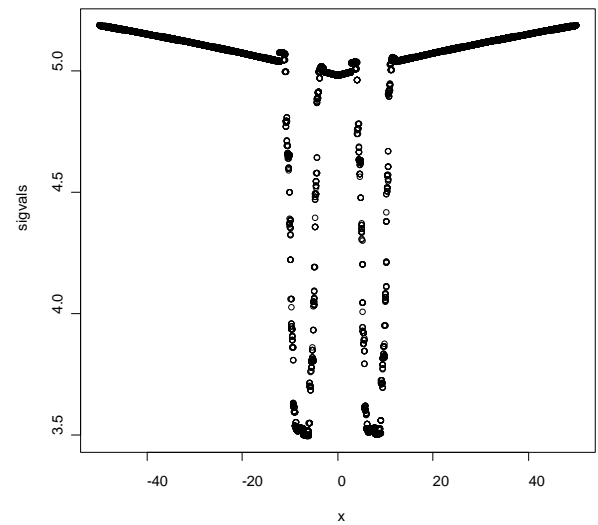
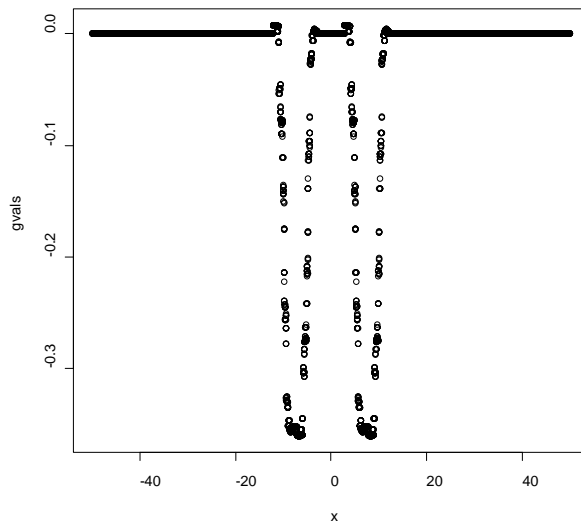
```
[1] 6.598833
```

```
[1] 0.008443037
```

```
[1] 0.5469699
```

2.1.4.12 case 62 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 5, $C = 0.01$, $\gamma = 0.1$ with fixed bandwidth

$b_n = 1$



Accepted 24397 out of 100000 (24.397%).

final beta = 1.605496

alpha(0.000000) is 0.196312

alpha(2.000000) is 0.351285

alpha(5.000000) is 0.508944

alpha(10.000000) is 0.503029

alpha(20.000000) is 0.505562

alpha(50.000000) is 0.500858

alpha(100.000000) is 0.498800

alpha(150.000000) is 0.498894

it takes 124.458000 seconds to run the adaptation algorithm

it takes 55.248000 seconds to compute g and sigma

it takes 19.847000 seconds to generate the first Markov Chain

it takes 18.661000 seconds to generate the second Markov Chain

it takes 18.698000 seconds to generate the third Markov Chain

it takes 19.318000 seconds to generate the fourth Markov Chain

it takes 20.375000 seconds to generate the fifth Markov Chain

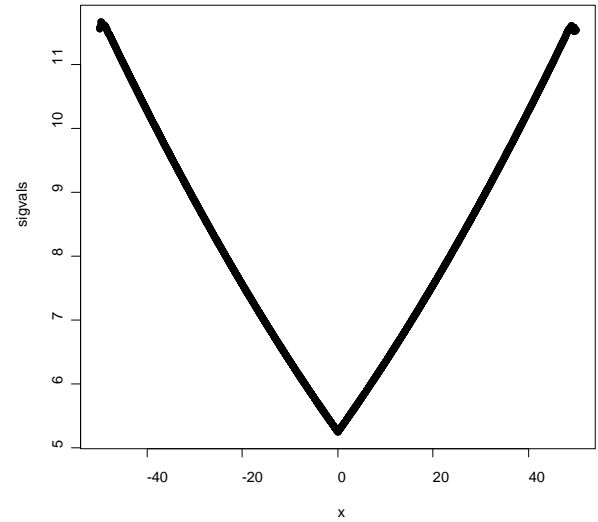
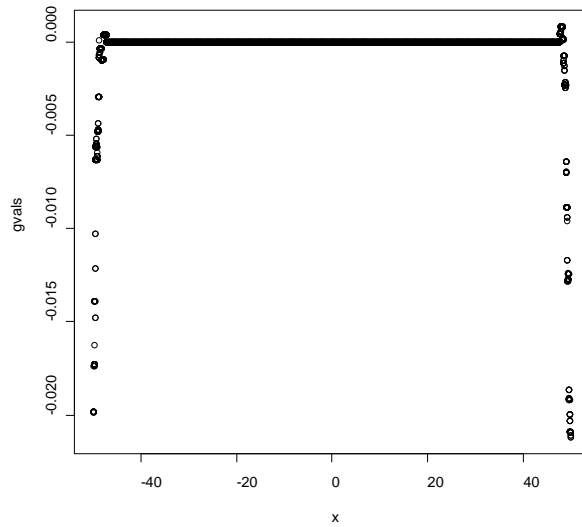
it takes 595.427000 seconds to test the local acceptance

1

[1] 6.12154
 [1] 0.00825666
 [1] 0.5646845

2.1.4.13 case 63 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 5, $C = 0.01$, $\gamma = 2$ with fixed bandwidth

$b_n = 10$



Accepted 22622 out of 100000 (22.622%).

final beta = 1.657513

alpha(0.000000) is 0.183999

alpha(2.000000) is 0.323600

alpha(5.000000) is 0.475474

alpha(10.000000) is 0.506252

alpha(20.000000) is 0.512030

alpha(50.000000) is 0.506490

alpha(100.000000) is 0.493719

alpha(150.000000) is 0.506028

it takes 130.990000 seconds to run the adaptation algorithm

it takes 57.461000 seconds to compute g and sigma

it takes 20.162000 seconds to generate the first Markov Chain

it takes 20.553000 seconds to generate the second Markov Chain

it takes 20.230000 seconds to generate the third Markov Chain

it takes 20.700000 seconds to generate the fourth Markov Chain

it takes 20.905000 seconds to generate the fifth Markov Chain

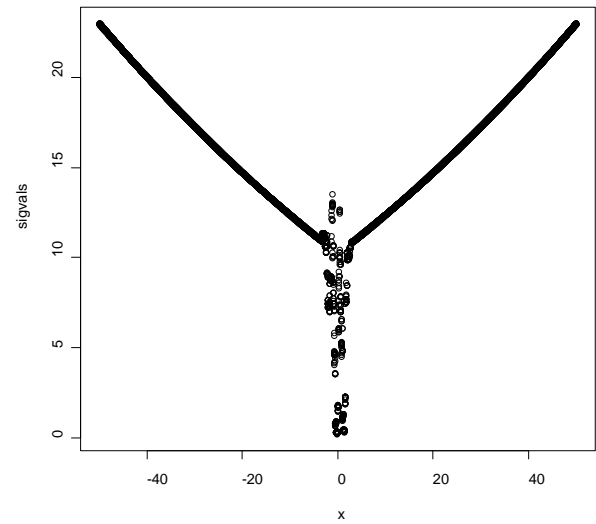
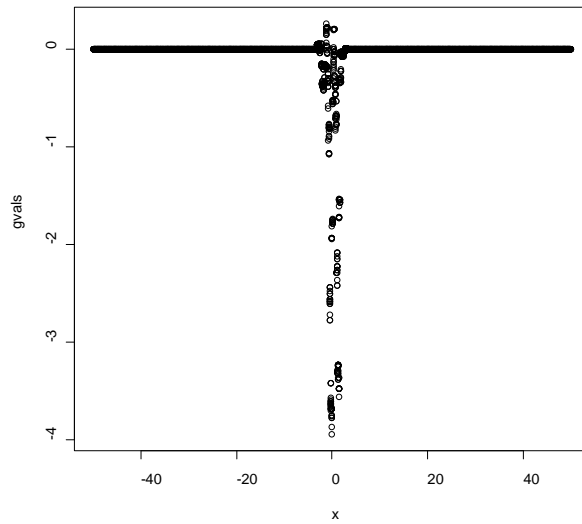
it takes 601.853000 seconds to test the local acceptance

1

[1] 6.666041
[1] 0.008627651
[1] 0.541695

2.1.4.14 case 64 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 5, $C = 0.01$, $\gamma = 2$ with fixed bandwidth

$b_n = 0.1$



Accepted 27016 out of 100000 (27.016%).

final beta = 2.323557

alpha(0.000000) is 0.292087

alpha(2.000000) is 0.172451

alpha(5.000000) is 0.303265

alpha(10.000000) is 0.435934

alpha(20.000000) is 0.496122

alpha(50.000000) is 0.502316

alpha(100.000000) is 0.500706

alpha(150.000000) is 0.497121

it takes 128.956000 seconds to run the adaptation algorithm

it takes 57.127000 seconds to compute g and sigma

it takes 18.625000 seconds to generate the first Markov Chain

it takes 18.546000 seconds to generate the second Markov Chain

it takes 18.632000 seconds to generate the third Markov Chain

it takes 18.589000 seconds to generate the fourth Markov Chain

it takes 18.534000 seconds to generate the fifth Markov Chain

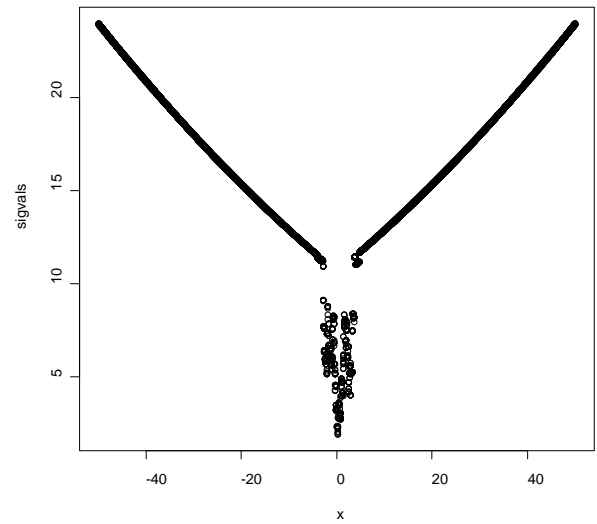
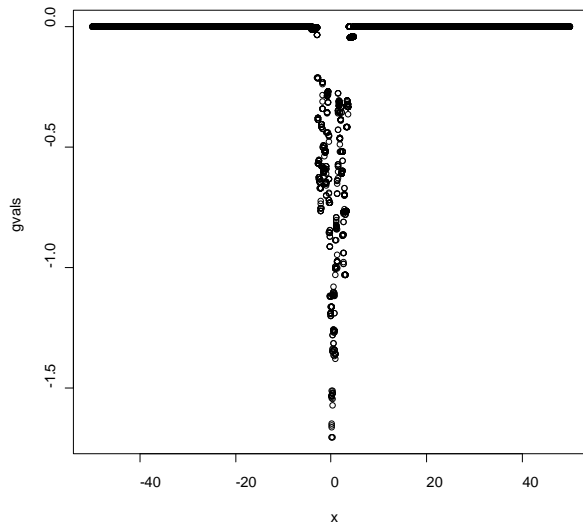
it takes 575.384000 seconds to test the local acceptance

1

[1] 13.51092
[1] 0.01197586
[1] 0.2913418

2.1.4.15 case 65 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 5, $C = 0.01$, $\gamma = 2$ with decreasing bandwidth

$$b_n = \frac{1}{n^{0.2}}$$



Accepted 22627 out of 100000 (22.627%).

final beta = 2.364856

alpha(0.000000) is 0.213898

alpha(2.000000) is 0.256772

alpha(5.000000) is 0.316926

alpha(10.000000) is 0.449290

alpha(20.000000) is 0.500463

alpha(50.000000) is 0.504012

alpha(100.000000) is 0.496350

alpha(150.000000) is 0.500614

it takes 128.110000 seconds to run the adaptation algorithm

it takes 56.517000 seconds to compute g and sigma

it takes 18.665000 seconds to generate the first Markov Chain

it takes 18.569000 seconds to generate the second Markov Chain

it takes 18.552000 seconds to generate the third Markov Chain

it takes 18.615000 seconds to generate the fourth Markov Chain

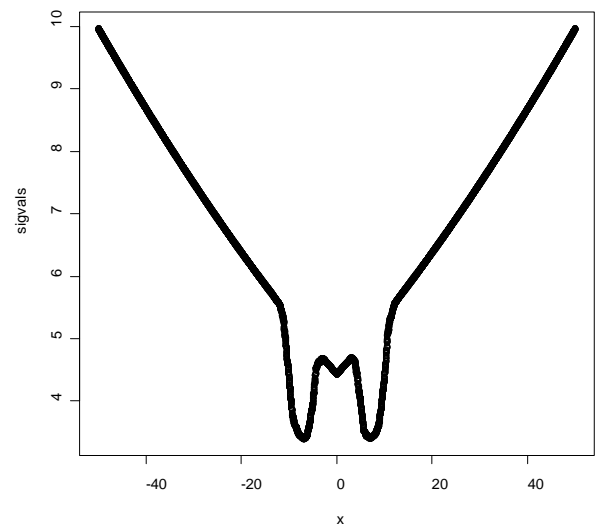
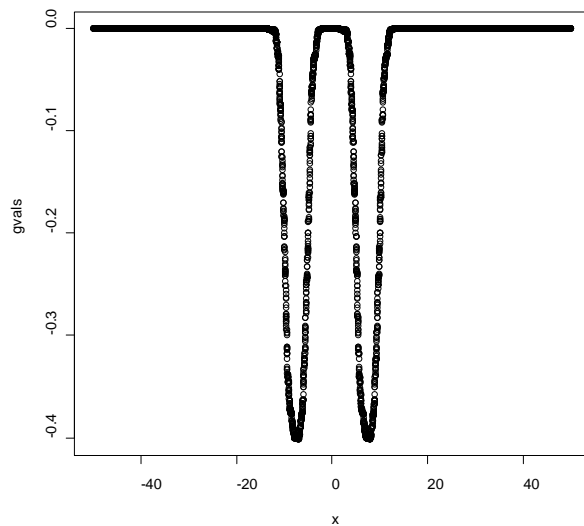
it takes 18.494000 seconds to generate the fifth Markov Chain

it takes 582.322000 seconds to test the local acceptance

1

[1] 7.970058
[1] 0.009514803
[1] 0.4789362

2.1.4.16 case 66 $\eta_n = \frac{1}{(n+5)^{0.8}}$, width = 5, $C = 0.01$, $\gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 26560 out of 100000 (26.560%).

final beta = 1.488413

alpha(0.000000) is 0.220851

alpha(2.000000) is 0.372854

alpha(5.000000) is 0.510782

alpha(10.000000) is 0.508244

alpha(20.000000) is 0.506292

alpha(50.000000) is 0.509547

alpha(100.000000) is 0.504294

alpha(150.000000) is 0.500956

it takes 125.194000 seconds to run the adaptation algorithm

it takes 55.229000 seconds to compute g and sigma

it takes 19.441000 seconds to generate the first Markov Chain

it takes 19.359000 seconds to generate the second Markov Chain

it takes 19.212000 seconds to generate the third Markov Chain

it takes 19.485000 seconds to generate the fourth Markov Chain

it takes 19.515000 seconds to generate the fifth Markov Chain

it takes 566.340000 seconds to test the local acceptance

1

```
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
```

```
[1] 5.940533
```

```
[1] 0.008155242
```

```
[1] 0.610068
```

2.3.5 constant $\sigma(x) = C$

The first run:

```
> cat("ran Metropolis algorithm for", M, "iterations, with burn-in", B, "\n");
ran Metropolis algorithm for 1e+05 iterations, with burn-in 10000
> cat("acceptance rate =", num/M, "\n");
acceptance rate = 0.23481
>
> varfact <- function(xxx) { 2 * sum(acf(xxx, plot=FALSE)$acf) - 1 }
> varf = varfact(xlist[(B+1):M]);
> se = sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
> val = 0
> for(i in (B+1):M )
+   val = val +(xlist[i]-xlist[i-1])^2
> asjd = val/(M-B)
>
> varf;
[1] 6.032679
> se;
[1] 0.008154245
> asjd;
[1] 0.5538456
```

The second run:

```
> cat("ran Metropolis algorithm for", M, "iterations, with burn-in", B, "\n");
ran Metropolis algorithm for 1e+05 iterations, with burn-in 10000
> cat("acceptance rate =", num/M, "\n");
acceptance rate = 0.23477
>
> varfact <- function(xxx) { 2 * sum(acf(xxx, plot=FALSE)$acf) - 1 }
> varf = varfact(xlist[(B+1):M]);
> se = sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
> val = 0
> for(i in (B+1):M )
+   val = val +(xlist[i]-xlist[i-1])^2
> asjd = val/(M-B)
>
> varf;
[1] 6.428601
> se;
[1] 0.008419095
> asjd;
```

```
[1] 0.5549895
```

The third run:

```
> cat("ran Metropolis algorithm for", M, "iterations, with burn-in", B, "\n");
ran Metropolis algorithm for 1e+05 iterations, with burn-in 10000
> cat("acceptance rate =", num/M, "\n");
acceptance rate = 0.23366
>
> varfact <- function(xxx) { 2 * sum(acf(xxx, plot=FALSE)$acf) - 1 }
> varf = varfact(xlist[(B+1):M]);
> se = sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
> val = 0
> for(i in (B+1):M )
+   val = val +(xlist[i]-xlist[i-1])^2
> asjd = val/(M-B)
>
> varf;
[1] 6.010923
> se;
[1] 0.008097415
> asjd;
[1] 0.5370982
```

The fourth run:

```
> cat("ran Metropolis algorithm for", M, "iterations, with burn-in", B, "\n");
ran Metropolis algorithm for 1e+05 iterations, with burn-in 10000
> cat("acceptance rate =", num/M, "\n");
acceptance rate = 0.23494
>
> varfact <- function(xxx) { 2 * sum(acf(xxx, plot=FALSE)$acf) - 1 }
> varf = varfact(xlist[(B+1):M]);
> se = sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );
> val = 0
> for(i in (B+1):M )
+   val = val +(xlist[i]-xlist[i-1])^2
> asjd = val/(M-B)
>
> varf;
[1] 6.143806
> se;
[1] 0.008276198
```

```
> asjd;  
[1] 0.5699829
```

The fifth run:

```
> cat("ran Metropolis algorithm for", M, "iterations, with burn-in", B, "\n");  
ran Metropolis algorithm for 1e+05 iterations, with burn-in 10000  
> cat("acceptance rate =", num/M, "\n");  
acceptance rate = 0.23071  
>  
> varfact <- function(xxx) { 2 * sum(acf(xxx, plot=FALSE)$acf) - 1 }  
> varf = varfact(xlist[(B+1):M]);  
> se = sd(xlist[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );  
> val = 0  
> for(i in (B+1):M )  
+   val = val +(xlist[i]-xlist[i-1])^2  
> asjd = val/(M-B)  
>  
> varf;  
[1] 6.654467  
> se;  
[1] 0.008502017  
> asjd;  
[1] 0.5473398
```

2.1.6 varfact comparison

kernel function $K(x) = e^{-\frac{ x ^{\alpha_1}}{\alpha_2}}$									
α_1	C	γ	η_n	b_n	First run	Second run	Third run	Fourth run	Fifth run
1	1	2	$\frac{1}{(n+5)^{0.5}}$	1	11.35909	12.05121	11.45263	10.70036	10.27269
2					12.87526	12.985	13.3621	12.5798	11.6263
10					11.95971	11.1817	12.009	11.1779	12.3533
0.1					12.4793	12.1969	12.509	12.4791	13.202
0.5					10.85975	9.60599	10.4611	11.1237	10.3478
2	2	15.7421			15.26345	15.33123	15.21730	14.3668	
	10	25.09042			30.3672	26.7781	28.74199	28.38106	
	0.1	6.533223			6.42219	6.045298	6.83526	6.91115	
	0.5	9.801138			9.868752	10.06519	10.29492	10.2363	
	0.01	6.521881			6.590561	7.095979	5.971771	6.151567	
	0.1	10	12.03479	11.71392	10.21051	10.77967	10.77254		
		0.5	6.6764022	6.618857	6.412747	6.739889	6.701922		
		1	7.184957	7.440486	7.480085	7.304401	8.057888		
		0.1	7.54	7.650029	6.898279	7.697511	7.061558		
		2	7.007102	7.612522	7.921151	7.508852	7.411572		
1	2	$\frac{1}{(n+5)^{0.8}}$	10	6.689204	6.323629	6.023003	6.549738	6.704092	
			0.1	7.638526	7.725935	8.350977	7.279248	7.577468	
			$\frac{1}{n^{0.2}}$	7.705133	7.408075	7.525139	7.189149	7.331579	

The best case is:

case 8 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth $b_n = 1$

kernel function $K(x) = \frac{1}{1 + \alpha_1 x ^{\alpha_2}}$									
α_1	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
1	1	2	1	$\frac{1}{(n+5)^{0.5}}$	10.69007	10.81582	11.26665	11.75963	10.69007
10					10.281	11.16265	11.00003	10.15537	12.06744
0.1					12.01854	14.03712	12.95212	12.25375	12.01854
1	10	26.62614			27.94747	28.96005	30.58577	26.62614	
	0.1	7.397457			7.050885	6.675549	7.357388	7.397457	
	0.01	6.515635			7.225982	6.216325	6.595525	6.515635	
	0.1	1			7.185476	6.92573	6.877931	7.298966	7.185476
		10			9.680703	9.388705	10.12533	11.79035	9.680703
		2			6.725084	6.679757	6.763915	7.555752	6.725084
		0.1			7.909221	7.823185	8.079191	8.019257	7.909221
		0.1	6.306029	6.253697	5.868809	6.429638	6.306029		
	2	$\frac{1}{n^{0.2}}$	6.861169	7.47218	7.089262	7.616252	6.861169		

			10	$\frac{1}{(n+5)^{0.8}}$	6.258227	5.779044	5.963561	6.285545	6.258227
--	--	--	----	-------------------------	----------	----------	----------	----------	----------

The best case is:

case 25 $\frac{1}{(n+5)^{0.8}}$ $\alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth $b_n = 10$

kernel function $K(x) = \begin{cases} 0, & x \geq 2 * width \\ -1 * height, & width < x < 2 * width \\ 1 * height, & x \leq width \end{cases}$														
C	γ	height	width	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run				
1	2	0.5	0.5	1	$\frac{1}{(n+5)^{0.5}}$	11.21697	11.01346	10.73923	11.00212	10.74114				
10						26.36981	27.70317	25.53938	24.13856	27.30234				
0.1						6.388425	6.44163	6.432831	6.348009	6.251577				
0.01						5.714605	6.093879	6.027745	6.093879	6.161878				
0						6.769783	6.339817	7.0314341	6.552781	6.861094				
0.001						6.480792	6.6654161	6.420364	6.372943	6.769786				
0.01	10	1	0.5	1	$\frac{1}{(n+5)^{0.5}}$	5.84989	6.229419	5.915948	6.139981	6.5259				
	1					6.338966	6.507104	5.854828	5.9643191	6.692964				
	0.1					6.755861	6.746315	6.918906	6.680906	6.49034				
	2	1	0.5	0.5	1	$\frac{1}{(n+5)^{0.5}}$	6.53588	5.974104	6.804957	6.391518	6.555601			
							10	9.536619	9.63294	9.340004	9.086103	9.308285		
							0.1	6.388736	5.793102	6.651792	6.726921	6.362033		
		0.5	2	0.5	0.5	1	$\frac{1}{(n+5)^{0.5}}$	6.989622	6.410413	6.045172	6.436296	7.392876		
								5	6.83254	6.885814	6.679356	6.848712	6.854895	
								0.1	6.610762	5.995149	6.148899	6.304812	6.081314	
								10	6.07822	6.375568	6.301751	6.438769	6.359084	
			0.5	0.1	0.5	0.5	1	$\frac{1}{(n+5)^{0.5}}$	6.460936	6.708183	6.249199	6.212332	6.130305	
									$\frac{1}{n^{0.2}}$	6.5368	7.150534	7.179354	7.156782	7.01146
									1	6.5368	7.150534	7.179354	7.156782	7.01146
									$\frac{1}{(n+5)^{0.8}}$	6.5368	7.150534	7.179354	7.156782	7.01146

The best case is:

case 38 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.5, width = 0.5, C = 0.01, $\gamma = 10$ with fixed bandwidth $b_n = 1$

Kernel function $K(x) = \begin{cases} 0, & x \geq 2 * width \text{ or } x \leq width \\ 1, & width < x < 2 * width \end{cases}$										
C	width	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run	
1	0.5	2	1	$\frac{1}{(n+5)^{0.5}}$	11.8298	11.3176	11.76312	11.11506	11.34705	
10					12.68587	12.2002	12.52693	12.71785	12.73849	
0.1					6.968693	7.780381	7.12373	6.84579	7.425369	

0.01					6.325229	6.238655	6.788932	6.642527	6.352072	
0.001					6.632203	6.651379	6.905611	6.9814	7.055358	
0.01	1	5			7.228149	6.63247	6.819531	6.440049	7.293104	
	5				5.72553	5.958359	5.350588	5.822084	5.500506	
	0.1				6.305438	6.342151	6.781963	6.660485	6.456669	
	8				7.512562	6.160492	6.884363	6.907896	6.965559	
	5	0.1	5			6.199165	6.789928	6.931863	6.463562	6.651483
			1			6.551915	6.891536	6.335435	6.279825	6.598833
			0.1			5.794013	6.270467	6.320622	6.509231	6.12154
		2	10			6.704157	6.904249	6.711725	6.449955	6.666041
			0.1			14.51732	13.42962	13.60299	13.92906	13.51092
			$\frac{1}{n^{0.2}}$			7.597946	7.456866	7.910384	7.821029	7.970058
			1	$\frac{1}{(n+5)^{0.8}}$		5.377442	5.680714	5.344205	5.464543	5.940533

The best case is:

case 57 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 5, $C = 0.01$, $\gamma = 2$ with fixed bandwidth $b_n = 1$

constant $\sigma(x) = C$				
First run	Second run	Third run	Fourth run	Fifth run
6.032679	6.428601	6.010923	6.143806	6.654467

2.1.7 variance comparison

kernel function $K(x) = e^{-\frac{ x ^{\alpha_1}}{\alpha_2}}$									
α_1	C	γ	η_n	b_n	First run	Second run	Third run	Fourth run	Fifth run
1	1	2	$\frac{1}{(n+5)^{0.5}}$	1	0.01122983	0.01172226	0.01136355	0.01089844	0.01078979
2					0.0118463	0.0120133	0.0122284	0.0116674	0.0111596
10					0.011360	0.0111945	0.0117056	0.0110526	0.0115645
0.1					0.0117178	0.0114601	0.0118072	0.0118785	0.0121816
0.5					0.0110567	0.0104420	0.0109040	0.0109978	0.0107297
2	2	0.0133701			0.0133216	0.0130189	0.0130471	0.0124461	
	10	0.0165678			0.0185194	0.0171344	0.0175987	0.0175510	
	0.1	0.0086311			0.0083967	0.0081392	0.0087408	0.0086971	
	0.5	0.0102999			0.0103018	0.0107431	0.0105740	0.010764	
	0.01	0.00852			0.0085	0.00899	0.00812	0.00832	
	0.1	10	0.0114	0.01135	0.01074	0.01113	0.01087		
		0.5	0.00871	0.00862	0.00835	0.00864	0.0087		
		1	0.00892	0.00901	0.0092	0.0091	0.00958		
		0.1	0.00909	0.00922	0.00868	0.00919	0.00885		
		2	0.00892	0.00919	0.00935	0.00916	0.009		
1	2	$\frac{1}{(n+5)^{0.8}}$	10	0.00863	0.00828	0.00813	0.00844	0.00855	
			0.1	0.00931	0.00922	0.00956	0.0089	0.00915	
			$\frac{1}{n^{0.2}}$	0.0093	0.00907	0.00906	0.00892	0.00883	

The best case is:

case 8 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth $b_n = 1$

kernel function $K(x) = \frac{1}{1 + \alpha_1 x ^{\alpha_2}}$									
α_1	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
1	1	2	1	$\frac{1}{(n+5)^{0.5}}$	0.01080392	0.01088505	0.01107906	0.01174345	0.01129308
10					0.0107729	0.01107101	0.01115669	0.01045884	0.01162421
0.1					0.0114314	0.01282429	0.01201123	0.0115313	0.01155291
1	10	0.01681819			0.01778243	0.01751706	0.01876566	0.01656713	
	0.1	0.009064997			0.008835046	0.008520924	0.009064476	0.008521907	
	0.01	0.008606985			0.008944422	0.008234797	0.008487706	0.008421049	
	1	0.00892049			0.008758606	0.00868717	0.008971944	0.009006958	
	10	0.01042457			0.01022211	0.01077376	0.01165331	0.01055025	
0.1	2	10			0.008629022	0.008642	0.008714656	0.009189865	0.008970417
	0.1	10			0.009410435	0.009324346	0.009459222	0.00931274	0.009549854
	0.1	10	0.008361173	0.008262193	0.008130423	0.008468772	0.008328171		
	2	$\frac{1}{n^{0.2}}$	0.00870455	0.00917211	0.00879794	0.00920209	0.00879953		

			10	$\frac{1}{(n+5)^{0.8}}$	0.00827424	0.00808351	0.00806594	0.00835063	0.00828150
--	--	--	----	-------------------------	------------	------------	------------	------------	------------

The best case is:

case 25 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 1$ with fixed bandwidth $b_n = 1$

kernel function $K(x) = \begin{cases} 0, & x \geq 2 * width \\ -1 * height, & width < x < 2 * width \\ 1 * height, & x \leq width \end{cases}$											
C	γ	height	width	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run	
1	2	0.5	0.5	1	$\frac{1}{(n+5)^{0.5}}$	0.01119531	0.01102779	0.01097638	0.01111038	0.01082565	
10						0.01708748	0.01719778	0.01633589	0.01621996	0.01750065	
0.1						0.00832147	0.00850810	0.00846442	0.00831120	0.00830861	
0.01						0.00796456	0.00818376	0.0081465	0.00818376	0.00825706	
0						0.00873404	0.00844347	0.00890642	0.00872350	0.00878673	
0.001						0.00849819	0.00867371	0.00841714	0.00832729	0.00862447	
0.01	10	0.5	0.5	1	$\frac{1}{(n+5)^{0.5}}$	0.00805243	0.00827595	0.00817826	0.00814704	0.00847703	
	1					0.0084309	0.0085183	0.00791077	0.00811096	0.00858695	
	0.1					0.0086998	0.00870021	0.00871831	0.00871517	0.00856057	
	2					1	0.00857281	0.00813515	0.00881743	0.00841922	0.00863647
						10	0.01022875	0.01028774	0.0103866	0.00999755	0.01020134
						0.1	0.00847153	0.00808108	0.00859385	0.00857070	0.00829111
	0.5	2	0.00883611	0.00846877	0.00813382	0.00846513	0.00902233				
		5	0.5247985	0.5225287	0.5246484	0.5300015	0.5201393				
		0.1	0.00867055	0.00873511	0.00868802	0.00864770	0.0087029				
		0.5	10	0.00858705	0.00829408	0.00832144	0.00814989	0.00825206			
			0.1	0.0081262	0.00833905	0.0082930	0.0084702	0.0084230			
	1	$\frac{1}{n^{0.2}}$	0.00843647	0.00861249	0.0083173	0.0081667	0.00825173				
	1	$\frac{1}{(n+5)^{0.8}}$	0.00856975	0.00877584	0.00891550	0.00881037	0.00888963				

The best case is:

case 38 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $height = 0.5, width = 0.5, C = 0.001, \gamma = 10$ with fixed bandwidth $b_n = 1$

Kernel function $K(x) = \begin{cases} 0, & x \geq 2 * width \text{ or } x \leq width \\ 1, & width < x < 2 * width \end{cases}$										
C	width	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run	
1	0.5	2	1	$\frac{1}{(n+5)^{0.5}}$	0.01145177	0.01115331	0.01128486	0.01087948	0.01121087	
10					0.01205766	0.01178141	0.01198769	0.01184585	0.01200023	
0.1					0.008753066	0.009387937	0.00893782	0.008729863	0.00926486	
0.01					0.008346846	0.008280165	0.008669679	0.008634343	0.008441499	

0.001					0.008636908	0.00860409	0.008797365	0.008743271	0.008838765
0.01	1	5			0.008857288	0.008613555	0.008615749	0.008473382	0.008969298
	5				0.00792509	0.008171163	0.007620757	0.008002132	0.007780254
	0.1				0.008363918	0.008285638	0.008547047	0.008700804	0.008401081
	8				0.009170728	0.008328777	0.008684492	0.008594844	0.008812787
					0.008384142	0.008724913	0.008774852	0.008414547	0.008605778
		0.008558539			0.008789663	0.008396568	0.008364616	0.008443037	
		0.008001875			0.008395209	0.00845136	0.008474585	0.00825666	
		0.00857308			0.008749343	0.008612675	0.00850364	0.008627651	
		0.01280593			0.01232926	0.01235656	0.01234854	0.0119758	
					2	10	0.009259425	0.009196404	0.009356108
			0.1						
			$\frac{1}{n^{0.2}}$						
			1	$\frac{1}{(n+5)^{0.8}}$	0.00780106	0.007956023	0.007668444	0.007867795	0.008155242

The best case is:

case 57 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 5, $C = 0.01$, $\gamma = 2$ with fixed bandwidth $b_n = 1$

constant $\sigma(x) = C$				
First run	Second run	Third run	Fourth run	Fifth run
0.00815424	0.00841909	0.00809741	0.00827619	0.00850201
5	5	5	8	7

2.1.8 comparison of average squared jump distance

kernel function $K(x) = e^{-\frac{ x ^{\alpha_1}}{\alpha_2}}$									
α_1	C	γ	η_n	b_n	First run	Second run	Third run	Fourth run	Fifth run
1	1	2	$\frac{1}{(n+5)^{0.5}}$	1	0.3482317	0.3378794	0.3383667	0.3463196	0.33542
2					0.3020888	0.3106892	0.3051376	0.3061098	0.309262
10					0.3301311	0.3358699	0.3388592	0.3208399	0.3275879
0.1					0.2985020	0.3010016	0.3049649	0.3073156	0.303518
0.5					0.3499498	0.3523485	0.3627218	0.3406725	0.3623652
2	2	0.270866			0.2717923	0.2693725	0.2657615	0.2595380	
	10	0.1661419			0.1613741	0.166271	0.1561579	0.1614916	
	0.1	0.545549			0.5252874	0.5203305	0.5352214	0.5301068	
	0.5	0.3768554			0.3621124	0.3841471	0.3711383	0.3784802	
	0.01	0.486626			0.47211	0.49826	0.49613	0.49295	
	0.1	10	0.35078	0.35504	0.37335	0.36722	0.35932		
		0.5	0.52328	0.51853	0.51545	0.52934	0.52331		
		1	0.48663	0.47211	0.49826	0.49613	0.49295		
		0.1	0.48265	0.48159	0.48307	0.47591	0.4898		
		2	0.494592	0.48125	0.47849	0.47118	0.477		
1	2	$\frac{1}{(n+5)^{0.8}}$	10	0.534894	0.52604	0.52935	0.51976	0.51584	
			0.1	0.458733	0.45319	0.45694	0.44814	0.45777	
			$\frac{1}{n^{0.2}}$	0.486247	0.48948	0.48803	0.48851	0.48079	

The best case is:

case 8 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth $b_n = 1$

kernel function $K(x) = \frac{1}{1 + \alpha_1 x ^{\alpha_2}}$										
α_1	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run	
1	1	2	1	$\frac{1}{(n+5)^{0.5}}$	0.3387809	0.3446142	0.3314934	0.3495083	0.3478964	
10					0.3506148	0.3349281	0.342898	0.3357567	0.333423	
0.1					0.3169546	0.3205971	0.3261828	0.3104705	0.3238721	
1	10				0.159876	0.1661034	0.1576704	0.1617906	0.1643911	
	0.1				0.4906771	0.4946082	0.4807281	0.4897404	0.4765741	
	0.01				0.5466972	0.5388166	0.5297919	0.5527384	0.5429365	
	0.1				1	0.5146352	0.5145474	0.5087591	0.4962806	0.5071021
					10	0.4082753	0.4054954	0.4134897	0.410045	0.3960828
					2	0.5297551	0.5084722	0.5256346	0.5121834	0.5260427
					0.1	0.447282	0.437752	0.4453548	0.43688	0.4514627
		10	0.5614798	0.5495616	0.5841707	0.5634893	0.5697796			
	2	$\frac{1}{n^{0.2}}$	0.498937	0.5065231	0.485246	0.488642	0.4994858			

			10	$\frac{1}{(n+5)^{0.8}}$	0.5487379	0.5700657	0.5551277	0.5553396	0.5653669
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The best case is:

case 29 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 0.1$ with fixed bandwidth $b_n = 10$

kernel function $K(x) = \begin{cases} 0, & x \geq 2 * width \\ -1 * height, & width < x < 2 * width \\ 1 * height, & x \leq width \end{cases}$											
C	γ	height	width	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run	
1	2	0.5	0.5	1	$\frac{1}{(n+5)^{0.5}}$	0.3480791	0.3393188	0.3521589	0.3414209	0.3407953	
10						0.1717606	0.1693742	0.169111	0.1736697	0.1734251	
0.1						0.5400879	0.5459329	0.5532259	0.5478521	0.5388973	
0.01						0.5832376	0.5765046	0.5731739	0.5765046	0.5782485	
0						0.5437982	0.5434355	0.5379284	0.5601083	0.5409318	
0.001						0.5554767	0.5492348	0.5508303	0.5473217	0.5400489	
0.01	10	1	0.5	1	$\frac{1}{(n+5)^{0.5}}$	0.5757201	0.5650518	0.5851384	0.5462827	0.555975	
	1					0.5539996	0.5513252	0.52823	0.5416636	0.5457672	
	0.1					0.531748	0.5351088	0.5204629	0.5416667	0.5352067	
	2					1	0.5418091	0.536561	0.5630413	0.548019	0.5541553
						10	0.4327383	0.4517592	0.4476535	0.4391682	0.4585032
						0.1	0.5548144	0.572752	0.5579829	0.5399683	0.5503619
	2	0.5	2	0.5230771	0.5227794	0.5236362	0.5200925	0.5164709			
			5	0.5615815	0.5478925	0.5628432	0.5608967	0.5518468			
			0.1	0.5533189	0.5475685	0.5356417	0.5613171	0.554771			
			10	0.5306976	0.5047632	0.5114743	0.510878	0.5306071			
			0.1	0.5306976	0.5047632	0.5114743	0.5108781	0.5306071			
	2	0.5	$\frac{1}{n^{0.2}}$	0.3480791	0.3393188	0.3521589	0.3414209	0.3407953			
			1	$\frac{1}{(n+5)^{0.8}}$	0.1717606	0.1693742	0.169111	0.1736697	0.1734251		

The best case is:

case 38 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $height = 0.5, width = 0.5, C = 0.001, \gamma = 10$ with fixed bandwidth $b_n = 1$

Kernel function $K(x) = \begin{cases} 0, & x \geq 2 * width \text{ or } x \leq width \\ 1, & width < x < 2 * width \end{cases}$										
C	width	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run	
1	0.5	2	1	$\frac{1}{(n+5)^{0.5}}$	0.316954	0.3105255	0.3226398	0.3064963	0.3157405	
10					0.4793217	0.4780706	0.4868769	0.4790695	0.4934043	
0.1					0.5616479	0.562497	0.5484761	0.5583827	0.5698832	
0.01					0.5399391	0.5072552	0.5181693	0.5078605	0.5103956	

0.001					0.5201501	0.5321433	0.5283818	0.5313193	0.5260217	
0.01	1	5			0.5872723	0.0605619	0.5860981	0.5982348	0.5968249	
	5				0.5499262	0.5435791	0.5322315	0.5504899	0.5444502	
	0.1				0.537842	0.546856	0.5303485	0.5117296	0.5334517	
	8				0.5624894	0.5548582	0.5508696	0.538276	0.5450531	
					0.5510387	0.5559884	0.5598121	0.5568019	0.5469699	
		1	2	10	0.5684341	0.5686782	0.5763505	0.5646907	0.5646845	
		0.1		0.1	0.5350034	0.5295421	0.5335563	0.5449261	0.541695	
				0.1	0.3080717	0.3065731	0.316869	0.3040506	0.2913418	
				$\frac{1}{n^{0.2}}$	0.4785666	0.475891	0.4682705	0.4743092	0.4789362	
				1	$\frac{1}{(n+5)^{0.8}}$	0.6113059	0.5972358	0.6040591	0.6167911	0.610068
						0.316954	0.3105255	0.3226398	0.3064963	0.3157405

The best case is:

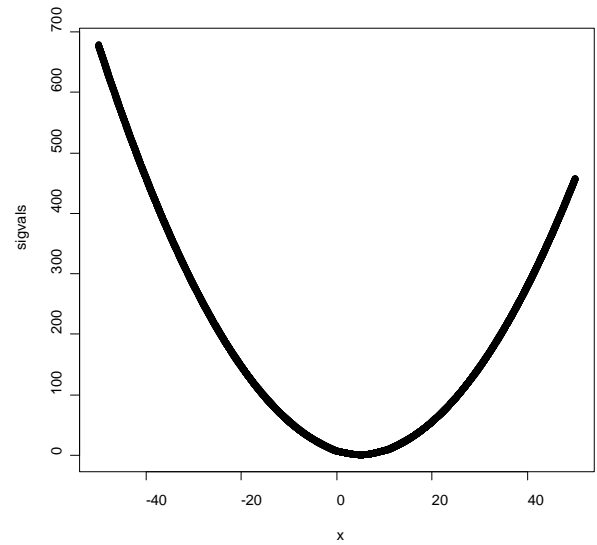
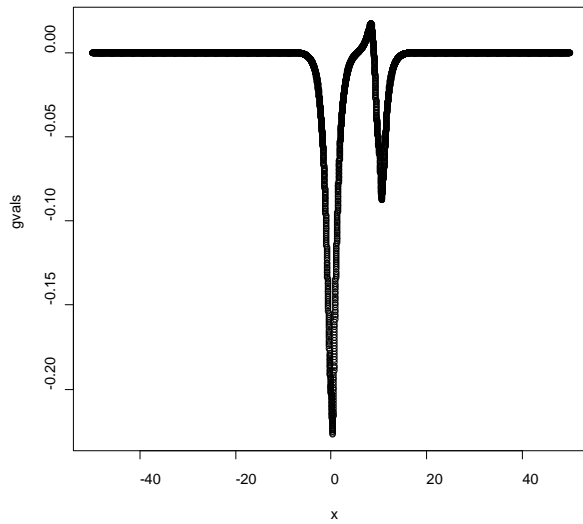
case 65 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 5, $C = 0.01$, $\gamma = 2$ with decreasing bandwidth $b_n = \frac{1}{n^{0.2}}$

constant $\sigma(x) = C$				
First run	Second run	Third run	Fourth run	Fifth run
0.553845	0.5549895	0.537098	0.569982	0.547339
6		2	9	8

2.2 Example 2: mixture of two normal distributions in R^1

2.2.1 kernel function $K(x) = e^{-\frac{|x|^{\alpha_1}}{\alpha_2}}$

2.2.1.1 case 67 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 23354 out of 100000 (23.354%).

final beta = -1.530327

alpha(5.000000) is 0.981209

alpha(7.000000) is 0.595073

alpha(10.000000) is 0.183040

alpha(20.000000) is 0.182034

alpha(30.000000) is 0.125577

alpha(50.000000) is 0.081246

alpha(70.000000) is 0.054118

alpha(120.000000) is 0.032300

alpha(150.000000) is 0.024200

it takes 211.785000 seconds to run the adaptation algorithm

it takes 93.757000 seconds to compute g and sigma

it takes 2380.770000 seconds to generate the first Markov Chain

it takes 2437.619000 seconds to generate the second Markov Chain

it takes 2437.086000 seconds to generate the third Markov Chain

it takes 2367.840000 seconds to generate the fourth Markov Chain

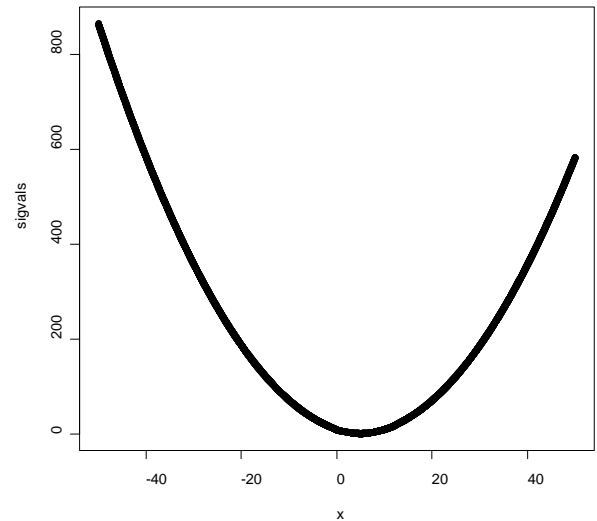
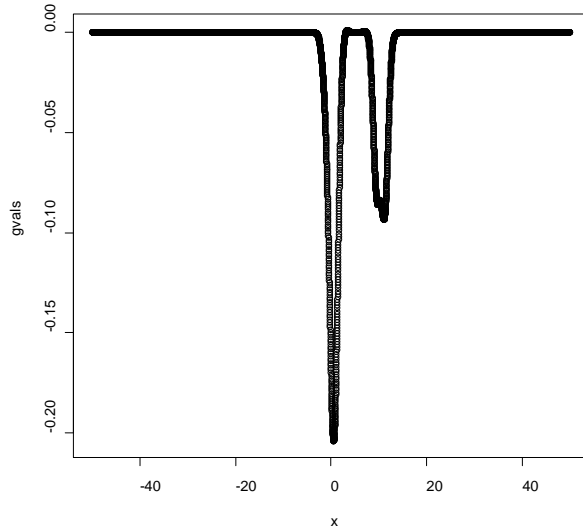
it takes 2366.400000 seconds to generate the fifth Markov Chain

it takes 3924.334000 seconds to test the local acceptance

1

[1] 17.14759
[1] 0.07038708
[1] 5.778095

2.2.1.2 case 68 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 21366 out of 100000 (21.366%).

final beta = -1.287503

alpha(5.000000) is 0.989037

alpha(7.000000) is 0.623838

alpha(10.000000) is 0.167483

alpha(20.000000) is 0.152847

alpha(30.000000) is 0.104381

alpha(50.000000) is 0.053026

alpha(70.000000) is 0.042200

alpha(120.000000) is 0.024900

alpha(150.000000) is 0.020700

it takes 213.984000 seconds to run the adaptation algorithm

it takes 140.214000 seconds to compute g and sigma

it takes 21.567000 seconds to generate the first Markov Chain

it takes 22.135000 seconds to generate the second Markov Chain

it takes 21.171000 seconds to generate the third Markov Chain

it takes 21.428000 seconds to generate the fourth Markov Chain

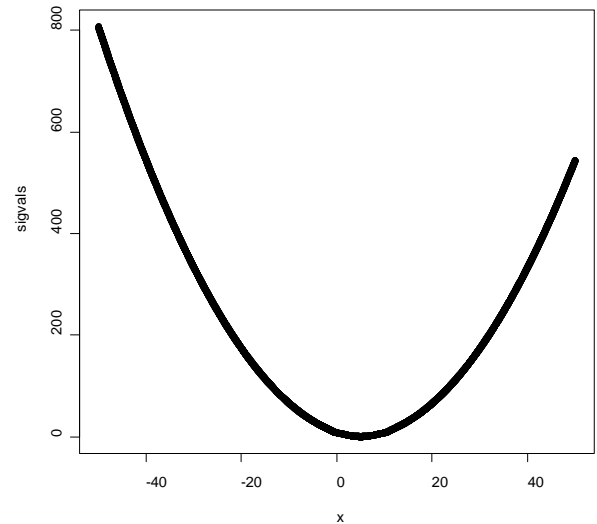
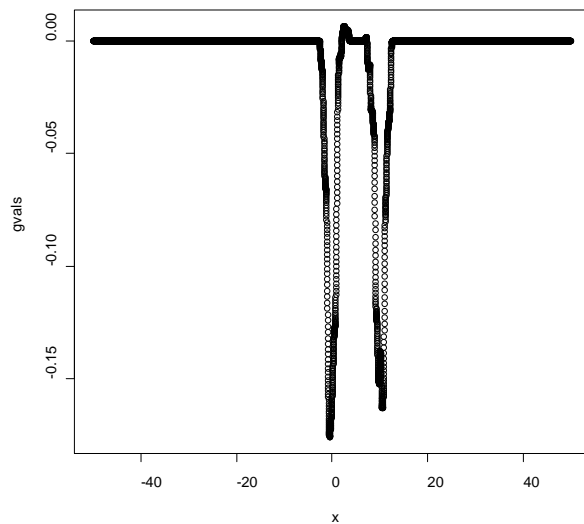
it takes 21.561000 seconds to generate the fifth Markov Chain

it takes 3266.257000 seconds to test the local acceptance

1

[1] 13.98678
[1] 0.06355741
[1] 6.943634

2.2.1.3 case 69 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 21953 out of 100000 (21.953%).

final beta = -1.356750

alpha(5.000000) is 0.988818

alpha(7.000000) is 0.610090

alpha(10.000000) is 0.176504

alpha(20.000000) is 0.159430

alpha(30.000000) is 0.108443

alpha(50.000000) is 0.058606

alpha(70.000000) is 0.043800

alpha(120.000000) is 0.026200

alpha(150.000000) is 0.023200

it takes 286.940000 seconds to run the adaptation algorithm

it takes 135.983000 seconds to compute g and sigma

it takes 21.773000 seconds to generate the first Markov Chain

it takes 21.542000 seconds to generate the second Markov Chain

it takes 22.802000 seconds to generate the third Markov Chain

it takes 21.843000 seconds to generate the fourth Markov Chain

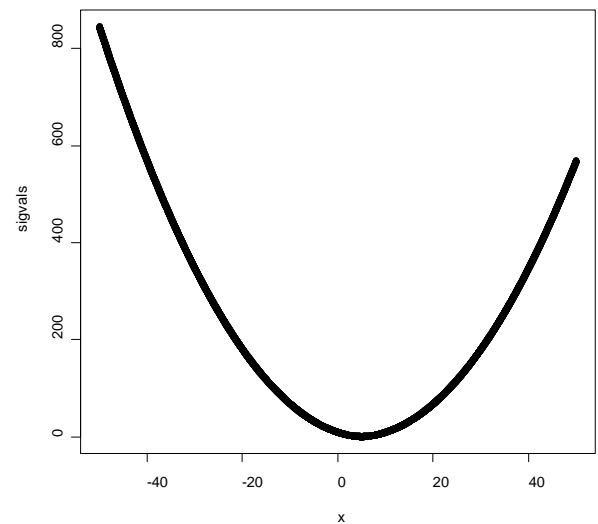
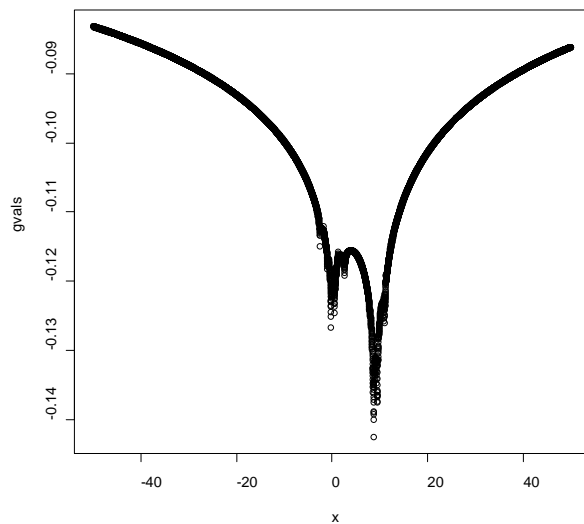
it takes 21.417000 seconds to generate the fifth Markov Chain

it takes 2777.904000 seconds to test the local acceptance

1

[1] 15.06675
 [1] 0.06591678
 [1] 6.664103

.2.1.4 case 70 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 21238 out of 100000 (21.238%).

final beta = -1.227692

alpha(5.000000) is 0.988853

alpha(7.000000) is 0.600787

alpha(10.000000) is 0.173634

alpha(20.000000) is 0.155803

alpha(30.000000) is 0.103307

alpha(50.000000) is 0.061476

alpha(70.000000) is 0.044889

alpha(120.000000) is 0.023100

alpha(150.000000) is 0.020700

it takes 238.775000 seconds to run the adaptation algorithm

it takes 104.928000 seconds to compute g and sigma

it takes 23.019000 seconds to generate the first Markov Chain

it takes 22.909000 seconds to generate the second Markov Chain

it takes 22.931000 seconds to generate the third Markov Chain

it takes 23.262000 seconds to generate the fourth Markov Chain

it takes 23.417000 seconds to generate the fifth Markov Chain

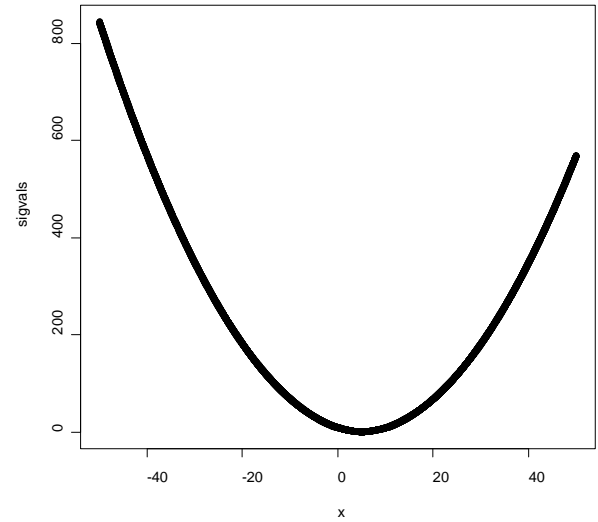
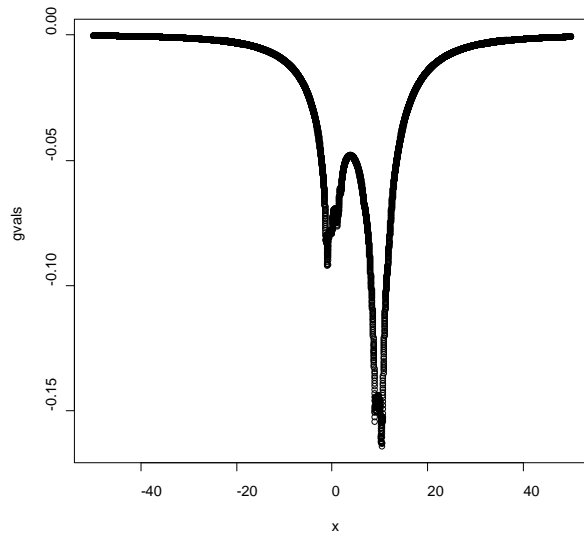
it takes 2066.982000 seconds to test the local acceptance

|

[1] 13.59459
[1] 0.06266335
[1] 7.059283

2.2.1.5 case 71 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.5, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth

$b_n = 1$



Accepted 21238 out of 100000 (21.238%).

final beta = -1.227692

alpha(5.000000) is 0.988853

alpha(7.000000) is 0.600787

alpha(10.000000) is 0.173634

alpha(20.000000) is 0.155803

alpha(30.000000) is 0.103307

alpha(50.000000) is 0.061476

alpha(70.000000) is 0.044889

alpha(120.000000) is 0.023100

alpha(150.000000) is 0.020700

it takes 238.775000 seconds to run the adaptation algorithm

it takes 104.928000 seconds to compute g and sigma

it takes 23.019000 seconds to generate the first Markov Chain

it takes 22.909000 seconds to generate the second Markov Chain

it takes 22.931000 seconds to generate the third Markov Chain

it takes 23.262000 seconds to generate the fourth Markov Chain

it takes 23.417000 seconds to generate the fifth Markov Chain

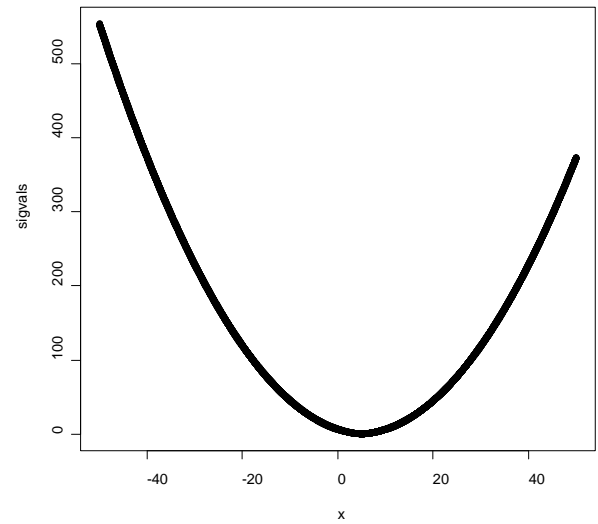
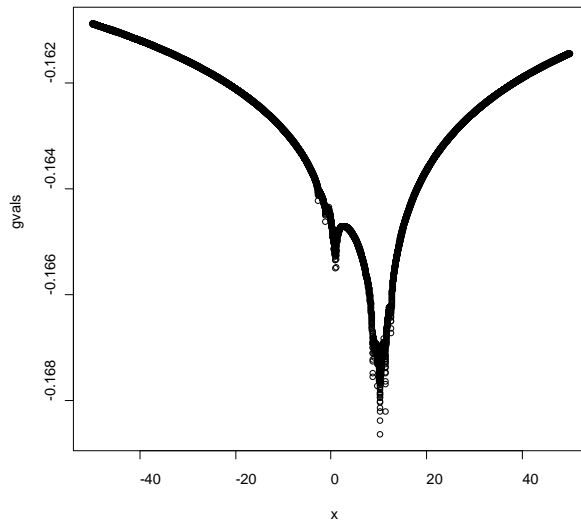
it takes 2066.982000 seconds to test the local acceptance

1

[1] 13.72507
[1] 0.06299655
[1] 6.884881

2.2.1.6 case 72 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.01, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth

$b_n = 1$



Accepted 24931 out of 100000 (24.931%).

final beta = -1.573366

alpha(5.000000) is 0.988528

alpha(7.000000) is 0.600182

alpha(10.000000) is 0.210625

alpha(20.000000) is 0.218254

alpha(30.000000) is 0.156754

alpha(50.000000) is 0.093247

alpha(70.000000) is 0.066904

alpha(120.000000) is 0.039000

alpha(150.000000) is 0.030100

it takes 227.191000 seconds to run the adaptation algorithm

it takes 102.547000 seconds to compute g and sigma

it takes 21.391000 seconds to generate the first Markov Chain

it takes 20.529000 seconds to generate the second Markov Chain

it takes 20.712000 seconds to generate the third Markov Chain

it takes 22.904000 seconds to generate the fourth Markov Chain

it takes 20.531000 seconds to generate the fifth Markov Chain

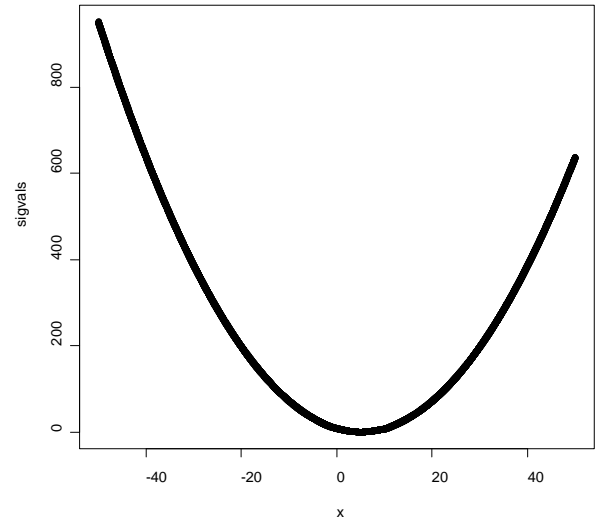
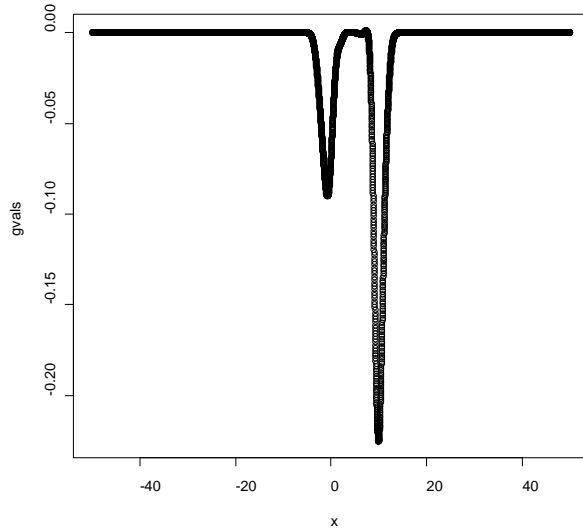
it takes 1969.599000 seconds to test the local acceptance

1

[1] 21.60776
[1] 0.0791383
[1] 4.975623

2.2.1.7 case 73 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 10, \gamma = 2$ with fixed bandwidth

$b_n = 1$



Accepted 23009 out of 100000 (23.009%).

final beta = -5.765632

alpha(5.000000) is 0.958174

alpha(7.000000) is 0.597633

alpha(10.000000) is 0.198928

alpha(20.000000) is 0.139649

alpha(30.000000) is 0.087800

alpha(50.000000) is 0.055351

alpha(70.000000) is 0.038322

alpha(120.000000) is 0.023300

alpha(150.000000) is 0.016500

it takes 220.284000 seconds to run the adaptation algorithm

it takes 139.986000 seconds to compute g and sigma

it takes 20.836000 seconds to generate the first Markov Chain

it takes 20.884000 seconds to generate the second Markov Chain

it takes 20.730000 seconds to generate the third Markov Chain

it takes 20.737000 seconds to generate the fourth Markov Chain

it takes 20.583000 seconds to generate the fifth Markov Chain

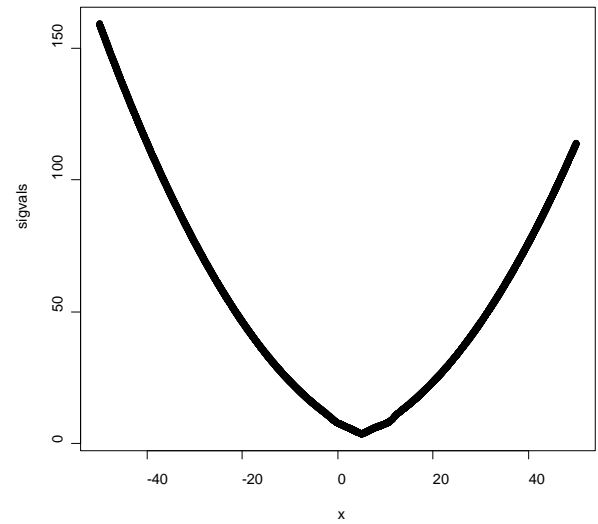
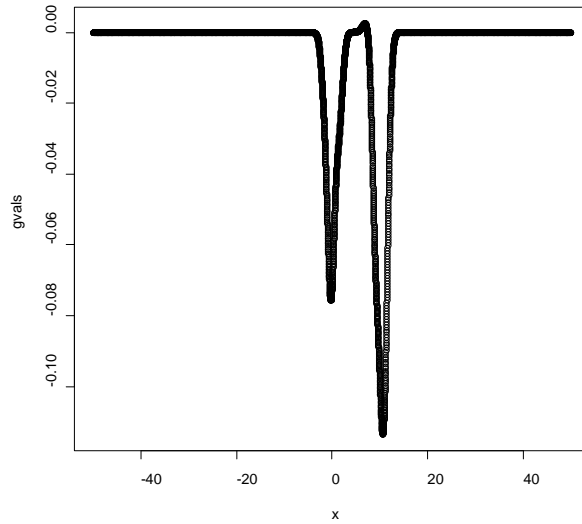
it takes 3317.109000 seconds to test the local acceptance

1

[1] 18.24566
[1] 0.07269454
[1] 5.745729

2.2.1.8 case 74 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$b_n = 1$



Accepted 23165 out of 100000 (23.165%).

final beta = 1.326566

alpha(5.000000) is 0.994617

alpha(7.000000) is 0.626367

alpha(10.000000) is 0.179817

alpha(20.000000) is 0.407404

alpha(30.000000) is 0.364035

alpha(50.000000) is 0.281372

alpha(70.000000) is 0.229441

alpha(120.000000) is 0.146200

alpha(150.000000) is 0.125800

it takes 225.062000 seconds to run the adaptation algorithm

it takes 147.438000 seconds to compute g and sigma

it takes 21.056000 seconds to generate the first Markov Chain

it takes 21.647000 seconds to generate the second Markov Chain

it takes 21.773000 seconds to generate the third Markov Chain

it takes 21.205000 seconds to generate the fourth Markov Chain

it takes 21.122000 seconds to generate the fifth Markov Chain

it takes 2874.449000 seconds to test the local acceptance

|

```
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M] ) );asjd(xlist[(B+1):M]);
```

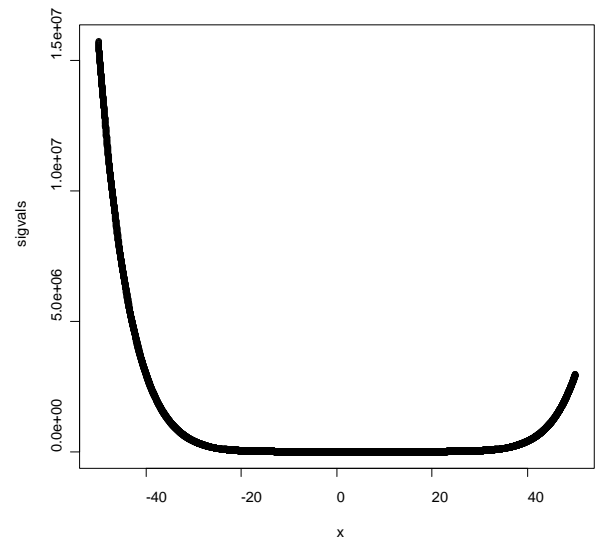
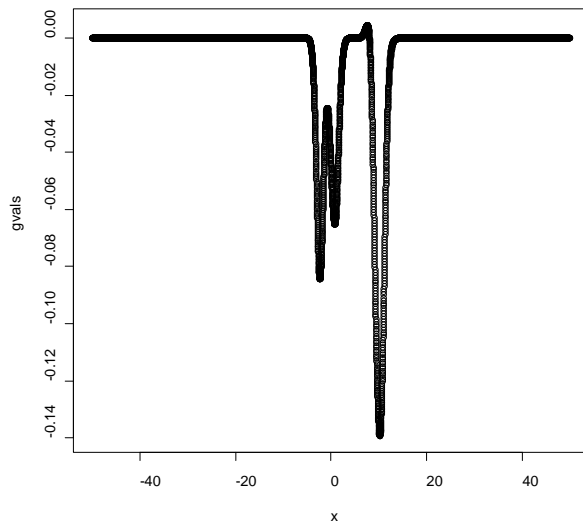
```
[1] 12.56142
```

```
[1] 0.06021042
```

```
[1] 7.484434
```

2.2.1.9 case 75 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 10$ with fixed bandwidth

$b_n = 1$



Accepted 23299 out of 100000 (23.299%).

final beta = -2.146768

alpha(5.000000) is 0.998253

alpha(7.000000) is 0.659461

alpha(10.000000) is 0.201391

alpha(20.000000) is 0.008940

alpha(30.000000) is 0.000600

alpha(50.000000) is 0.000000

alpha(70.000000) is 0.000000

alpha(120.000000) is 0.000000

alpha(150.000000) is 0.000000

it takes 217.680000 seconds to run the adaptation algorithm

it takes 145.329000 seconds to compute g and sigma

it takes 27.535000 seconds to generate the first Markov Chain

it takes 29.751000 seconds to generate the second Markov Chain

it takes 27.858000 seconds to generate the third Markov Chain

it takes 28.172000 seconds to generate the fourth Markov Chain

it takes 29.909000 seconds to generate the fifth Markov Chain

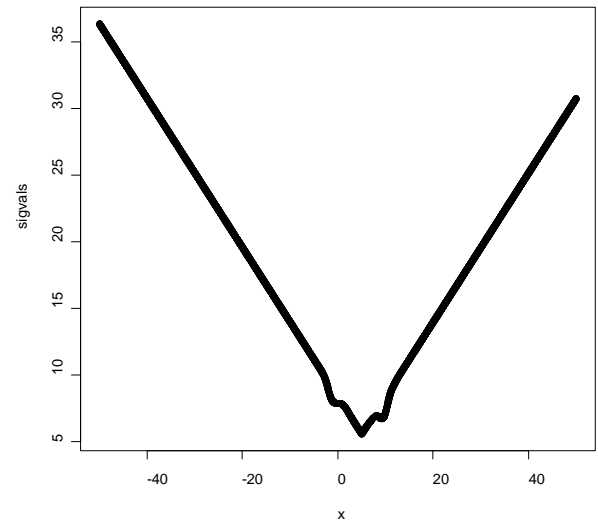
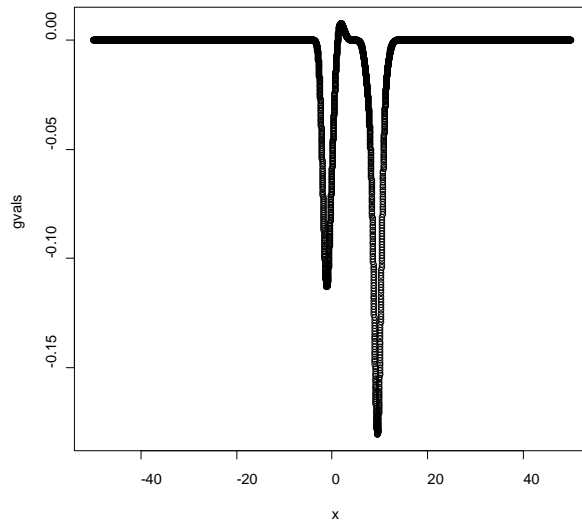
it takes 3552.758000 seconds to test the local acceptance

1

[1] 33.06702
[1] 0.09774311
[1] 3.609716

2.2.1.10 case 76 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 1$ with fixed bandwidth

$b_n = 1$



Accepted 23278 out of 100000 (23.278%).

final beta = 1.720646

alpha(5.000000) is 0.932807

alpha(7.000000) is 0.579465

alpha(10.000000) is 0.189430

alpha(20.000000) is 0.478537

alpha(30.000000) is 0.497733

alpha(50.000000) is 0.497044

alpha(70.000000) is 0.499786

alpha(120.000000) is 0.510260

alpha(150.000000) is 0.494803

it takes 219.482000 seconds to run the adaptation algorithm

it takes 145.520000 seconds to compute g and sigma

it takes 22.165000 seconds to generate the first Markov Chain

it takes 21.901000 seconds to generate the second Markov Chain

it takes 21.597000 seconds to generate the third Markov Chain

it takes 21.378000 seconds to generate the fourth Markov Chain

it takes 22.742000 seconds to generate the fifth Markov Chain

it takes 2409.464000 seconds to test the local acceptance

1

```
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M] ) );asjd(xlist[(B+1):M]);
```

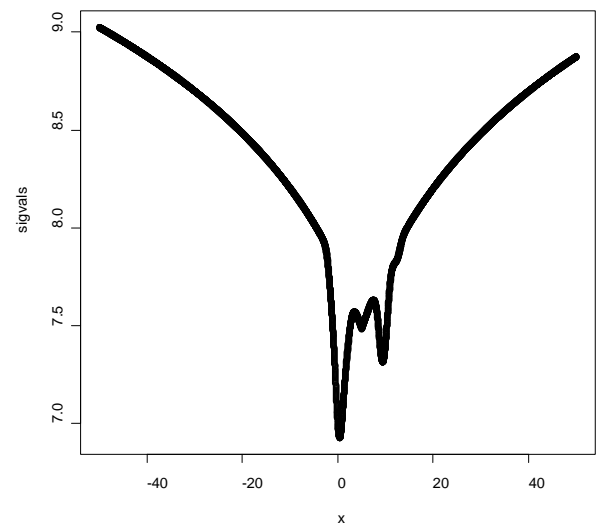
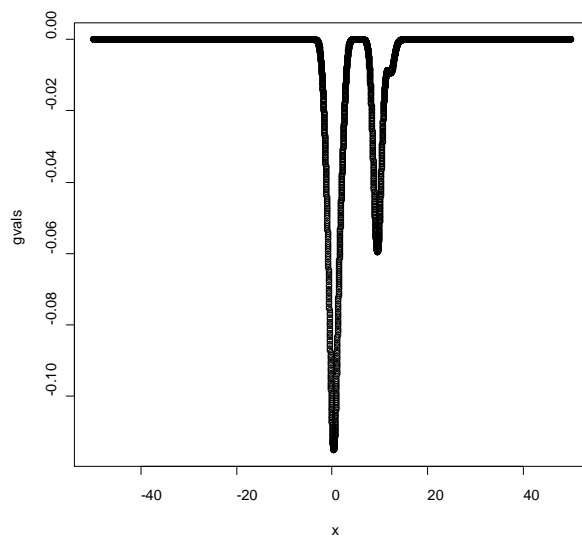
```
[1] 12.76278
```

```
[1] 0.06078702
```

```
[1] 7.467558
```

2.2.1.11 case 77 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 0.1$ with fixed bandwidth

$b_n = 1$



Accepted 23701 out of 100000 (23.701%).

final beta = 2.012694

alpha(5.000000) is 0.817731

alpha(7.000000) is 0.540472

alpha(10.000000) is 0.186645

alpha(20.000000) is 0.505608

alpha(30.000000) is 0.501515

alpha(50.000000) is 0.504638

alpha(70.000000) is 0.499089

alpha(120.000000) is 0.501855

alpha(150.000000) is 0.504430

it takes 487.270000 seconds to run the adaptation algorithm

it takes 277.239000 seconds to compute g and sigma

it takes 51.754000 seconds to generate the first Markov Chain

it takes 53.247000 seconds to generate the second Markov Chain

it takes 54.769000 seconds to generate the third Markov Chain

it takes 53.697000 seconds to generate the fourth Markov Chain

it takes 50.302000 seconds to generate the fifth Markov Chain

it takes 4301.456000 seconds to test the local acceptance

1

```
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
```

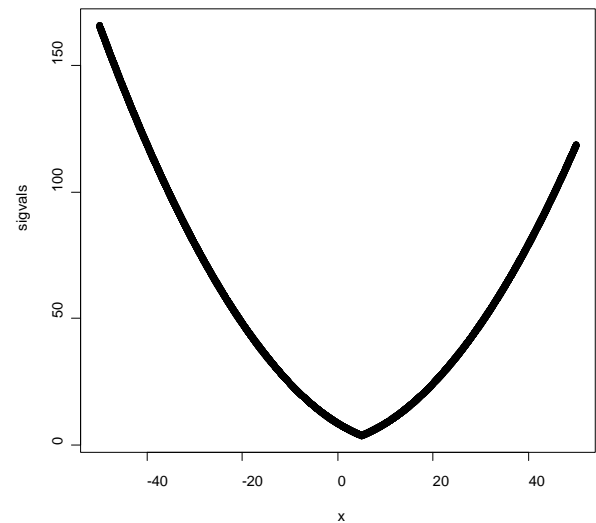
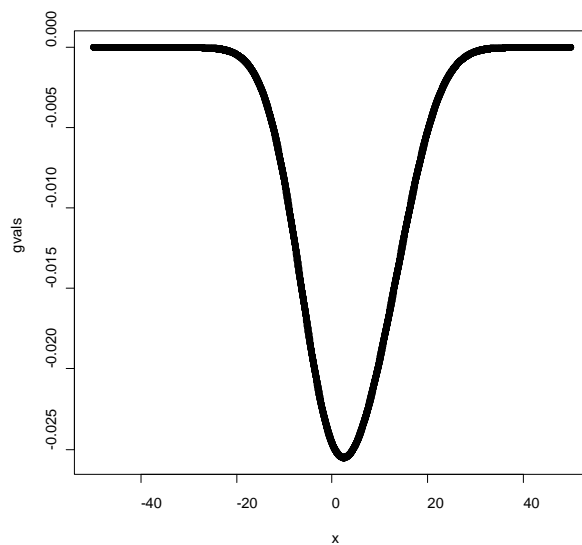
```
[1] 14.24509
```

```
[1] 0.06419357
```

```
[1] 6.900112
```

2.2.1.12 case 78 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$b_n = 10$



Accepted 22066 out of 100000 (22.066%).

final beta = 1.366644

alpha(5.000000) is 0.993489

alpha(7.000000) is 0.616531

alpha(10.000000) is 0.177149

alpha(20.000000) is 0.392194

alpha(30.000000) is 0.338101

alpha(50.000000) is 0.271826

alpha(70.000000) is 0.228907

alpha(120.000000) is 0.147800

alpha(150.000000) is 0.124100

it takes 225.032000 seconds to run the adaptation algorithm

it takes 100.500000 seconds to compute g and sigma

it takes 21.698000 seconds to generate the first Markov Chain

it takes 21.345000 seconds to generate the second Markov Chain

it takes 21.250000 seconds to generate the third Markov Chain

it takes 21.398000 seconds to generate the fourth Markov Chain

it takes 22.055000 seconds to generate the fifth Markov Chain

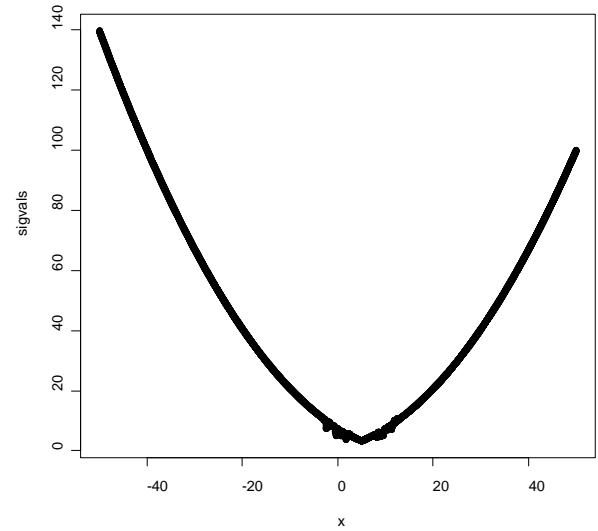
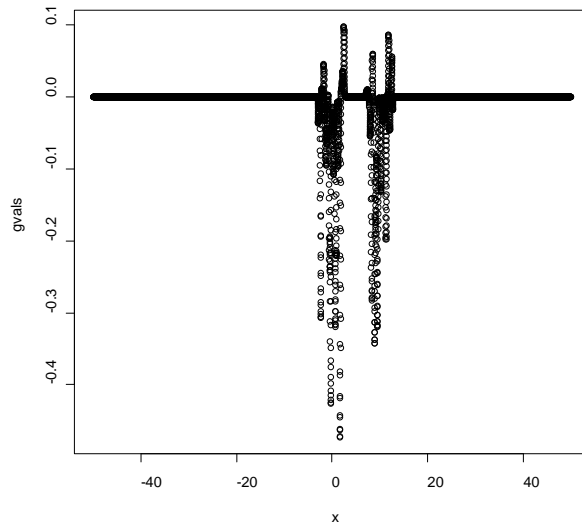
it takes 2007.569000 seconds to test the local acceptance

1

[1] 12.88139
[1] 0.06114331
[1] 7.709572

2.2.1.13 case 79 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$b_n = 0.1$



Accepted 24301 out of 100000 (24.301%).

final beta = 1.194554

alpha(5.000000) is 0.998548

alpha(7.000000) is 0.641290

alpha(10.000000) is 0.196131

alpha(20.000000) is 0.437494

alpha(30.000000) is 0.399110

alpha(50.000000) is 0.316721

alpha(70.000000) is 0.254963

alpha(120.000000) is 0.171400

alpha(150.000000) is 0.141227

it takes 351.445000 seconds to run the adaptation algorithm

it takes 153.841000 seconds to compute g and sigma

it takes 21.685000 seconds to generate the first Markov Chain

it takes 21.738000 seconds to generate the second Markov Chain

it takes 21.278000 seconds to generate the third Markov Chain

it takes 21.452000 seconds to generate the fourth Markov Chain

it takes 21.341000 seconds to generate the fifth Markov Chain

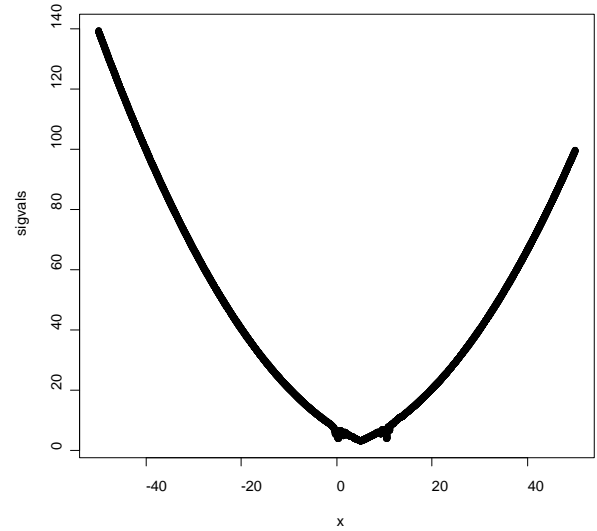
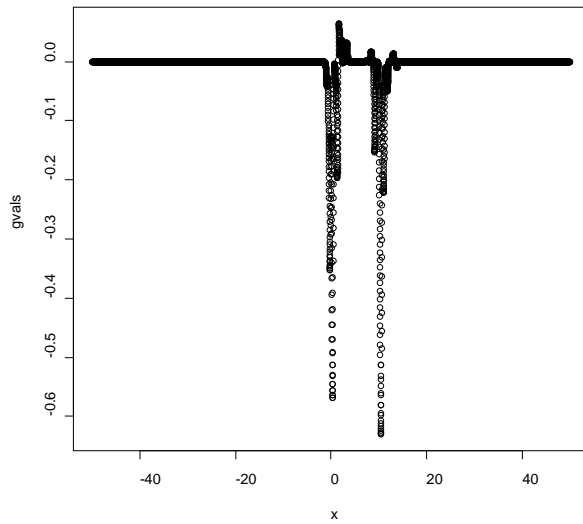
it takes 2306.552000 seconds to test the local acceptance

1

[1] 15.5557
 [1] 0.06697404
 [1] 6.533062

2.2.1.14 case 80 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with decreasing

bandwidth $b_n = \frac{1}{n^{0.2}}$



Accepted 24208 out of 100000 (24.208%).

final beta = 1.192546

alpha(5.000000) is 0.998591

alpha(7.000000) is 0.640761

alpha(10.000000) is 0.194188

alpha(20.000000) is 0.425004

alpha(30.000000) is 0.392819

alpha(50.000000) is 0.317502

alpha(70.000000) is 0.260490

alpha(120.000000) is 0.171910

alpha(150.000000) is 0.144109

it takes 324.573000 seconds to run the adaptation algorithm

it takes 153.297000 seconds to compute g and sigma

it takes 20.367000 seconds to generate the first Markov Chain

it takes 20.281000 seconds to generate the second Markov Chain

it takes 20.337000 seconds to generate the third Markov Chain

it takes 20.305000 seconds to generate the fourth Markov Chain

it takes 20.278000 seconds to generate the fifth Markov Chain

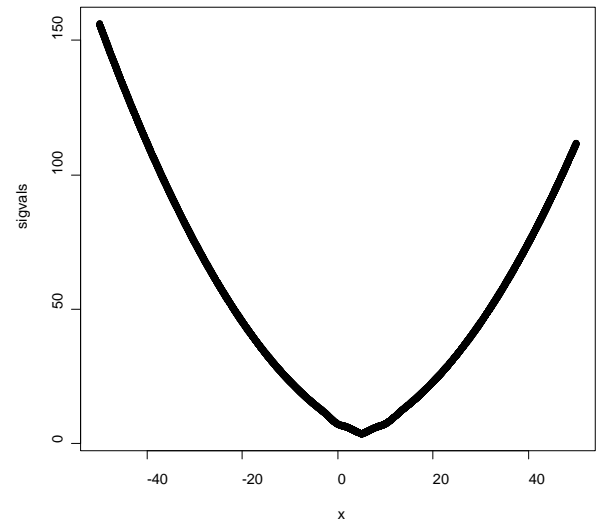
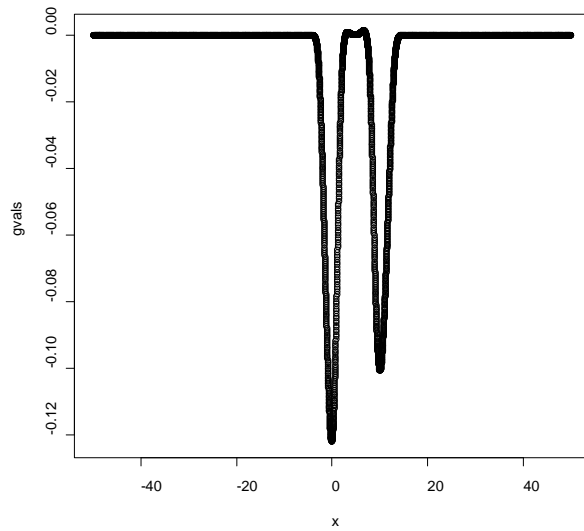
it takes 2252.503000 seconds to test the local acceptance

1

[1] 17.61966
[1] 0.0711586
[1] 6.218763

2.2.1.15 case 81 $\eta_n = \frac{1}{(n+5)^{0.8}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$b_n = 10$



Accepted 23329 out of 100000 (23.329%).

final beta = 1.307548

alpha(5.000000) is 0.994511

alpha(7.000000) is 0.618129

alpha(10.000000) is 0.182081

alpha(20.000000) is 0.409533

alpha(30.000000) is 0.366793

alpha(50.000000) is 0.289425

alpha(70.000000) is 0.239334

alpha(120.000000) is 0.158200

alpha(150.000000) is 0.128500

it takes 214.443000 seconds to run the adaptation algorithm

it takes 139.279000 seconds to compute g and sigma

it takes 20.489000 seconds to generate the first Markov Chain

it takes 20.609000 seconds to generate the second Markov Chain

it takes 20.549000 seconds to generate the third Markov Chain

it takes 20.468000 seconds to generate the fourth Markov Chain

it takes 20.479000 seconds to generate the fifth Markov Chain

it takes 2795.277000 seconds to test the local acceptance

1

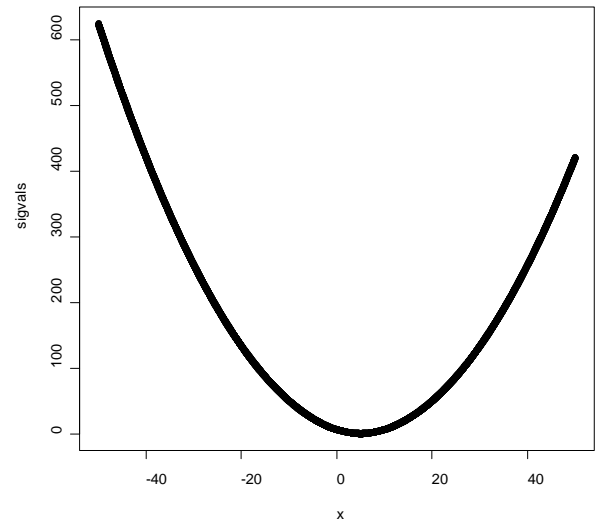
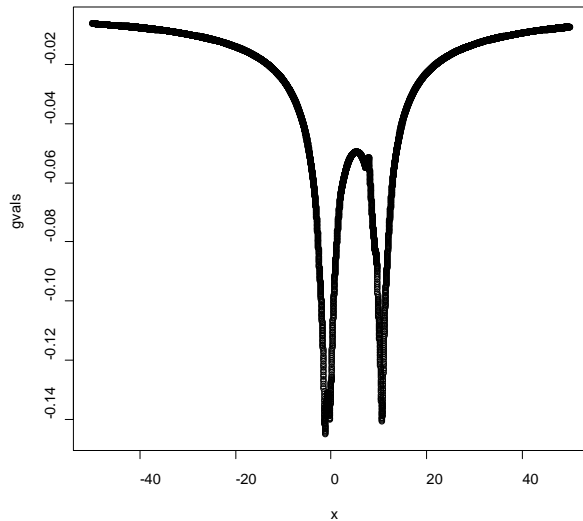
[1] 13.18471

[1] 0.06168104

[1] 7.440597

2.2.2 kernel function $K(x) = \frac{1}{1 + \alpha_1 |x|^{\alpha_2}}$

2.2.2.1 case 90 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 24720 out of 100000 (24.720%).

final beta = -1.607328

alpha(5.000000) is 0.988139

alpha(7.000000) is 0.589771

alpha(10.000000) is 0.200291

alpha(20.000000) is 0.196613

alpha(30.000000) is 0.137781

alpha(50.000000) is 0.081525

alpha(70.000000) is 0.057500

alpha(120.000000) is 0.032600

alpha(150.000000) is 0.024600

it takes 184.334000 seconds to run the adaptation algorithm

it takes 81.864000 seconds to compute g and sigma

it takes 21.676000 seconds to generate the first Markov Chain

it takes 20.450000 seconds to generate the second Markov Chain

it takes 20.362000 seconds to generate the third Markov Chain

it takes 20.683000 seconds to generate the fourth Markov Chain

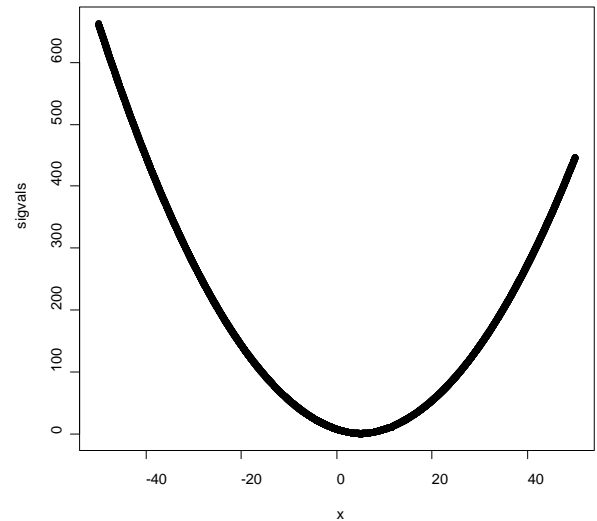
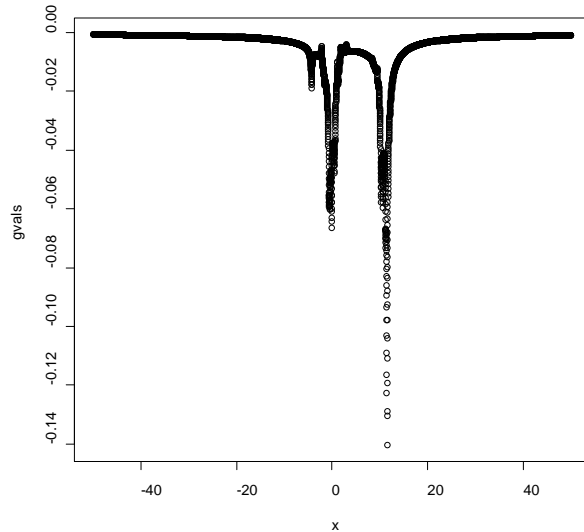
it takes 20.657000 seconds to generate the fifth Markov Chain

it takes 1592.689000 seconds to test the local acceptance

1

[1] 19.49482
[1] 0.07497625
[1] 5.323529

2.2.2.2 case 91 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 23284 out of 100000 (23.284%).

final beta = -1.553623

alpha(5.000000) is 0.988174

alpha(7.000000) is 0.596101

alpha(10.000000) is 0.194054

alpha(20.000000) is 0.188999

alpha(30.000000) is 0.127711

alpha(50.000000) is 0.076924

alpha(70.000000) is 0.056700

alpha(120.000000) is 0.034100

alpha(150.000000) is 0.024600

it takes 185.151000 seconds to run the adaptation algorithm

it takes 82.135000 seconds to compute g and sigma

it takes 21.671000 seconds to generate the first Markov Chain

it takes 21.784000 seconds to generate the second Markov Chain

it takes 21.923000 seconds to generate the third Markov Chain

it takes 22.090000 seconds to generate the fourth Markov Chain

it takes 22.497000 seconds to generate the fifth Markov Chain

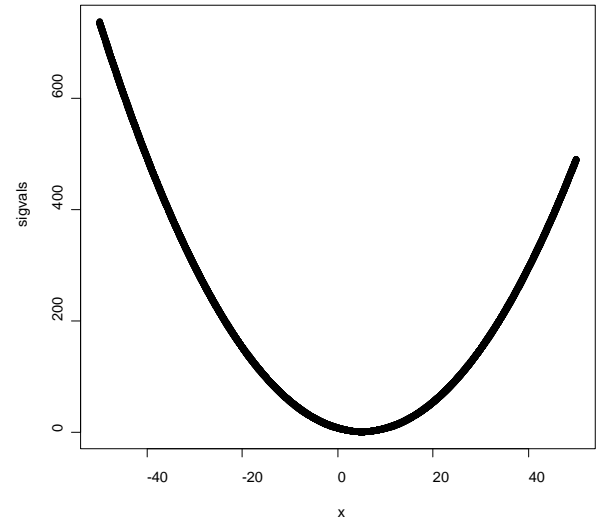
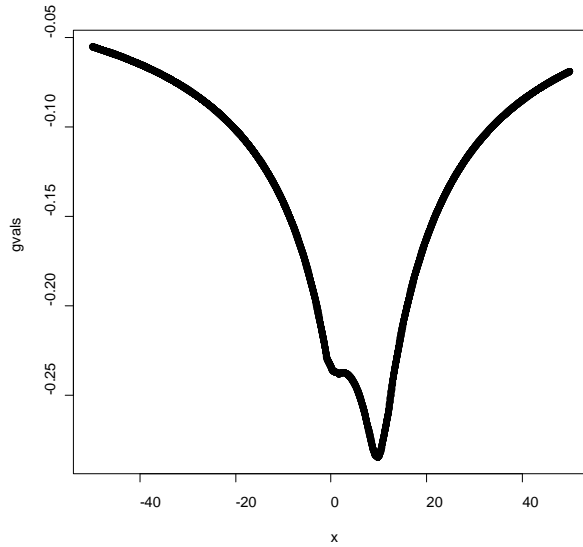
it takes 1604.363000 seconds to test the local acceptance

1

[1] 16.85428
[1] 0.06995134
[1] 6.095268

2.2.2.3 case 92 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth

$b_n = 1$



Accepted 23990 out of 100000 (23.990%).

final beta = -1.392714

alpha(5.000000) is 0.988405

alpha(7.000000) is 0.593630

alpha(10.000000) is 0.195274

alpha(20.000000) is 0.185996

alpha(30.000000) is 0.121447

alpha(50.000000) is 0.068600

alpha(70.000000) is 0.049300

alpha(120.000000) is 0.028100

alpha(150.000000) is 0.022400

it takes 179.813000 seconds to run the adaptation algorithm

it takes 80.313000 seconds to compute g and sigma

it takes 21.353000 seconds to generate the first Markov Chain

it takes 21.448000 seconds to generate the second Markov Chain

it takes 21.540000 seconds to generate the third Markov Chain

it takes 21.411000 seconds to generate the fourth Markov Chain

it takes 21.412000 seconds to generate the fifth Markov Chain

it takes 1617.949000 seconds to test the local acceptance

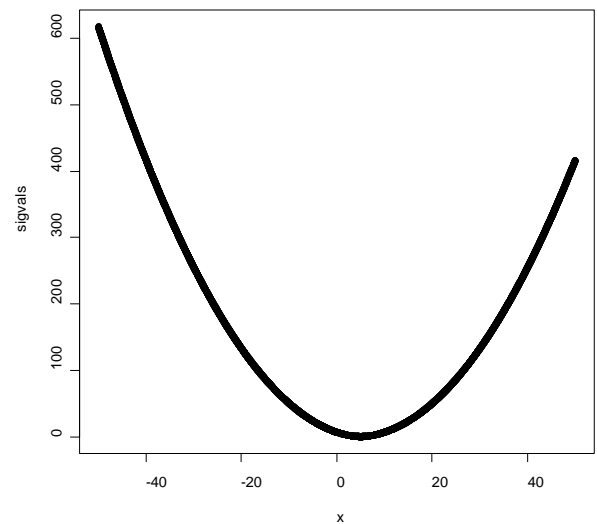
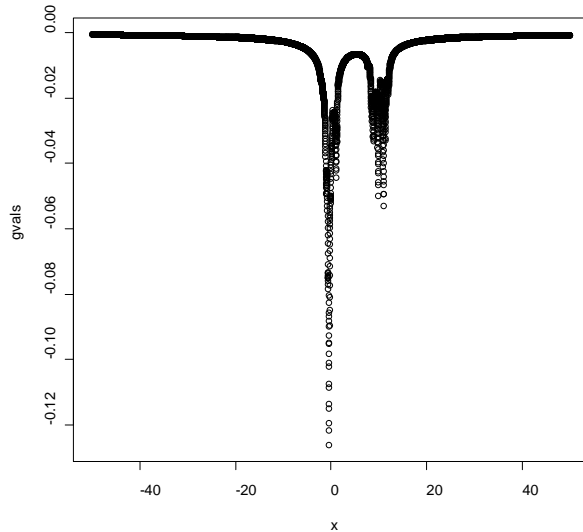
1

[1] 18.48608

[1] 0.07306009

[1] 5.840868

2.2.2.4 case 93 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 12, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 24077 out of 100000 (24.077%).

final beta = -1.624033

alpha(5.000000) is 0.988294

alpha(7.000000) is 0.593646

alpha(10.000000) is 0.198721

alpha(20.000000) is 0.199731

alpha(30.000000) is 0.138526

alpha(50.000000) is 0.078896

alpha(70.000000) is 0.059563

alpha(120.000000) is 0.033700

alpha(150.000000) is 0.027705

it takes 184.236000 seconds to run the adaptation algorithm

it takes 80.468000 seconds to compute g and sigma

it takes 21.800000 seconds to generate the first Markov Chain

it takes 21.435000 seconds to generate the second Markov Chain

it takes 22.060000 seconds to generate the third Markov Chain

it takes 22.133000 seconds to generate the fourth Markov Chain

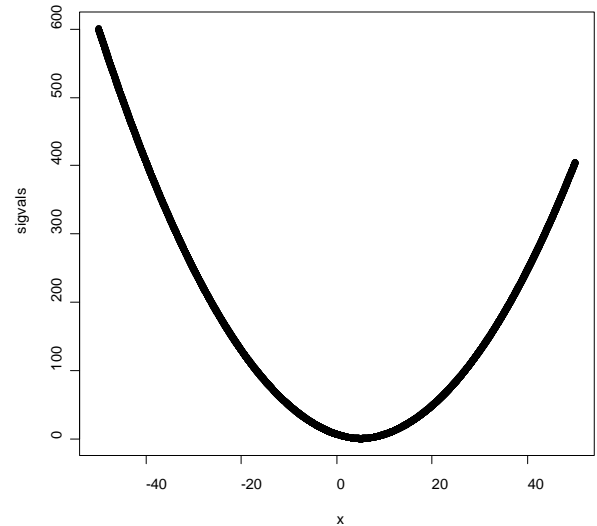
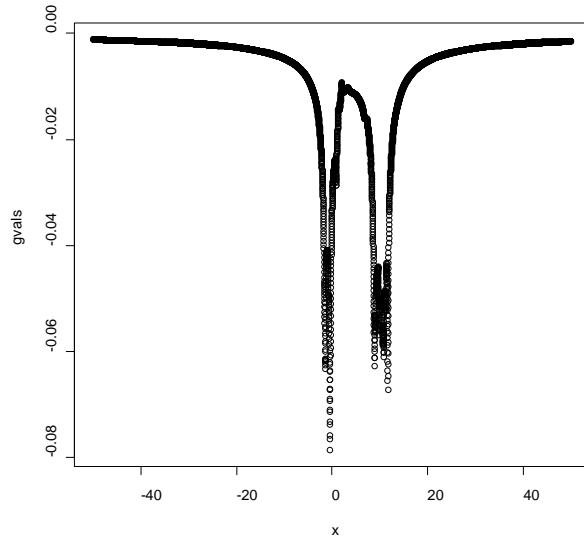
it takes 21.635000 seconds to generate the fifth Markov Chain

it takes 1601.408000 seconds to test the local acceptance

1

[1] 19.10133
[1] 0.07426885
[1] 5.761007

2.2.2.5 case 94 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 5, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 24465 out of 100000 (24.465%).

final beta = -1.651342

alpha(5.000000) is 0.988520

alpha(7.000000) is 0.585530

alpha(10.000000) is 0.197157

alpha(20.000000) is 0.200606

alpha(30.000000) is 0.136503

alpha(50.000000) is 0.085026

alpha(70.000000) is 0.054800

alpha(120.000000) is 0.034400

alpha(150.000000) is 0.026400

it takes 182.533000 seconds to run the adaptation algorithm

it takes 79.414000 seconds to compute g and sigma

it takes 20.642000 seconds to generate the first Markov Chain

it takes 20.342000 seconds to generate the second Markov Chain

it takes 20.352000 seconds to generate the third Markov Chain

it takes 20.449000 seconds to generate the fourth Markov Chain

it takes 20.339000 seconds to generate the fifth Markov Chain

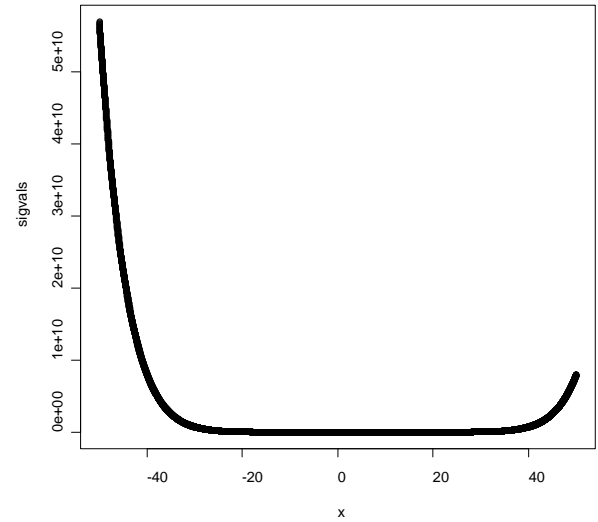
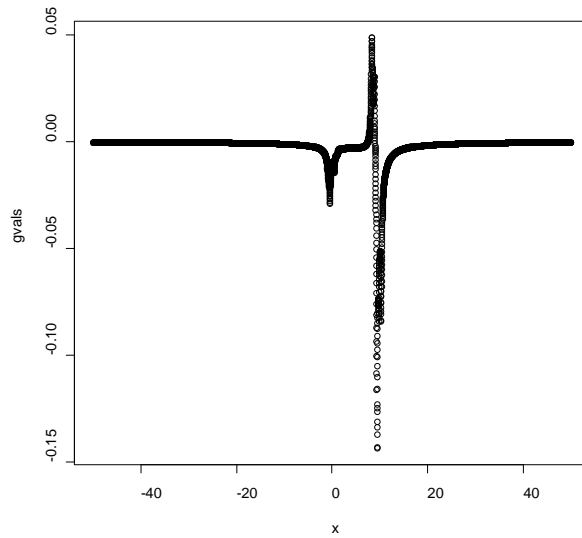
it takes 1575.653000 seconds to test the local acceptance

1

[1] 19.09234
[1] 0.07416466
[1] 5.474942

2.2.2.6 case 95 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 1, \gamma = 10$ with fixed bandwidth

$b_n = 1$



Accepted 18062 out of 100000 (18.062%).

final beta = -15.487329

alpha(5.000000) is 0.975604

alpha(7.000000) is 0.970986

alpha(10.000000) is 0.099708

alpha(20.000000) is 0.000000

alpha(30.000000) is 0.000000

alpha(50.000000) is 0.000000

alpha(70.000000) is 0.000000

alpha(120.000000) is 0.000000

alpha(150.000000) is 0.000000

it takes 184.158000 seconds to run the adaptation algorithm

it takes 80.077000 seconds to compute g and sigma

it takes 129.847000 seconds to generate the first Markov Chain

it takes 106.905000 seconds to generate the second Markov Chain

it takes 114.789000 seconds to generate the third Markov Chain

it takes 111.836000 seconds to generate the fourth Markov Chain

it takes 122.212000 seconds to generate the fifth Markov Chain

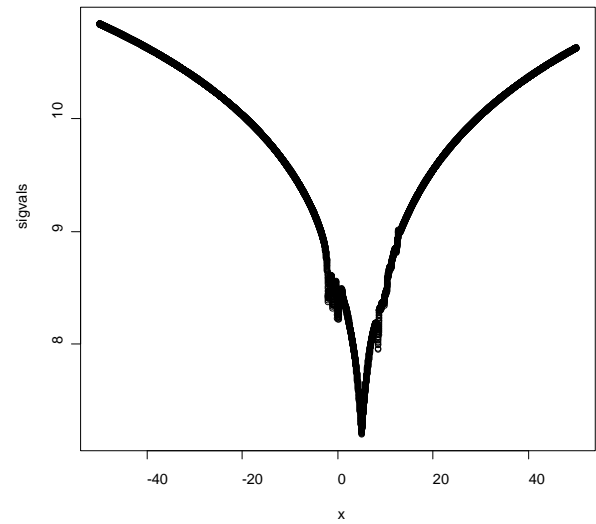
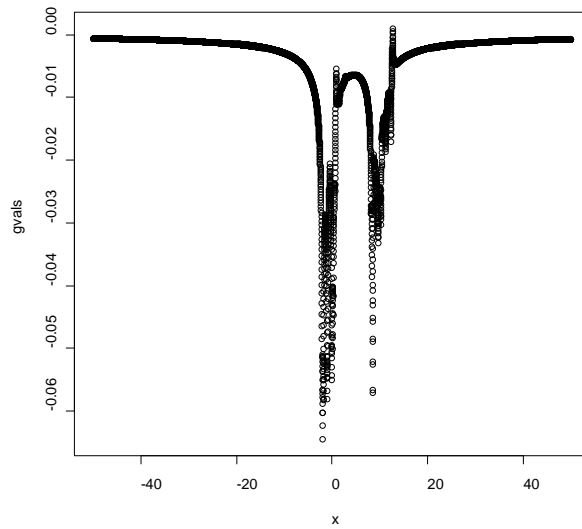
it takes 1797.306000 seconds to test the local acceptance

1

[1] 53.60444
[1] 0.1244969
[1] 1.709541

2.2.2.7 case 96 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 1, \gamma = 0.1$ with fixed bandwidth

$b_n = 1$



Accepted 22236 out of 100000 (22.236%).

final beta = 1.981254

alpha(5.000000) is 0.837339

alpha(7.000000) is 0.525632

alpha(10.000000) is 0.178894

alpha(20.000000) is 0.504550

alpha(30.000000) is 0.500767

alpha(50.000000) is 0.498991

alpha(70.000000) is 0.497244

alpha(120.000000) is 0.500871

alpha(150.000000) is 0.500862

it takes 180.159000 seconds to run the adaptation algorithm

it takes 80.338000 seconds to compute g and sigma

it takes 20.996000 seconds to generate the first Markov Chain

it takes 20.246000 seconds to generate the second Markov Chain

it takes 20.903000 seconds to generate the third Markov Chain

it takes 20.337000 seconds to generate the fourth Markov Chain

it takes 20.582000 seconds to generate the fifth Markov Chain

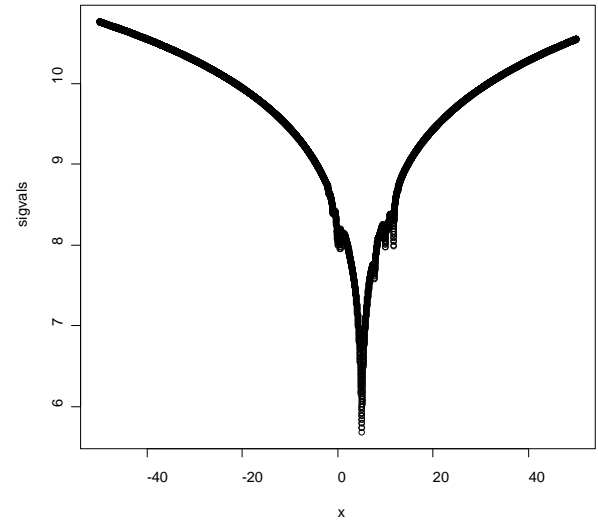
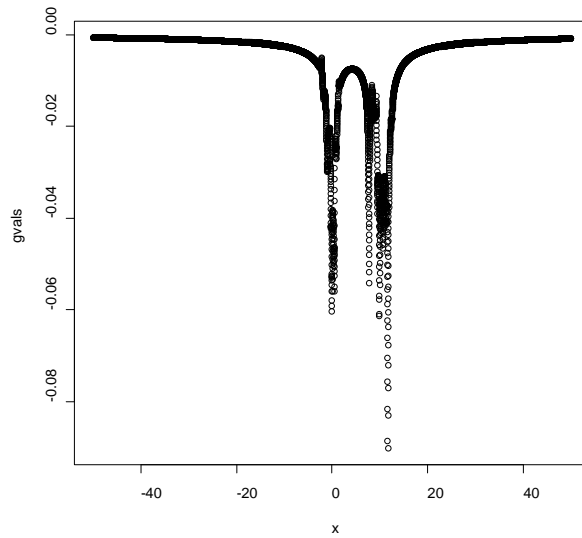
it takes 1096.667000 seconds to test the local acceptance

1

[1] 12.47803
[1] 0.05992151
[1] 7.639173

2.2.2.8 case 97 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 10$ with fixed bandwidth

$b_n = 1$



Accepted 22723 out of 100000 (22.723%).

final beta = 2.082104

alpha(5.000000) is 0.000000

alpha(7.000000) is 0.000000

alpha(10.000000) is 0.000000

alpha(20.000000) is 0.000000

alpha(30.000000) is 0.000000

alpha(50.000000) is 0.018600

alpha(70.000000) is 0.129300

alpha(120.000000) is 0.286300

alpha(150.000000) is 0.341000

it takes 193.949000 seconds to run the adaptation algorithm

it takes 85.107000 seconds to compute g and sigma

it takes 22.242000 seconds to generate the first Markov Chain

it takes 22.288000 seconds to generate the second Markov Chain

it takes 22.125000 seconds to generate the third Markov Chain

it takes 22.425000 seconds to generate the fourth Markov Chain

it takes 22.492000 seconds to generate the fifth Markov Chain

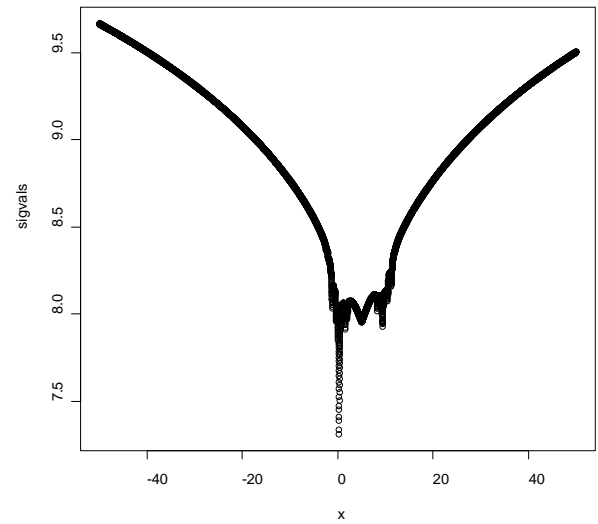
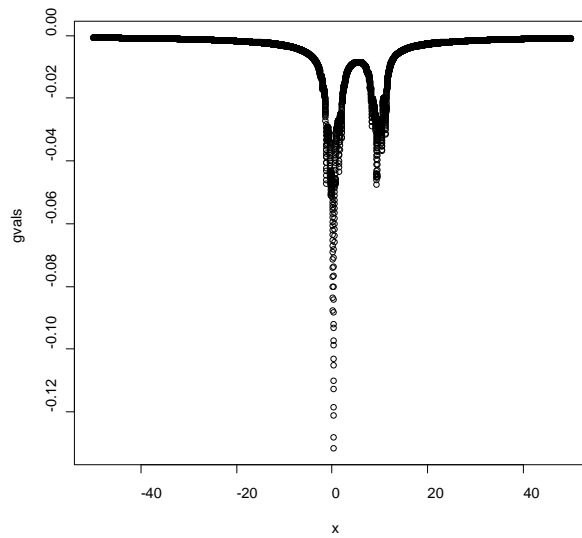
it takes 814.063000 seconds to test the local acceptance

1

[1] 12.94998
[1] 0.06111524
[1] 7.64341

2.2.2.9 case 98 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$b_n = 10$



Accepted 24628 out of 100000 (24.628%).

final beta = 1.935983

alpha(5.000000) is 0.856700

alpha(7.000000) is 0.567400

alpha(10.000000) is 0.195400

alpha(20.000000) is 0.497600

alpha(30.000000) is 0.502600

alpha(50.000000) is 0.495200

alpha(70.000000) is 0.510000

alpha(120.000000) is 0.498000

alpha(150.000000) is 0.506600

it takes 180.883000 seconds to run the adaptation algorithm

it takes 79.484000 seconds to compute g and sigma

it takes 20.451000 seconds to generate the first Markov Chain

it takes 20.749000 seconds to generate the second Markov Chain

it takes 20.666000 seconds to generate the third Markov Chain

it takes 20.354000 seconds to generate the fourth Markov Chain

it takes 20.373000 seconds to generate the fifth Markov Chain

it takes 771.898000 seconds to test the local acceptance

1

```
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M] ) );asjd(xlist[(B+1):M]);
```

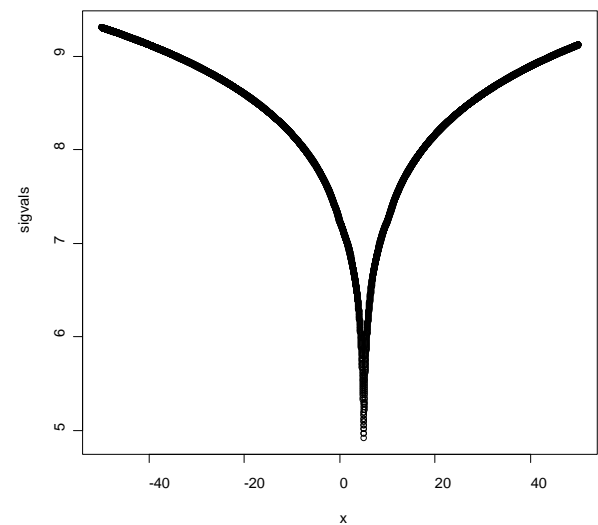
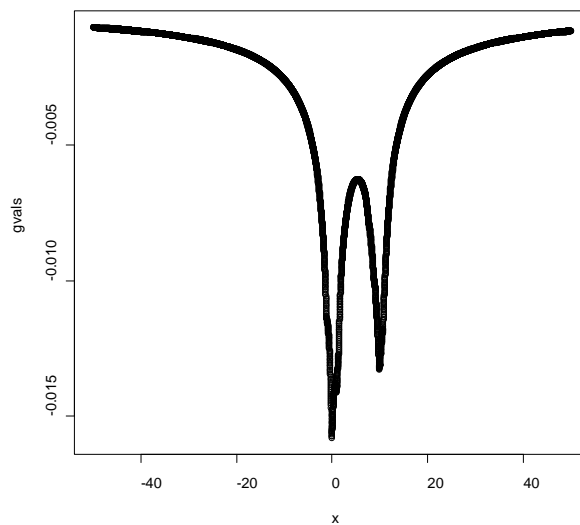
```
[1] 13.93196
```

```
[1] 0.06357011
```

```
[1] 7.406249
```

2.2.2.10 case 99 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$b_n = 0.1$



Accepted 24127 out of 100000 (24.127%).

final beta = 1.600481

alpha(5.000000) is 0.959075

alpha(7.000000) is 0.577982

alpha(10.000000) is 0.189727

alpha(20.000000) is 0.504383

alpha(30.000000) is 0.501884

alpha(50.000000) is 0.493078

alpha(70.000000) is 0.497578

alpha(120.000000) is 0.491683

alpha(150.000000) is 0.498875

it takes 189.887000 seconds to run the adaptation algorithm

it takes 82.323000 seconds to compute g and sigma

it takes 20.289000 seconds to generate the first Markov Chain

it takes 21.285000 seconds to generate the second Markov Chain

it takes 20.836000 seconds to generate the third Markov Chain

it takes 21.327000 seconds to generate the fourth Markov Chain

it takes 20.622000 seconds to generate the fifth Markov Chain

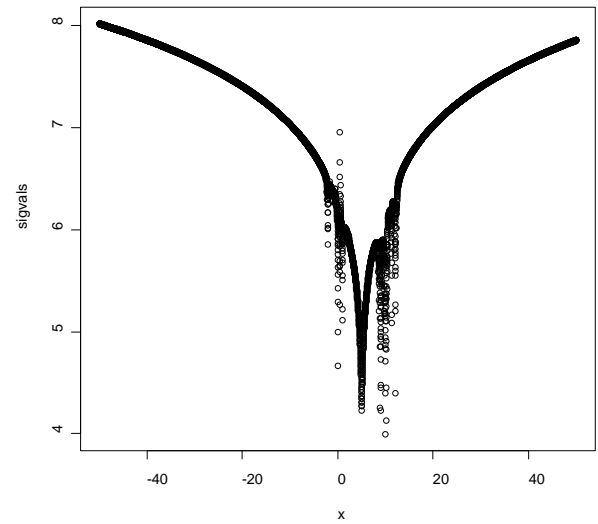
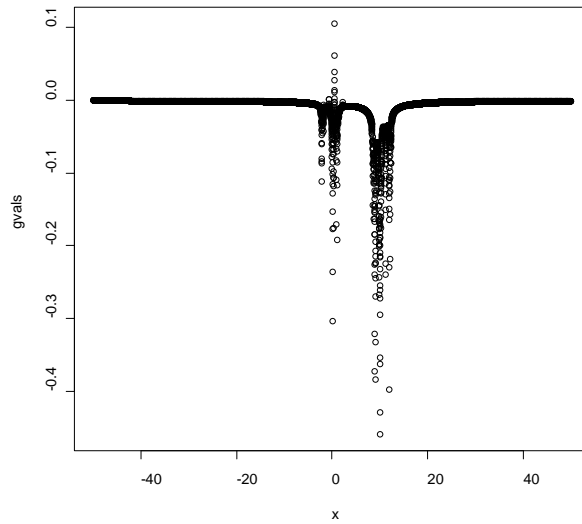
it takes 1120.381000 seconds to test the local acceptance

1

[1] 14.33295
[1] 0.06422718
[1] 7.005803

2.2.2.11 case 100 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 0.1$ with fixed bandwidth

$b_n = 10$



Accepted 25905 out of 100000 (25.905%).

final beta = 1.450997

alpha(5.000000) is 0.982768

alpha(7.000000) is 0.614188

alpha(10.000000) is 0.204066

alpha(20.000000) is 0.511236

alpha(30.000000) is 0.501774

alpha(50.000000) is 0.494540

alpha(70.000000) is 0.499826

alpha(120.000000) is 0.498532

alpha(150.000000) is 0.499842

it takes 185.462000 seconds to run the adaptation algorithm

it takes 81.620000 seconds to compute g and sigma

it takes 20.542000 seconds to generate the first Markov Chain

it takes 21.623000 seconds to generate the second Markov Chain

it takes 20.950000 seconds to generate the third Markov Chain

it takes 21.644000 seconds to generate the fourth Markov Chain

it takes 21.796000 seconds to generate the fifth Markov Chain

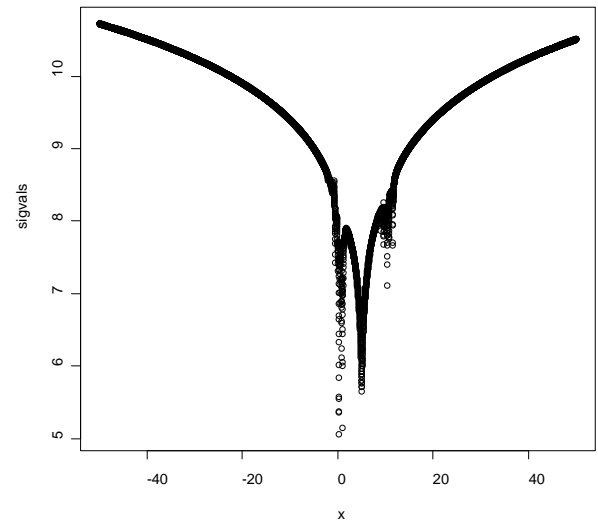
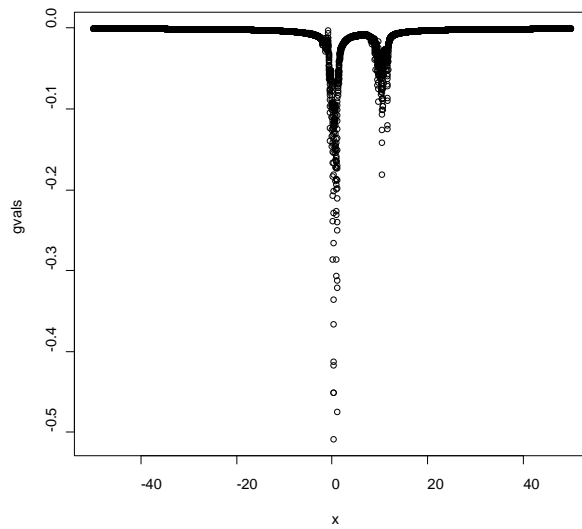
it takes 1133.939000 seconds to test the local acceptance

1

[1] 18.55894
 [1] 0.07316876
 [1] 5.515589

2.2.2.12 case 101 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 2$ with decreasing bandwidth

$$b_n = \frac{1}{n^{0.2}}$$



Accepted 23002 out of 100000 (23.002%).

final beta = 1.742155

alpha(5.000000) is 0.925394

alpha(7.000000) is 0.534543

alpha(10.000000) is 0.179065

alpha(20.000000) is 0.500864

alpha(30.000000) is 0.495748

alpha(50.000000) is 0.495755

alpha(70.000000) is 0.497514

alpha(120.000000) is 0.498657

alpha(150.000000) is 0.500898

it takes 186.083000 seconds to run the adaptation algorithm

it takes 82.053000 seconds to compute g and sigma

it takes 22.213000 seconds to generate the first Markov Chain

it takes 21.654000 seconds to generate the second Markov Chain

it takes 22.906000 seconds to generate the third Markov Chain

it takes 23.243000 seconds to generate the fourth Markov Chain

it takes 23.168000 seconds to generate the fifth Markov Chain

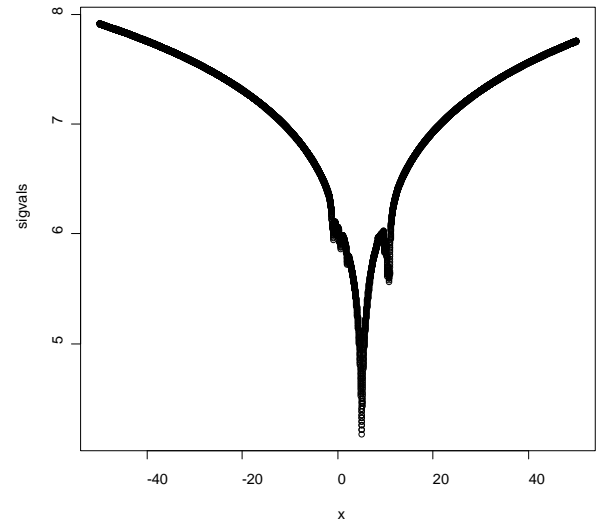
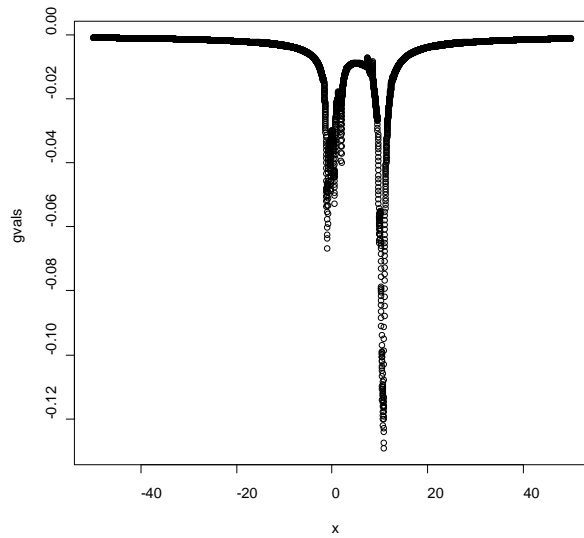
it takes 1133.776000 seconds to test the local acceptance

1

[1] 14.00296
[1] 0.06365483
[1] 7.400967

2.2.2.13 case 102 $\eta_n = \frac{1}{(n+5)^{0.8}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth

$b_n = 10$



Accepted 23672 out of 100000 (23.672%).

final beta = 1.658811

alpha(5.000000) is 0.945195

alpha(7.000000) is 0.568038

alpha(10.000000) is 0.189494

alpha(20.000000) is 0.501942

alpha(30.000000) is 0.496667

alpha(50.000000) is 0.496623

alpha(70.000000) is 0.501563

alpha(120.000000) is 0.490541

alpha(150.000000) is 0.492890

it takes 181.352000 seconds to run the adaptation algorithm

it takes 78.941000 seconds to compute g and sigma

it takes 20.257000 seconds to generate the first Markov Chain

it takes 20.210000 seconds to generate the second Markov Chain

it takes 20.094000 seconds to generate the third Markov Chain

it takes 20.147000 seconds to generate the fourth Markov Chain

it takes 20.194000 seconds to generate the fifth Markov Chain

it takes 1087.941000 seconds to test the local acceptance

1

[1] 18.03951

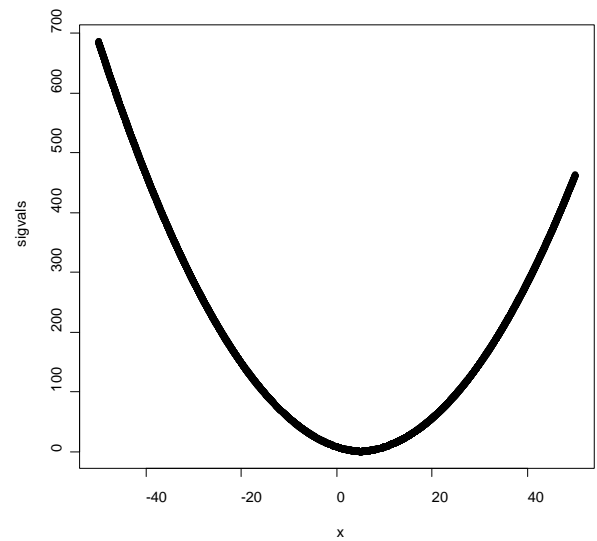
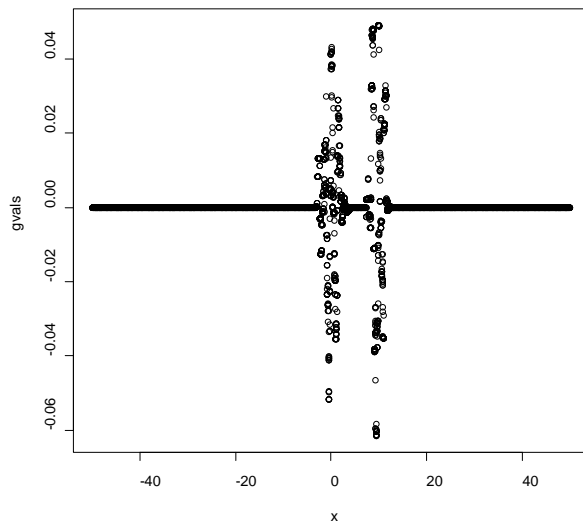
[1] 0.07210694

[1] 5.518752

2.2.3 kernel function
$$K(x) = \begin{cases} 0, & |x| \geq 2 * width \\ -1 * height, & width < |x| < 2 * width \\ 1 * height, & |x| \leq width \end{cases}$$

2.2.3.1 case 103 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 1, \gamma = 2, height = 0.5, width = 0.5$, with fixed

bandwidth $b_n = 1$



Accepted 23171 out of 100000 (23.171%).

final beta = -1.519856

alpha(5.000000) is 0.988000

alpha(7.000000) is 0.603800

alpha(10.000000) is 0.185000

alpha(20.000000) is 0.182000

alpha(30.000000) is 0.125600

alpha(50.000000) is 0.072000

alpha(70.000000) is 0.051400

alpha(120.000000) is 0.029100

alpha(150.000000) is 0.023900

it takes 125.983000 seconds to run the adaptation algorithm

it takes 33.358000 seconds to compute g and sigma

it takes 18.496000 seconds to generate the first Markov Chain

it takes 18.395000 seconds to generate the second Markov Chain

it takes 19.412000 seconds to generate the third Markov Chain

it takes 18.896000 seconds to generate the fourth Markov Chain

it takes 19.008000 seconds to generate the fifth Markov Chain

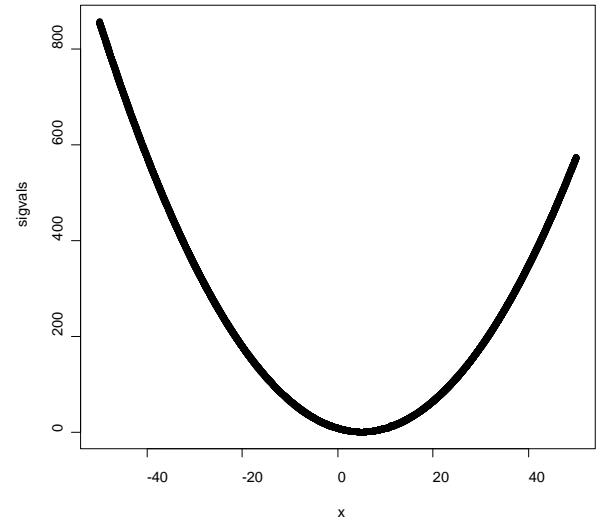
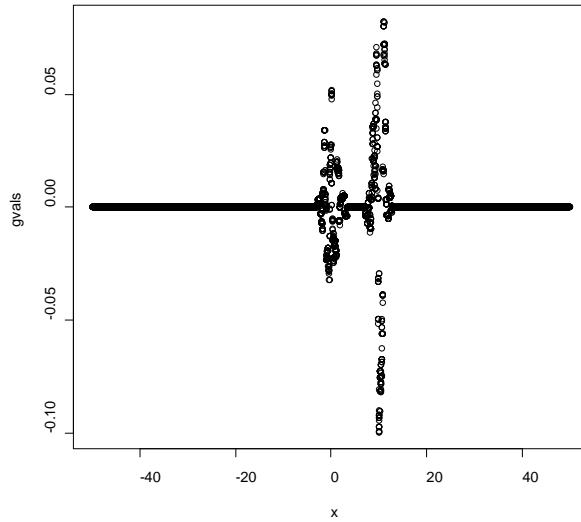
it takes 721.432000 seconds to test the local acceptance

1

[1] 15.87749
[1] 0.06777017
[1] 6.794295

2.2.3.2 case 104 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 10, \gamma = 2$, height = 0.5, width = 0.5, with fixed

bandwidth $b_n = 1$



Accepted 23433 out of 100000 (23.433%).

final beta = -5.869167

alpha(5.000000) is 0.956600

alpha(7.000000) is 0.610600

alpha(10.000000) is 0.193700

alpha(20.000000) is 0.154200

alpha(30.000000) is 0.101700

alpha(50.000000) is 0.061300

alpha(70.000000) is 0.043000

alpha(120.000000) is 0.023500

alpha(150.000000) is 0.018200

it takes 126.170000 seconds to run the adaptation algorithm

it takes 33.355000 seconds to compute g and sigma

it takes 18.941000 seconds to generate the first Markov Chain

it takes 19.131000 seconds to generate the second Markov Chain

it takes 18.991000 seconds to generate the third Markov Chain

it takes 18.368000 seconds to generate the fourth Markov Chain

it takes 18.620000 seconds to generate the fifth Markov Chain

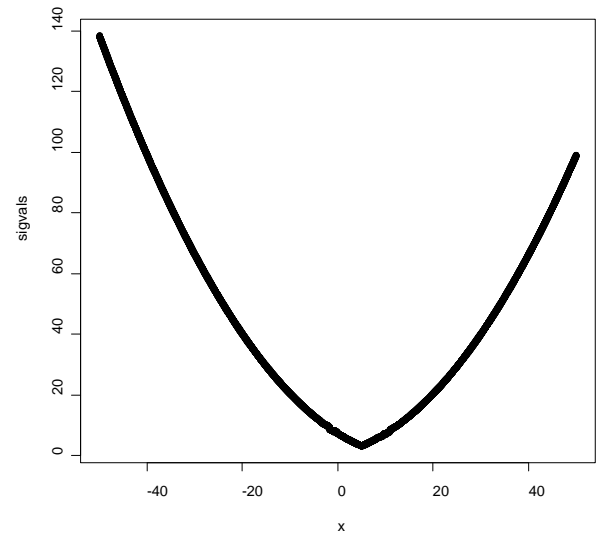
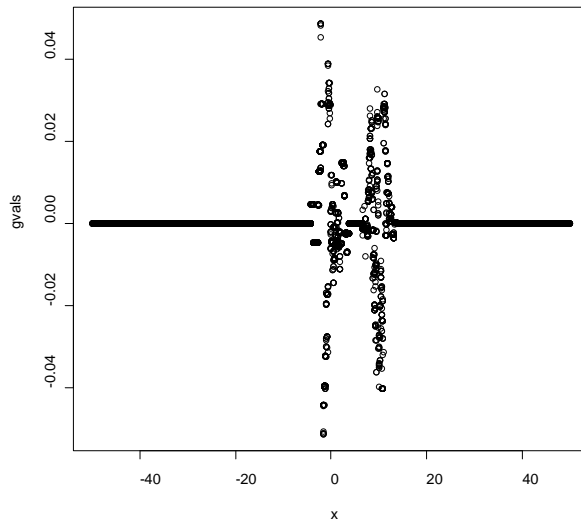
it takes 728.738000 seconds to test the local acceptance

1

[1] 18.30191
[1] 0.07264643
[1] 5.623555

2.2.3.3 case 105 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 2$, height = 0.5, width = 0.5, with fixed

bandwidth $b_n = 1$



Accepted 24212 out of 100000 (24.212%).

final beta = 1.185992

alpha(5.000000) is 0.998500

alpha(7.000000) is 0.641800

alpha(10.000000) is 0.193100

alpha(20.000000) is 0.437000

alpha(30.000000) is 0.398400

alpha(50.000000) is 0.316700

alpha(70.000000) is 0.265200

alpha(120.000000) is 0.171600

alpha(150.000000) is 0.146700

it takes 124.856000 seconds to run the adaptation algorithm

it takes 33.247000 seconds to compute g and sigma

it takes 14.799000 seconds to generate the first Markov Chain

it takes 15.013000 seconds to generate the second Markov Chain

it takes 14.871000 seconds to generate the third Markov Chain

it takes 15.018000 seconds to generate the fourth Markov Chain

it takes 14.761000 seconds to generate the fifth Markov Chain

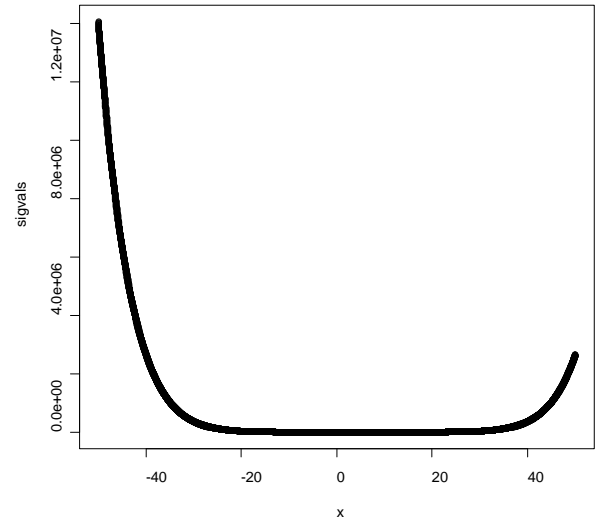
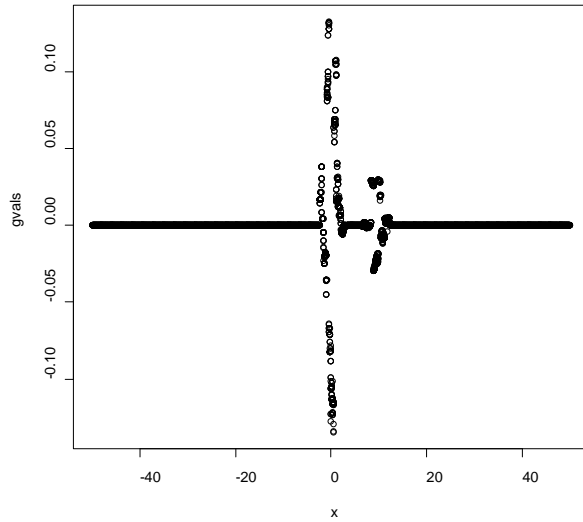
it takes 681.928000 seconds to test the local acceptance

1

[1] 13.42696
 [1] 0.06233687
 [1] 7.217294

2.2.3.4 case 106 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 10, \text{height} = 0.5, \text{width} = 0.5$, with fixed

bandwidth $b_n = 1$



Accepted 23920 out of 100000 (23.920%).

final beta = -2.260178

alpha(5.000000) is 0.998600

alpha(7.000000) is 0.675300

alpha(10.000000) is 0.198500

alpha(20.000000) is 0.011200

alpha(30.000000) is 0.000700

alpha(50.000000) is 0.000000

alpha(70.000000) is 0.000000

alpha(120.000000) is 0.000000

alpha(150.000000) is 0.000000

it takes 126.420000 seconds to run the adaptation algorithm

it takes 33.691000 seconds to compute g and sigma

it takes 26.633000 seconds to generate the first Markov Chain

it takes 26.667000 seconds to generate the second Markov Chain

it takes 25.153000 seconds to generate the third Markov Chain

it takes 24.161000 seconds to generate the fourth Markov Chain

it takes 23.908000 seconds to generate the fifth Markov Chain

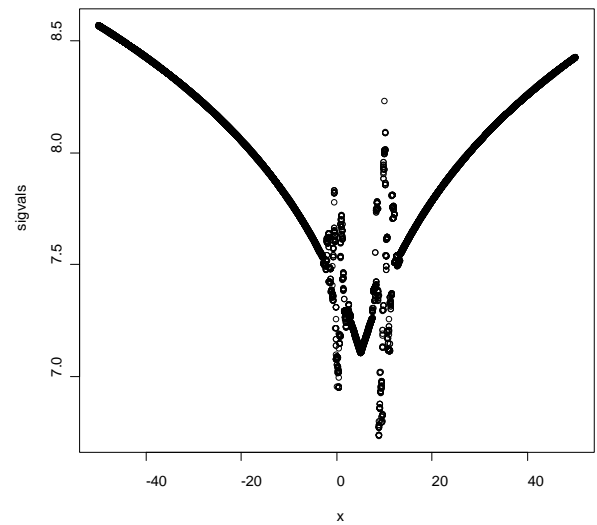
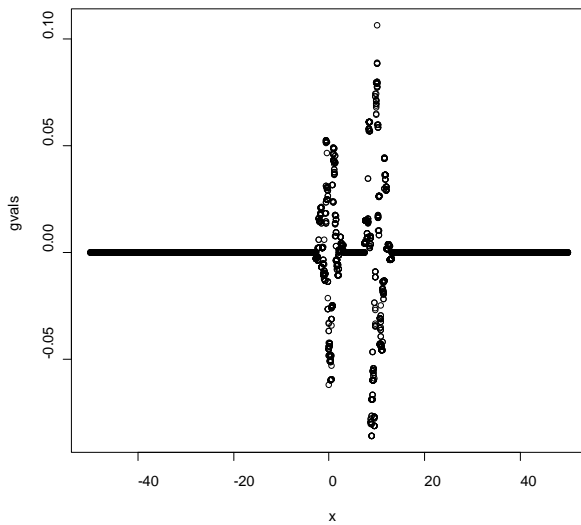
it takes 763.257000 seconds to test the local acceptance

1

[1] 36.67233
 [1] 0.1030286
 [1] 3.271804

2.2.3.5 case 107 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{height} = 0.5, \text{width} = 0.5$, with fixed

bandwidth $b_n = 1$



Accepted 24069 out of 100000 (24.069%).

final beta = 1.960744

alpha(5.000000) is 0.845900

alpha(7.000000) is 0.563800

alpha(10.000000) is 0.187600

alpha(20.000000) is 0.502400

alpha(30.000000) is 0.498400

alpha(50.000000) is 0.490100

alpha(70.000000) is 0.501200

alpha(120.000000) is 0.499200

alpha(150.000000) is 0.495100

it takes 126.576000 seconds to run the adaptation algorithm

it takes 33.654000 seconds to compute g and sigma

it takes 14.539000 seconds to generate the first Markov Chain

it takes 14.438000 seconds to generate the second Markov Chain

it takes 14.539000 seconds to generate the third Markov Chain

it takes 14.475000 seconds to generate the fourth Markov Chain

it takes 14.386000 seconds to generate the fifth Markov Chain

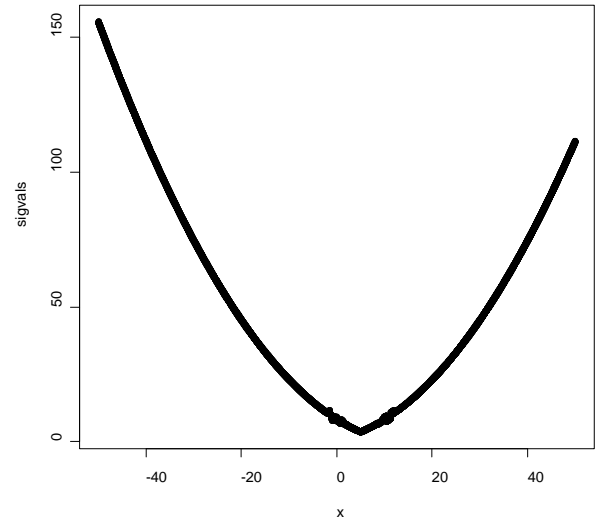
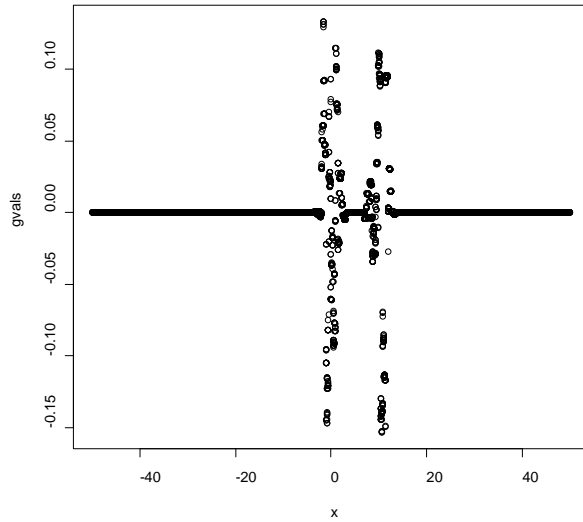
it takes 688.012000 seconds to test the local acceptance

1

[1] 13.54641
[1] 0.06246479
[1] 7.10335

2.2.3.6 case 108 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 2, \text{height} = 1, \text{width} = 0.5$, with fixed

bandwidth $b_n = 1$



Accepted 22858 out of 100000 (22.858%).

final beta = 1.305092

alpha(5.000000) is 0.994700

alpha(7.000000) is 0.623500

alpha(10.000000) is 0.175000

alpha(20.000000) is 0.406200

alpha(30.000000) is 0.354900

alpha(50.000000) is 0.291400

alpha(70.000000) is 0.231900

alpha(120.000000) is 0.156500

alpha(150.000000) is 0.128000

it takes 128.046000 seconds to run the adaptation algorithm

it takes 34.032000 seconds to compute g and sigma

it takes 17.171000 seconds to generate the first Markov Chain

it takes 16.964000 seconds to generate the second Markov Chain

it takes 16.993000 seconds to generate the third Markov Chain

it takes 17.088000 seconds to generate the fourth Markov Chain

it takes 17.015000 seconds to generate the fifth Markov Chain

it takes 696.429000 seconds to test the local acceptance

1

```
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
```

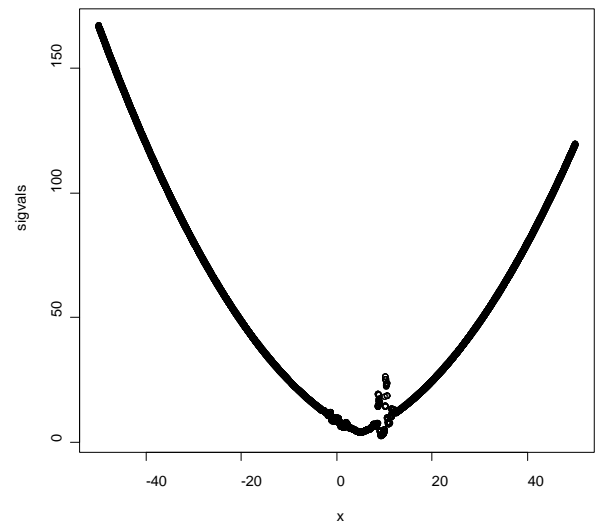
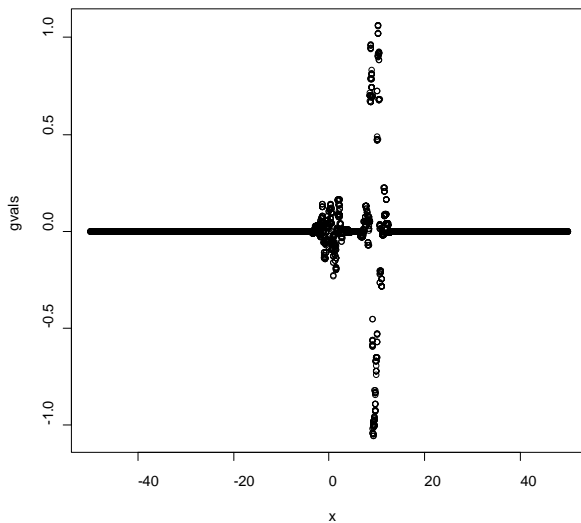
```
[1] 13.20776
```

```
[1] 0.06187482
```

```
[1] 7.630405
```

2.2.3.7 case 109 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 2, \text{height} = 5, \text{width} = 0.5$, with fixed

bandwidth $b_n = 1$



Accepted 19990 out of 100000 (19.990%).

final beta = 1.374566

alpha(5.000000) is 0.990800

alpha(7.000000) is 0.611700

alpha(10.000000) is 0.175300

alpha(20.000000) is 0.396700

alpha(30.000000) is 0.356900

alpha(50.000000) is 0.280000

alpha(70.000000) is 0.224500

alpha(120.000000) is 0.146700

alpha(150.000000) is 0.114400

it takes 126.505000 seconds to run the adaptation algorithm

it takes 33.891000 seconds to compute g and sigma

it takes 28.960000 seconds to generate the first Markov Chain

it takes 30.148000 seconds to generate the second Markov Chain

it takes 29.466000 seconds to generate the third Markov Chain

it takes 30.076000 seconds to generate the fourth Markov Chain

it takes 29.000000 seconds to generate the fifth Markov Chain

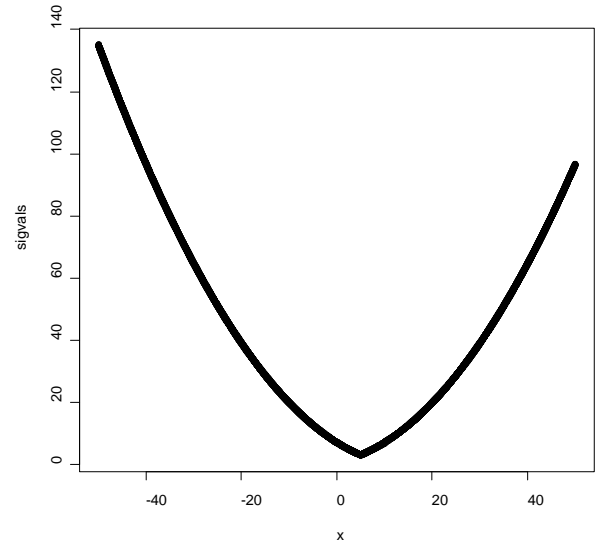
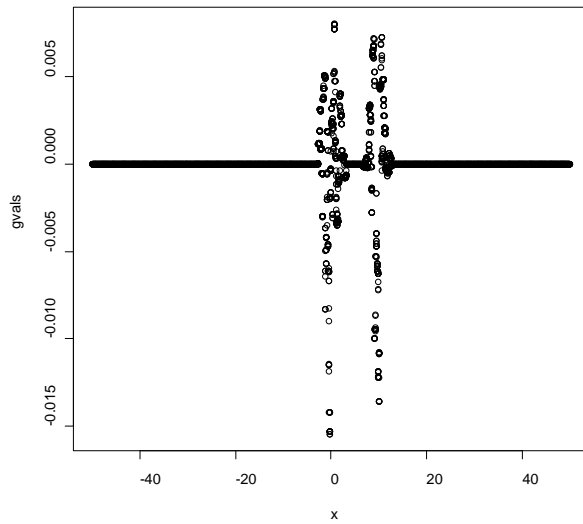
it takes 698.858000 seconds to test the local acceptance

1

[1] 19.00901
[1] 0.07394524
[1] 6.026763

2.2.3.8 case 110 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 2$, height = 0.1, width = 0.5, with fixed

bandwidth $b_n = 1$



Accepted 24162 out of 100000 (24.162%).

final beta = 1.162301

alpha(5.000000) is 0.999400

alpha(7.000000) is 0.644200

alpha(10.000000) is 0.195200

alpha(20.000000) is 0.443100

alpha(30.000000) is 0.397500

alpha(50.000000) is 0.326200

alpha(70.000000) is 0.264600

alpha(120.000000) is 0.169000

alpha(150.000000) is 0.150200

it takes 128.729000 seconds to run the adaptation algorithm

it takes 34.300000 seconds to compute g and sigma

it takes 14.885000 seconds to generate the first Markov Chain

it takes 15.071000 seconds to generate the second Markov Chain

it takes 15.083000 seconds to generate the third Markov Chain

it takes 15.030000 seconds to generate the fourth Markov Chain

it takes 15.525000 seconds to generate the fifth Markov Chain

it takes 687.539000 seconds to test the local acceptance

1

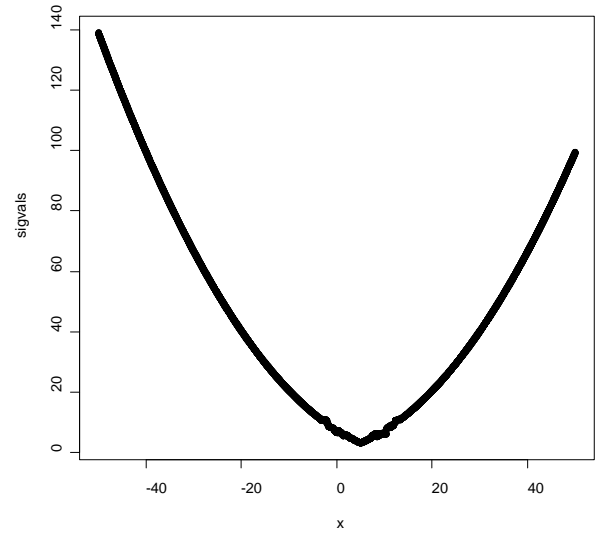
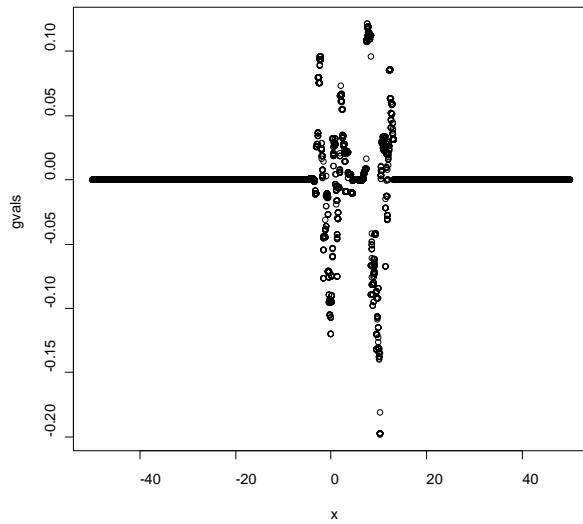
[1] 14.73459

[1] 0.0653481

[1] 6.995348

2.2.3.9 case 111 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 1, \gamma = 0.1, \text{height} = 1, \text{width} = 1$, with fixed

bandwidth $b_n = 1$



Accepted 24070 out of 100000 (24.070%).

final beta = 1.190445

alpha(5.000000) is 0.998200

alpha(7.000000) is 0.637100

alpha(10.000000) is 0.194100

alpha(20.000000) is 0.431700

alpha(30.000000) is 0.396000

alpha(50.000000) is 0.313700

alpha(70.000000) is 0.260200

alpha(120.000000) is 0.172400

alpha(150.000000) is 0.146100

it takes 130.494000 seconds to run the adaptation algorithm

it takes 34.635000 seconds to compute g and sigma

it takes 15.504000 seconds to generate the first Markov Chain

it takes 15.325000 seconds to generate the second Markov Chain

it takes 15.827000 seconds to generate the third Markov Chain

it takes 15.820000 seconds to generate the fourth Markov Chain

it takes 15.180000 seconds to generate the fifth Markov Chain

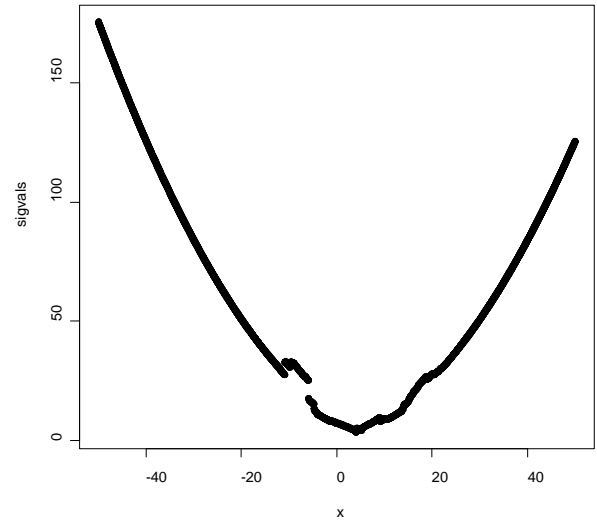
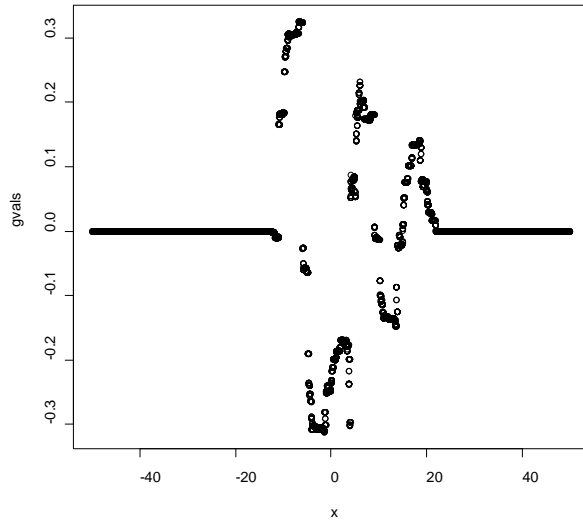
it takes 673.514000 seconds to test the local acceptance

1

[1] 14.21126
[1] 0.0639442
[1] 7.098321

2.2.3.10 case 112 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{height} = 1, \text{width} = 5$, with fixed

bandwidth $b_n = 1$



Accepted 22764 out of 100000 (22.764%).

final beta = 1.423704

alpha(5.000000) is 0.979500

alpha(7.000000) is 0.562100

alpha(10.000000) is 0.171100

alpha(20.000000) is 0.362800

alpha(30.000000) is 0.331700

alpha(50.000000) is 0.256200

alpha(70.000000) is 0.207300

alpha(120.000000) is 0.138500

alpha(150.000000) is 0.112700

it takes 124.856000 seconds to run the adaptation algorithm

it takes 33.271000 seconds to compute g and sigma

it takes 17.093000 seconds to generate the first Markov Chain

it takes 16.845000 seconds to generate the second Markov Chain

it takes 16.925000 seconds to generate the third Markov Chain

it takes 17.035000 seconds to generate the fourth Markov Chain

it takes 16.817000 seconds to generate the fifth Markov Chain

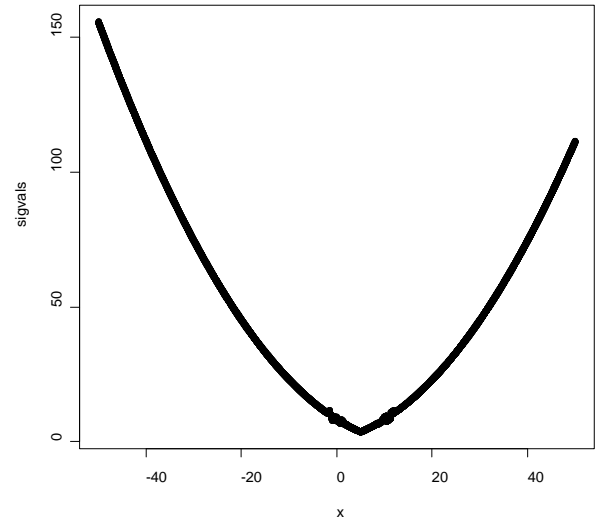
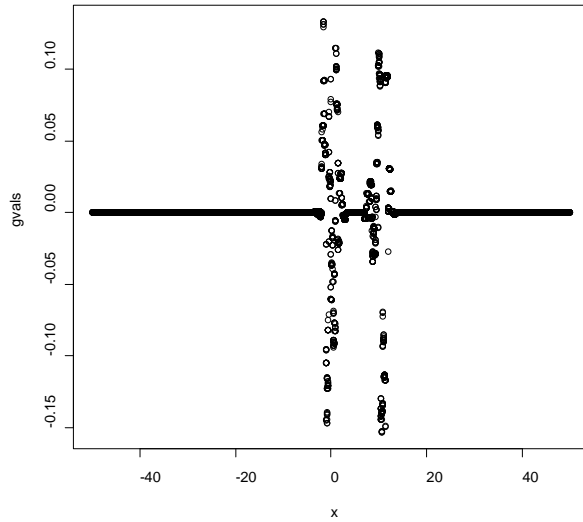
it takes 682.008000 seconds to test the local acceptance

1

[1] 13.13645
[1] 0.06167256
[1] 7.480724

2.2.3.11 case 113 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{height} = 1, \text{width} = 0.1$, with fixed

bandwidth $b_n = 1$



Accepted 22512 out of 100000 (22.512%).

final beta = 1.354120

alpha(5.000000) is 0.992200

alpha(7.000000) is 0.613300

alpha(10.000000) is 0.175600

alpha(20.000000) is 0.391400

alpha(30.000000) is 0.355300

alpha(50.000000) is 0.277000

alpha(70.000000) is 0.221500

alpha(120.000000) is 0.153500

alpha(150.000000) is 0.121700

it takes 124.137000 seconds to run the adaptation algorithm

it takes 33.218000 seconds to compute g and sigma

it takes 96.215000 seconds to generate the first Markov Chain

it takes 17.237000 seconds to generate the second Markov Chain

it takes 16.931000 seconds to generate the third Markov Chain

it takes 17.485000 seconds to generate the fourth Markov Chain

it takes 17.579000 seconds to generate the fifth Markov Chain

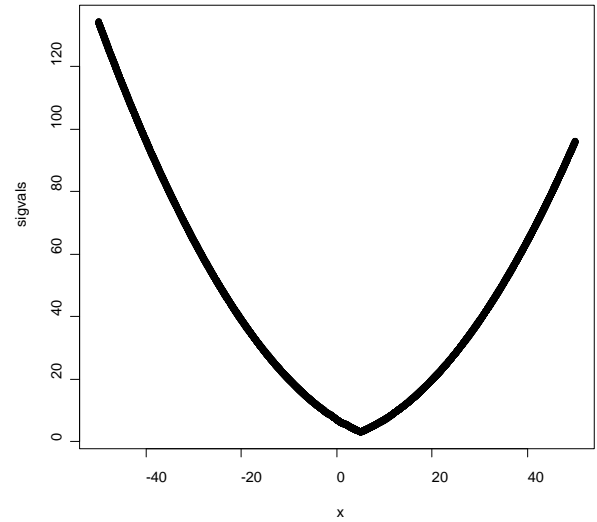
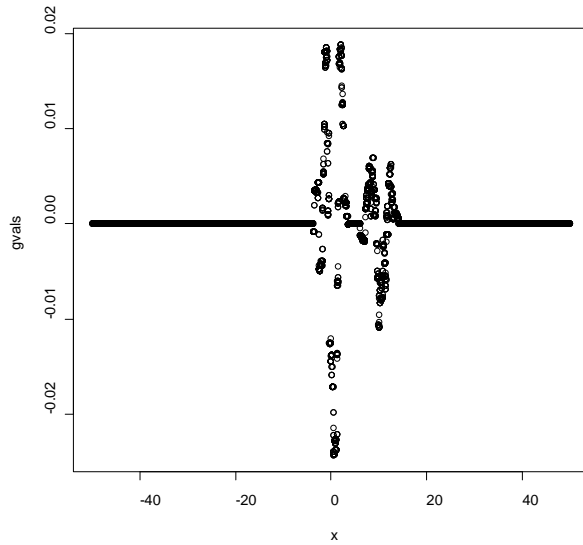
it takes 675.932000 seconds to test the local acceptance

1

[1] 12.13842
[1] 0.05919573
[1] 7.954234

2.2.3.12 case 114 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{height} = 1, \text{width} = 0.1$, with fixed

bandwidth $b_n = 10$



Accepted 24426 out of 100000 (24.426%).

final beta = 1.156102

alpha(5.000000) is 0.999300

alpha(7.000000) is 0.649700

alpha(10.000000) is 0.199600

alpha(20.000000) is 0.443400

alpha(30.000000) is 0.398200

alpha(50.000000) is 0.324700

alpha(70.000000) is 0.264000

alpha(120.000000) is 0.177500

alpha(150.000000) is 0.150800

it takes 129.592000 seconds to run the adaptation algorithm

it takes 34.583000 seconds to compute g and sigma

it takes 15.233000 seconds to generate the first Markov Chain

it takes 15.353000 seconds to generate the second Markov Chain

it takes 15.480000 seconds to generate the third Markov Chain

it takes 15.380000 seconds to generate the fourth Markov Chain

it takes 15.365000 seconds to generate the fifth Markov Chain

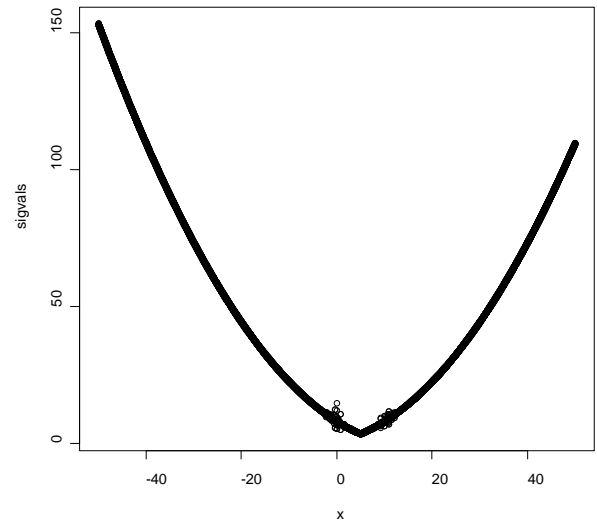
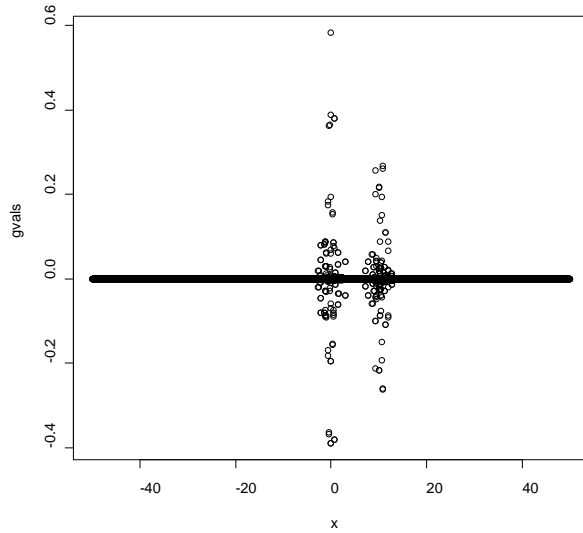
it takes 710.588000 seconds to test the local acceptance

1

[1] 13.40427
[1] 0.06225008
[1] 6.997632

2.2.3.13 case 115 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{height} = 1, \text{width} = 0.1$, with fixed

bandwidth $b_n = 0.1$



Accepted 22790 out of 100000 (22.790%).

final beta = 1.287911

alpha(5.000000) is 0.996700

alpha(7.000000) is 0.633100

alpha(10.000000) is 0.183000

alpha(20.000000) is 0.406000

alpha(30.000000) is 0.363800

alpha(50.000000) is 0.288600

alpha(70.000000) is 0.233700

alpha(120.000000) is 0.157000

alpha(150.000000) is 0.137300

it takes 131.432000 seconds to run the adaptation algorithm

it takes 35.259000 seconds to compute g and sigma

it takes 17.457000 seconds to generate the first Markov Chain

it takes 17.422000 seconds to generate the second Markov Chain

it takes 17.078000 seconds to generate the third Markov Chain

it takes 17.222000 seconds to generate the fourth Markov Chain

it takes 17.383000 seconds to generate the fifth Markov Chain

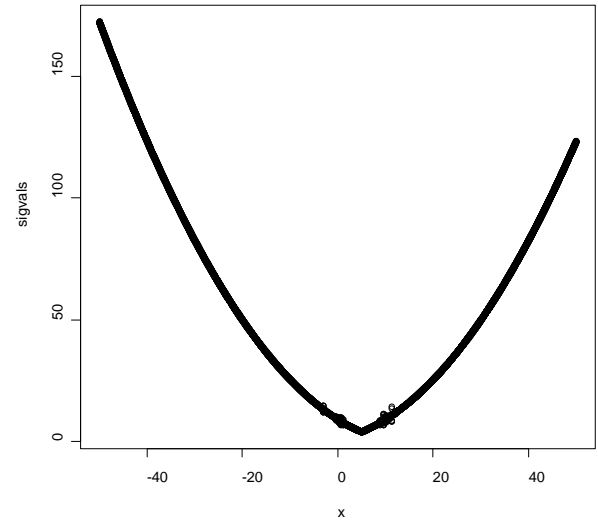
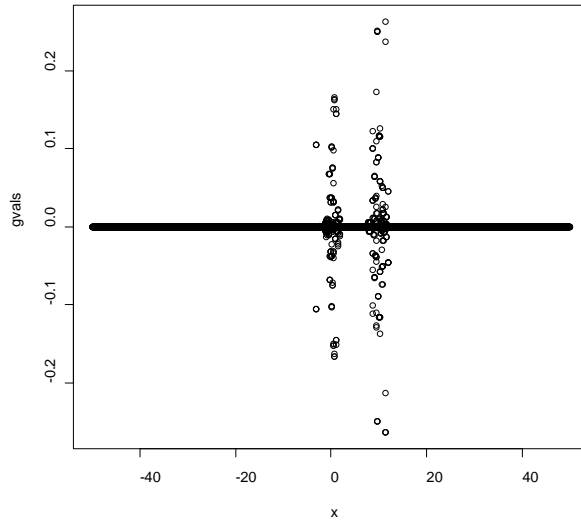
it takes 695.595000 seconds to test the local acceptance

1

[1] 11.9384
[1] 0.05869727
[1] 7.548351

2.2.3.14 case 116 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{height} = 1, \text{width} = 0.1$, with

decreasing bandwidth $b_n = \frac{1}{n^{0.2}}$



Accepted 21764 out of 100000 (21.764%).

final beta = 1.405223

alpha(5.000000) is 0.990500

alpha(7.000000) is 0.604200

alpha(10.000000) is 0.169900

alpha(20.000000) is 0.384300

alpha(30.000000) is 0.342200

alpha(50.000000) is 0.272700

alpha(70.000000) is 0.209200

alpha(120.000000) is 0.138600

alpha(150.000000) is 0.113700

it takes 127.433000 seconds to run the adaptation algorithm

it takes 34.299000 seconds to compute g and sigma

it takes 19.226000 seconds to generate the first Markov Chain

it takes 19.014000 seconds to generate the second Markov Chain

it takes 19.349000 seconds to generate the third Markov Chain

it takes 20.065000 seconds to generate the fourth Markov Chain

it takes 21.261000 seconds to generate the fifth Markov Chain

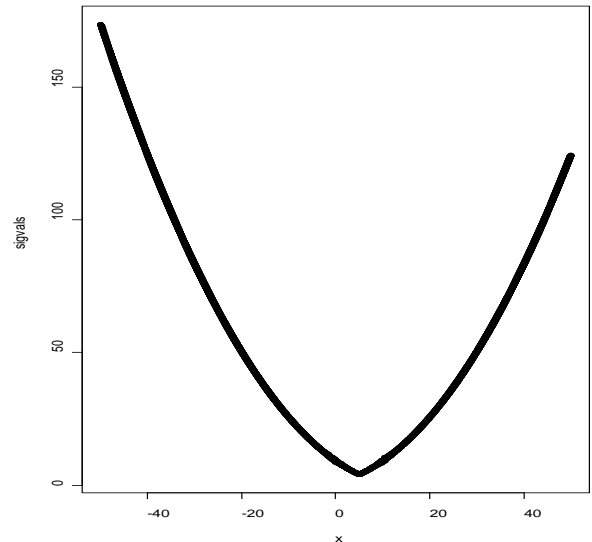
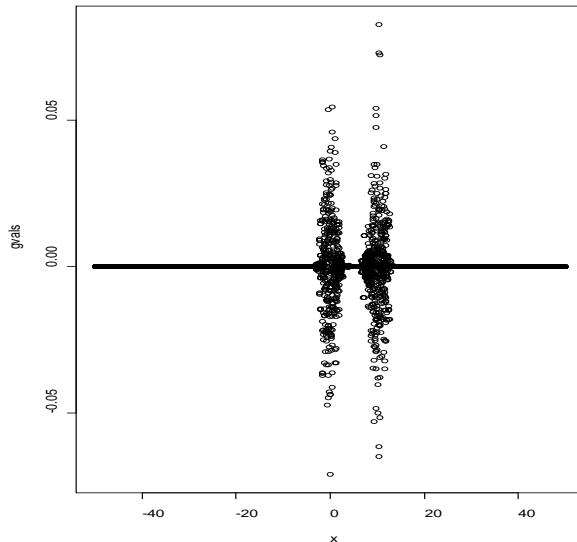
it takes 716.572000 seconds to test the local acceptance

1

[1] 11.16328
[1] 0.05691963
[1] 8.158163

2.2.3.15 case 117 $\eta_n = \frac{1}{(n+5)^{0.8}}$, $C = 0.1, \gamma = 0.1, \text{height} = 1, \text{width} = 0.1$, with

decreasing bandwidth $b_n = \frac{1}{n^{0.2}}$



Accepted 21518 out of 100000 (21.518%).

final beta = 1.413473

alpha(5.000000) is 0.988200

alpha(7.000000) is 0.611800

alpha(10.000000) is 0.168800

alpha(20.000000) is 0.380700

alpha(30.000000) is 0.341300

alpha(50.000000) is 0.269300

alpha(70.000000) is 0.220400

alpha(120.000000) is 0.138000

alpha(150.000000) is 0.110700

it takes 129.851000 seconds to run the adaptation algorithm

it takes 34.370000 seconds to compute g and sigma

it takes 19.528000 seconds to generate the first Markov Chain

it takes 20.341000 seconds to generate the second Markov Chain

it takes 19.515000 seconds to generate the third Markov Chain

it takes 19.079000 seconds to generate the fourth Markov Chain

it takes 19.145000 seconds to generate the fifth Markov Chain

it takes 713.662000 seconds to test the local acceptance

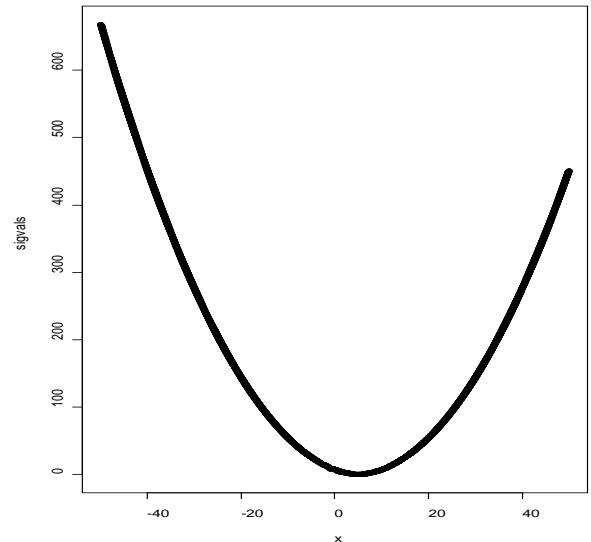
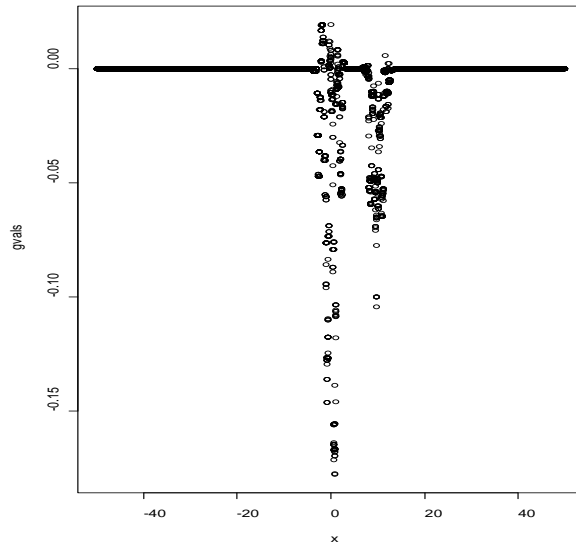
1

[1] 12.90081
[1] 0.0611555
[1] 7.84211

2.2.4 kernel function $K(x) = \begin{cases} 0, & |x| \geq 2 * width \text{ or } |x| \leq width \\ 1, & width < |x| < 2 * width \end{cases}$

2.2.4.1 case 119 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 1, \gamma = 0.5, width = 0.5$, with fixed bandwidth

$b_n = 1$



Accepted 23479 out of 100000 (23.479%).

final beta = -1.546046

alpha(5.000000) is 0.979400

alpha(7.000000) is 0.598700

alpha(10.000000) is 0.189100

alpha(20.000000) is 0.184800

alpha(30.000000) is 0.132600

alpha(50.000000) is 0.076700

alpha(70.000000) is 0.051700

alpha(120.000000) is 0.029300

alpha(150.000000) is 0.027400

it takes 309.700000 seconds to run the adaptation algorithm

it takes 84.090000 seconds to compute g and sigma

it takes 126.250000 seconds to generate the first Markov Chain

it takes 127.470000 seconds to generate the second Markov Chain

it takes 127.730000 seconds to generate the third Markov Chain

it takes 127.230000 seconds to generate the fourth Markov Chain

it takes 127.370000 seconds to generate the fifth Markov Chain

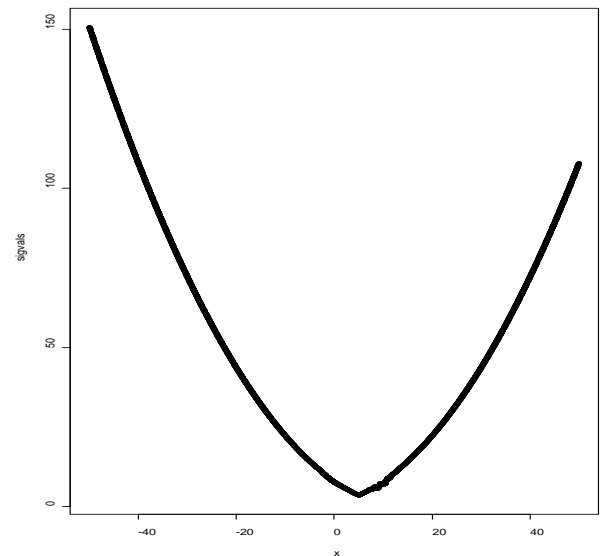
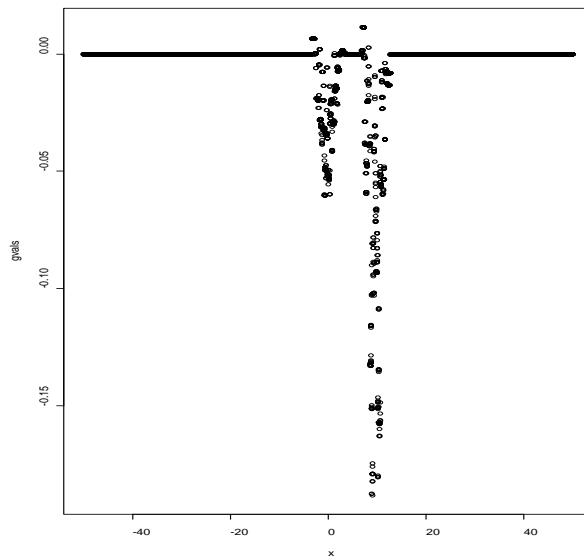
it takes 1860.250000 seconds to test the local acceptance

1

[1] 17.38122
[1] 0.07095952
[1] 6.096523

2.2.4.2 case 120 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 1, \gamma = 0.5$, width = 0.5, with fixed bandwidth

$b_n = 1$



Accepted 23535 out of 100000 (23.535%).

final beta = 1.271283

alpha(5.000000) is 0.995900

alpha(7.000000) is 0.619400

alpha(10.000000) is 0.199300

alpha(20.000000) is 0.416000

alpha(30.000000) is 0.376300

alpha(50.000000) is 0.289800

alpha(70.000000) is 0.240800

alpha(120.000000) is 0.164500

alpha(150.000000) is 0.133500

it takes 310.460000 seconds to run the adaptation algorithm

it takes 84.390000 seconds to compute g and sigma

it takes 121.920000 seconds to generate the first Markov Chain

it takes 121.700000 seconds to generate the second Markov Chain

it takes 122.100000 seconds to generate the third Markov Chain

it takes 121.570000 seconds to generate the fourth Markov Chain

it takes 121.940000 seconds to generate the fifth Markov Chain

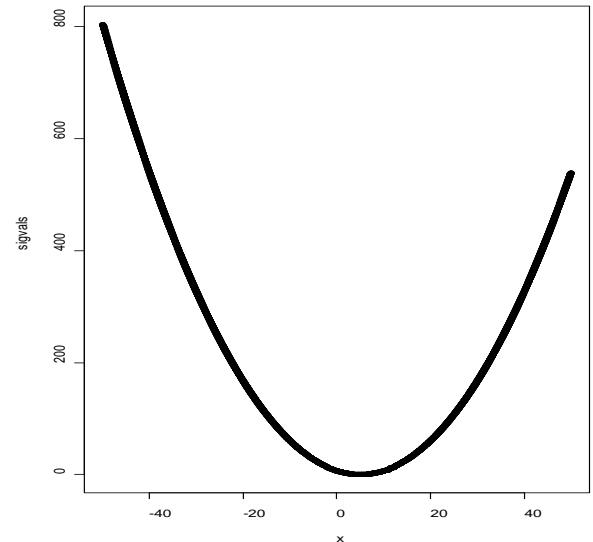
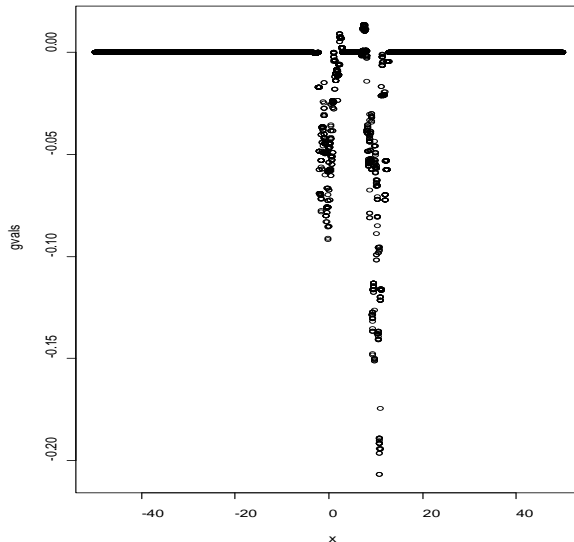
it takes 1754.020000 seconds to test the local acceptance

1

[1] 13.80102
[1] 0.0632373
[1] 7.232841

2.2.4.3 case 121 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 1, \gamma = 0.5$, width = 0.5, with fixed bandwidth

$b_n = 1$



Accepted 24444 out of 100000 (24.444%).

final beta = -5.933267

alpha(5.000000) is 0.951800

alpha(7.000000) is 0.614000

alpha(10.000000) is 0.207400

alpha(20.000000) is 0.164300

alpha(30.000000) is 0.113200

alpha(50.000000) is 0.067500

alpha(70.000000) is 0.043800

alpha(120.000000) is 0.027100

alpha(150.000000) is 0.020600

it takes 309.940000 seconds to run the adaptation algorithm

it takes 84.140000 seconds to compute g and sigma

it takes 125.430000 seconds to generate the first Markov Chain

it takes 124.300000 seconds to generate the second Markov Chain

it takes 125.330000 seconds to generate the third Markov Chain

it takes 124.340000 seconds to generate the fourth Markov Chain

it takes 123.770000 seconds to generate the fifth Markov Chain

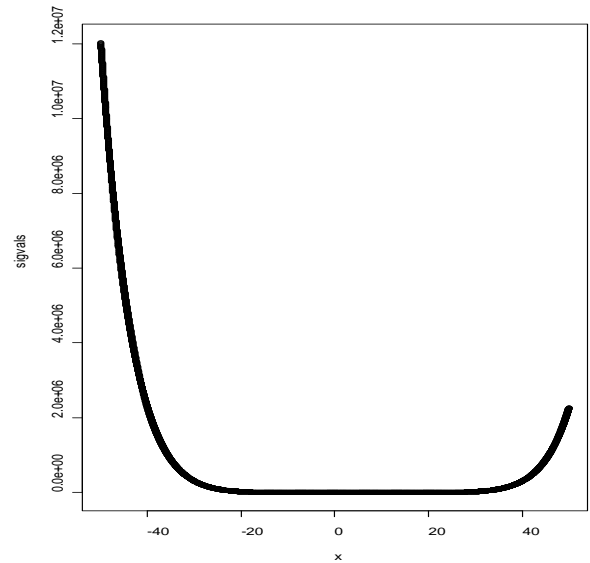
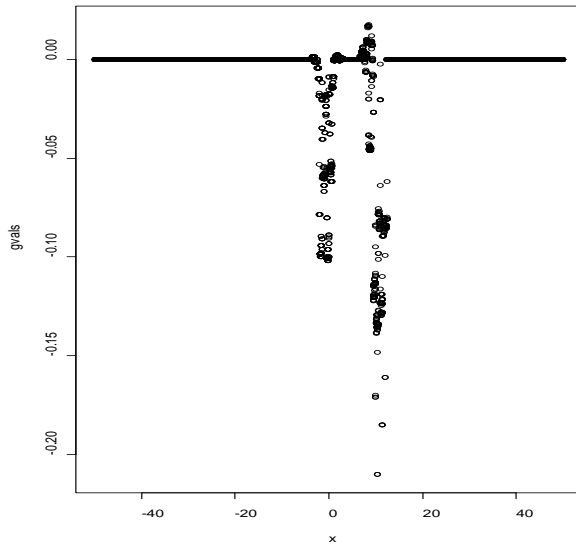
it takes 1865.350000 seconds to test the local acceptance

1

[1] 22.79518
 [1] 0.08128286
 [1] 4.885462

2.2.4.4 case 121 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 10$, width = 0.5, with fixed bandwidth

$b_n = 1$



Accepted 27356 out of 100000 (27.356%).

final beta = -2.414094

alpha(5.000000) is 0.992400

alpha(7.000000) is 0.689500

alpha(10.000000) is 0.218500

alpha(20.000000) is 0.011800

alpha(30.000000) is 0.000600

alpha(50.000000) is 0.000000

alpha(70.000000) is 0.000000

alpha(120.000000) is 0.000000

alpha(150.000000) is 0.000000

it takes 309.330000 seconds to run the adaptation algorithm

it takes 83.960000 seconds to compute g and sigma

it takes 127.880000 seconds to generate the first Markov Chain

it takes 131.110000 seconds to generate the second Markov Chain

it takes 129.140000 seconds to generate the third Markov Chain

it takes 129.650000 seconds to generate the fourth Markov Chain

it takes 129.490000 seconds to generate the fifth Markov Chain

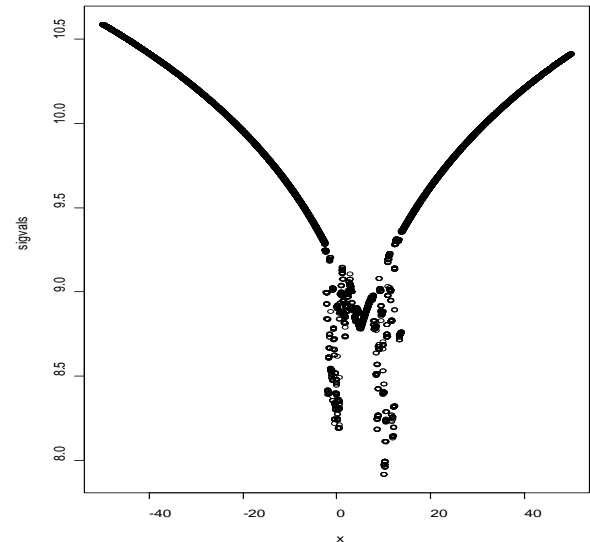
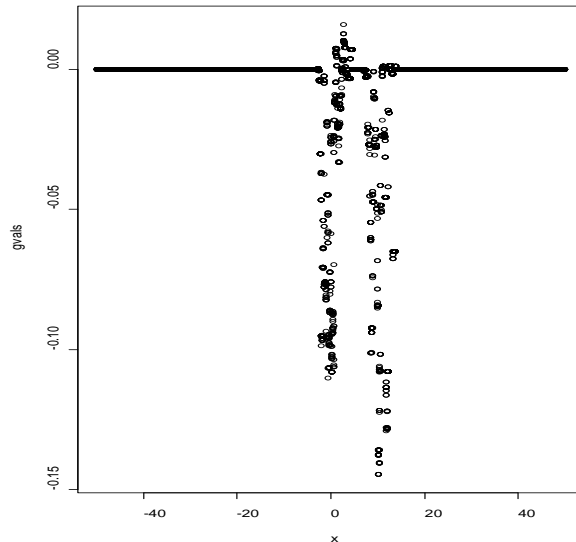
it takes 1955.590000 seconds to test the local acceptance

1

[1] 48.46781
[1] 0.1181587
[1] 2.552771

2.2.4.5 case 122 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{width} = 0.5$, with fixed bandwidth

$b_n = 1$



Accepted 21973 out of 100000 (21.973%).

final beta = 2.172493

alpha(5.000000) is 0.743600

alpha(7.000000) is 0.486600

alpha(10.000000) is 0.171900

alpha(20.000000) is 0.507400

alpha(30.000000) is 0.504300

alpha(50.000000) is 0.506300

alpha(70.000000) is 0.504300

alpha(120.000000) is 0.504100

alpha(150.000000) is 0.499500

it takes 309.810000 seconds to run the adaptation algorithm

it takes 84.110000 seconds to compute g and sigma

it takes 124.310000 seconds to generate the first Markov Chain

it takes 124.430000 seconds to generate the second Markov Chain

it takes 124.950000 seconds to generate the third Markov Chain

it takes 124.400000 seconds to generate the fourth Markov Chain

it takes 124.030000 seconds to generate the fifth Markov Chain

it takes 1775.810000 seconds to test the local acceptance

1

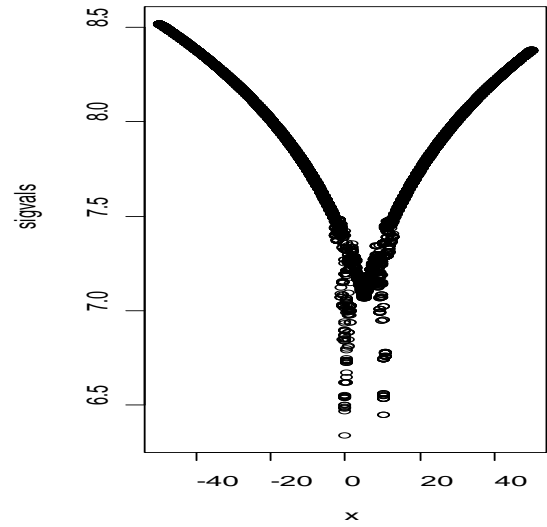
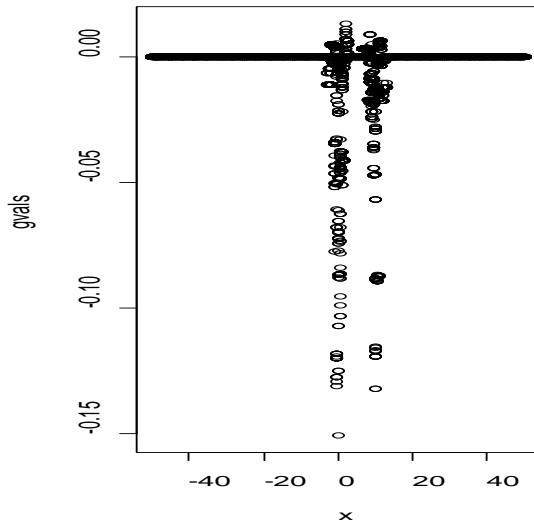
[1] 12.94547

[1] 0.06114334

[1] 7.74818

2.2.4.6 case 123 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{width} = 1$, with fixed bandwidth

$b_n = 1$

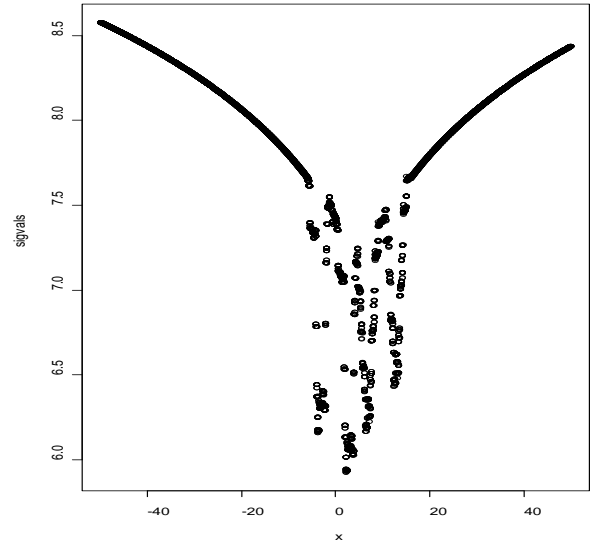
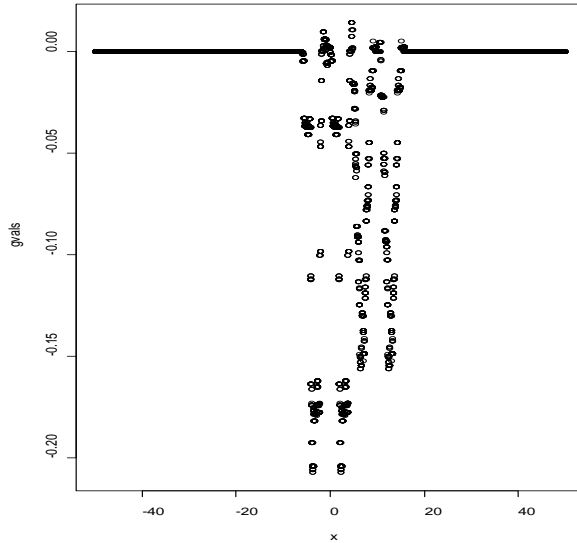


1

[1] 14.42627
 [1] 0.06452843
 [1] 7.019186

2.2.4.7 case 124 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{width} = 2$, with fixed bandwidth

$b_n = 1$



Accepted 24217 out of 100000 (24.217%).

final beta = 1.961981

alpha(5.000000) is 0.855500

alpha(7.000000) is 0.584500

alpha(10.000000) is 0.185600

alpha(20.000000) is 0.505800

alpha(30.000000) is 0.494700

alpha(50.000000) is 0.499600

alpha(70.000000) is 0.494600

alpha(120.000000) is 0.501400

alpha(150.000000) is 0.501700

it takes 307.750000 seconds to run the adaptation algorithm

it takes 84.090000 seconds to compute g and sigma

it takes 118.580000 seconds to generate the first Markov Chain

it takes 118.320000 seconds to generate the second Markov Chain

it takes 118.810000 seconds to generate the third Markov Chain

it takes 118.700000 seconds to generate the fourth Markov Chain

it takes 118.490000 seconds to generate the fifth Markov Chain

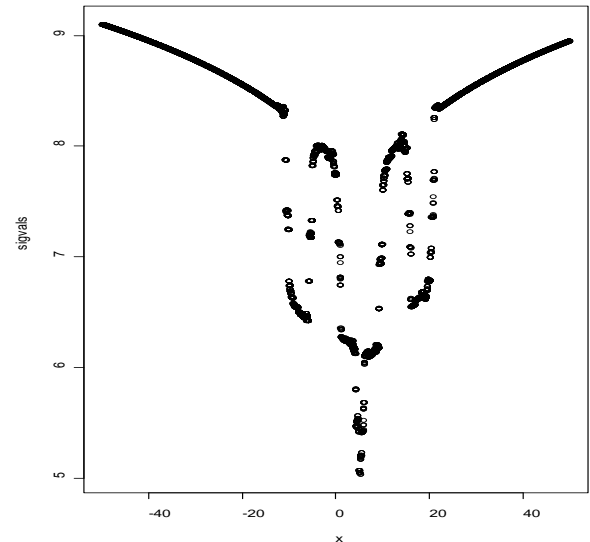
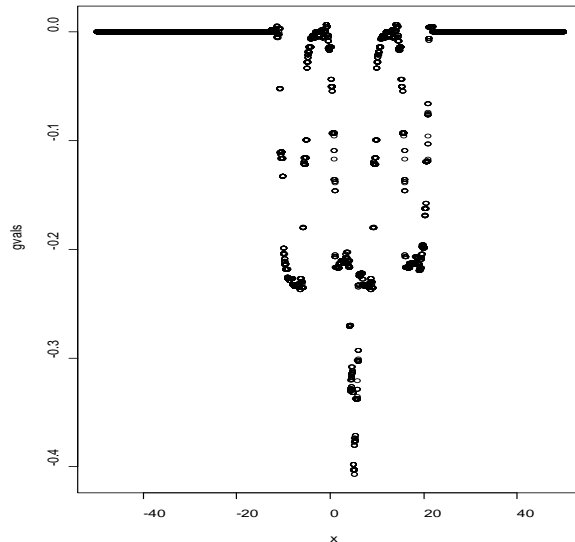
it takes 1760.380000 seconds to test the local acceptance

1

[1] 14.49698
[1] 0.06464175
[1] 6.796207

2.2.4.8 case 125 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{width} = 5$, with fixed bandwidth

$b_n = 1$



Accepted 24435 out of 100000 (24.435%).

final beta = 2.021228

alpha(5.000000) is 0.953600

alpha(7.000000) is 0.595700

alpha(10.000000) is 0.194000

alpha(20.000000) is 0.508900

alpha(30.000000) is 0.505300

alpha(50.000000) is 0.498600

alpha(70.000000) is 0.496300

alpha(120.000000) is 0.496100

alpha(150.000000) is 0.495600

it takes 307.200000 seconds to run the adaptation algorithm

it takes 83.720000 seconds to compute g and sigma

it takes 119.290000 seconds to generate the first Markov Chain

it takes 118.780000 seconds to generate the second Markov Chain

it takes 119.190000 seconds to generate the third Markov Chain

it takes 119.890000 seconds to generate the fourth Markov Chain

it takes 119.000000 seconds to generate the fifth Markov Chain

it takes 1754.180000 seconds to test the local acceptance

1

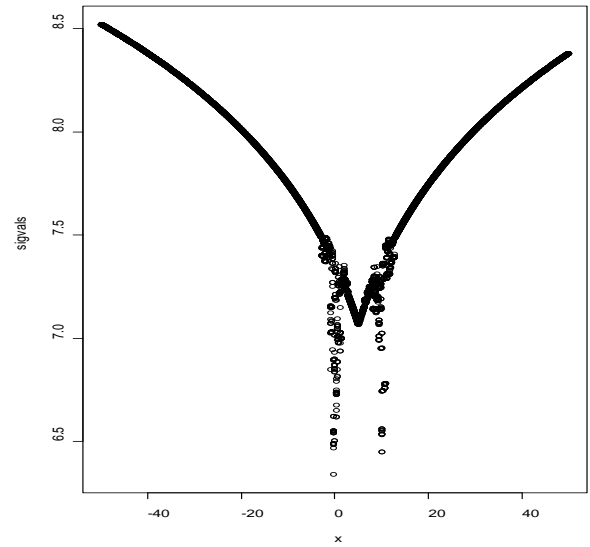
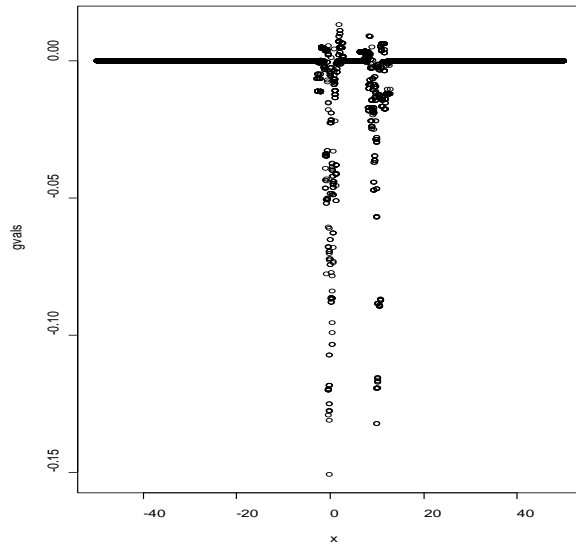
[1] 14.63965

[1] 0.06480795

[1] 7.008607

2.2.4.9 case 126 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{width} = 0.2$, with fixed bandwidth

$b_n = 1$



1

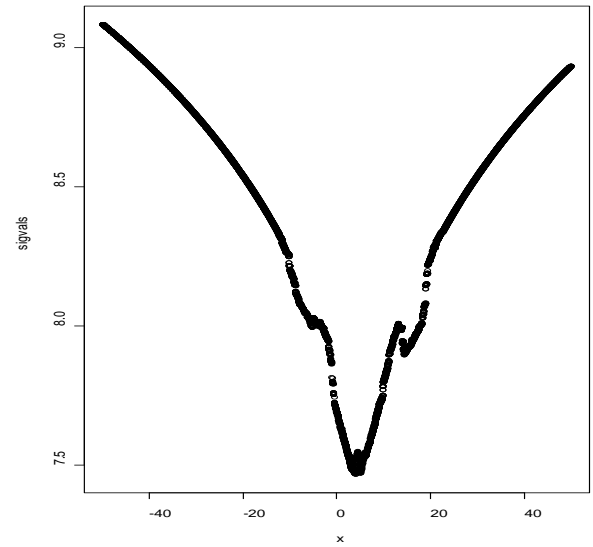
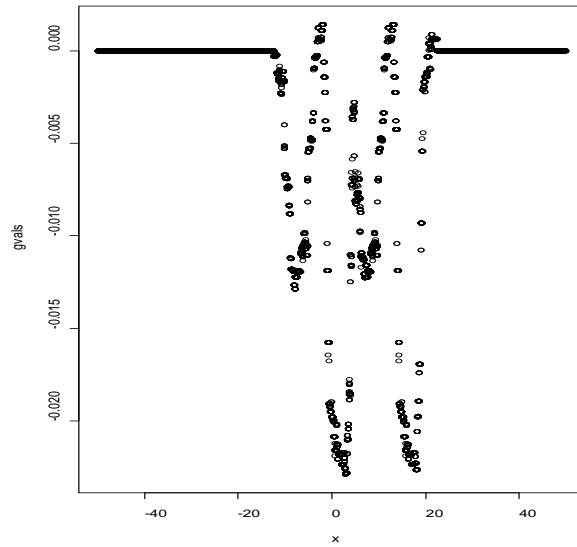
[1] 15.07854

[1] 0.06592749

[1] 6.8665

2.2.4.10 case 127 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1$, width = 0.2, with fixed bandwidth

$b_n = 10$



1

```

> asjd = function(x){
+ val = 0
+ for(i in (B+1):M )
+   val = val +(xlist[i]-xlist[i-1])^2
+ return (val/(M-B))
+ }
> L = length(gvals)
> x = seq(-50,50,length = L)
> M = 10^5
> B = 10^4
> varfact = function(xxx) { 2 * sum(acf(xxx, plot=FALSE)$acf) - 1 }
> asjd = function(x){
+ val = 0
+ for(i in (B+1):M )
+   val = val +(xlist[i]-xlist[i-1])^2
+ return (val/(M-B))
+ }
>
>
>
>
> pdf(file = ifelse(T, "trace plot.pdf", "trace plot%03d.pdf"),width=10,height=5,pointsize =
1/200)
> par(mfrow=c(3,2))
> source("xlist1");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 14.10879
[1] 0.0637883
[1] 7.253909
> source("xlist2");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 13.49518
[1] 0.06256611
[1] 7.351082
> source("xlist3");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 13.22538
[1] 0.06178781
[1] 7.209034
> source("xlist4");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 13.95147
[1] 0.06346684
[1] 7.0977

```

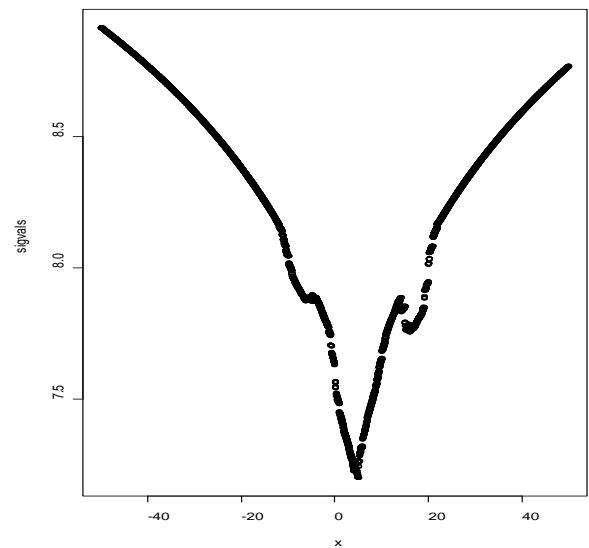
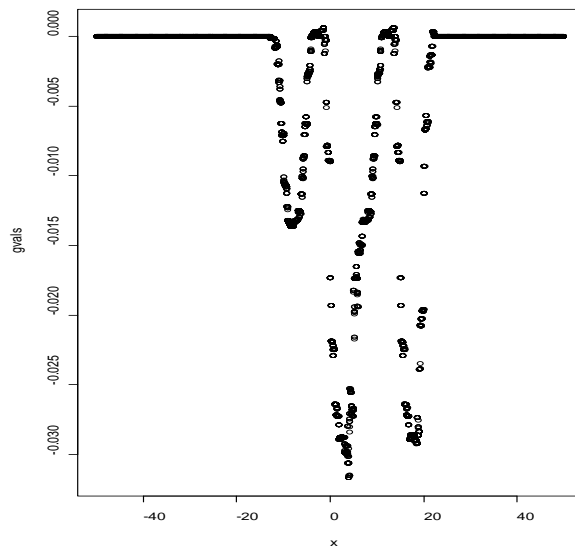
```

> source("xlist5");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 13.37783
[1] 0.06227059
[1] 7.294676

```

2.2.4.11 case 128 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{width} = 0.2$, with fixed bandwidth

$b_n = 0.1$



Accepted 23425 out of 100000 (23.425%).

final beta = 2.000723

alpha(5.000000) is 0.835800

alpha(7.000000) is 0.543300

alpha(10.000000) is 0.191800

alpha(20.000000) is 0.509000

alpha(30.000000) is 0.506600

alpha(50.000000) is 0.507000

alpha(70.000000) is 0.499800

alpha(120.000000) is 0.503600

alpha(150.000000) is 0.497900

it takes 307.160000 seconds to run the adaptation algorithm

it takes 83.710000 seconds to compute g and sigma

it takes 119.950000 seconds to generate the first Markov Chain

it takes 118.830000 seconds to generate the second Markov Chain

it takes 119.610000 seconds to generate the third Markov Chain

it takes 119.170000 seconds to generate the fourth Markov Chain

it takes 118.640000 seconds to generate the fifth Markov Chain

it takes 1751.980000 seconds to test the local acceptance

1

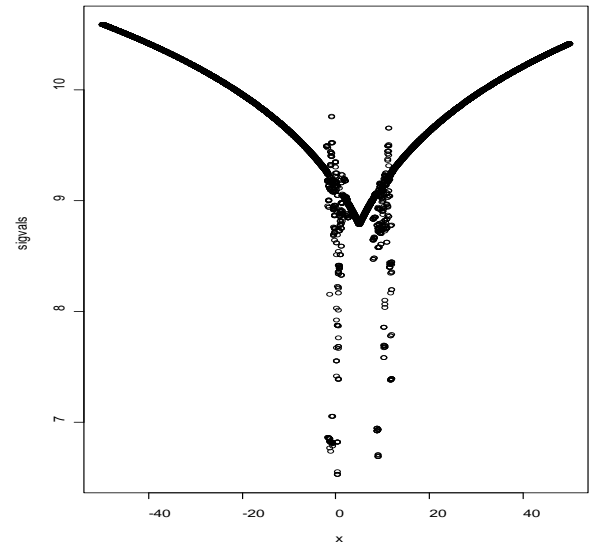
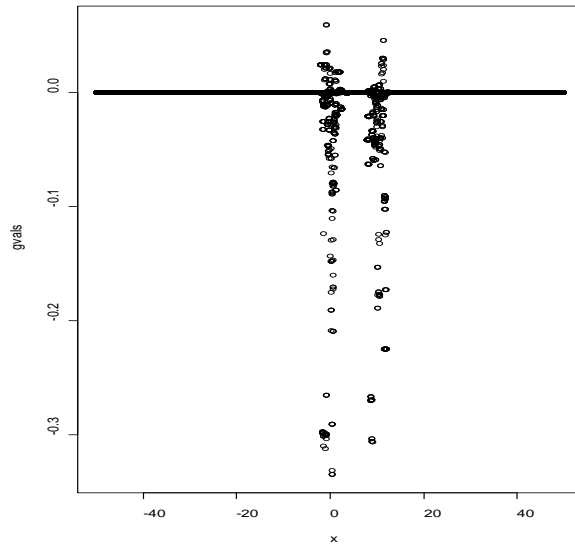
[1] 13.83392

[1] 0.06320622

[1] 7.1248

2.2.4.12 case 127 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{width} = 0.2$, with decreasing

bandwidth $b_n = \frac{1}{n^{0.2}}$

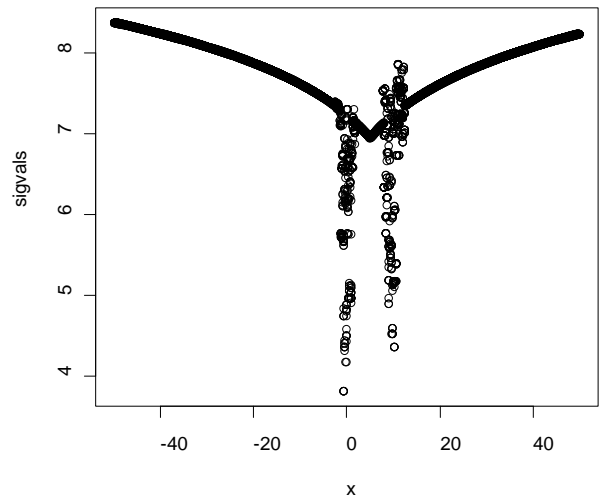
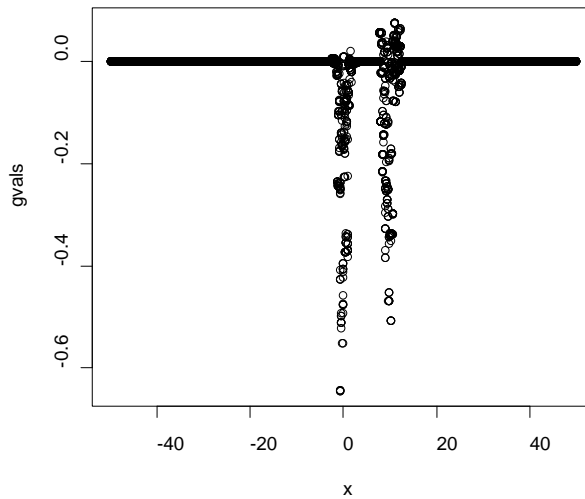


1

[1] 14.64450
 [1] 0.0651862
 [1] 7.411176

2.2.4.13 case 128 $\eta_n = \frac{1}{(n+5)^{0.8}}$, $C = 0.1, \gamma = 0.1$, width = 0.2, with fixed bandwidth

$b_n = 1$



Accepted 24581 out of 100000 (24.581%).

final beta = 1.938198

alpha(5.000000) is 0.851400

alpha(7.000000) is 0.553300

alpha(10.000000) is 0.197900

alpha(20.000000) is 0.503200

alpha(30.000000) is 0.494000

alpha(50.000000) is 0.498300

alpha(70.000000) is 0.496000

alpha(120.000000) is 0.496600

alpha(150.000000) is 0.512100

it takes 312.800000 seconds to run the adaptation algorithm

it takes 83.730000 seconds to compute g and sigma

it takes 117.950000 seconds to generate the first Markov Chain

it takes 118.380000 seconds to generate the second Markov Chain

it takes 118.000000 seconds to generate the third Markov Chain

it takes 117.490000 seconds to generate the fourth Markov Chain

it takes 117.520000 seconds to generate the fifth Markov Chain

it takes 1752.870000 seconds to test the local acceptance

1

[1] 18.1577

[1] 0.07247686

[1] 5.867065

2.2.5 constant $\sigma(x) = C$

```
> cat("ran Metropolis algorithm for", M, "iterations, with burn-in", B, "\n");
ran Metropolis algorithm for 1e+05 iterations, with burn-in 10000
> cat("acceptance rate =", num/M, "\n");
acceptance rate = 0.23382
>
> varf;
[1] 13.13618
> se;
[1] 0.0616654
> asjd;
[1] 7.204595
```

```
> cat("ran Metropolis algorithm for", M, "iterations, with burn-in", B, "\n");
ran Metropolis algorithm for 1e+05 iterations, with burn-in 10000
> cat("acceptance rate =", num/M, "\n");
acceptance rate = 0.23263
>
> varf;
[1] 13.87016
> se;
[1] 0.06330728
> asjd;
[1] 7.282846
```

```
> cat("ran Metropolis algorithm for", M, "iterations, with burn-in", B, "\n");
ran Metropolis algorithm for 1e+05 iterations, with burn-in 10000
> cat("acceptance rate =", num/M, "\n");
acceptance rate = 0.23461
>
> varf;
[1] 13.78088
> se;
[1] 0.06301751
> asjd;
[1] 7.396178
```

```
> cat("ran Metropolis algorithm for", M, "iterations, with burn-in", B, "\n");
ran Metropolis algorithm for 1e+05 iterations, with burn-in 10000
> cat("acceptance rate =", num/M, "\n");
acceptance rate = 0.23545
```

```
> varf;  
[1] 13.15203  
> se;  
[1] 0.0615862  
> asjd;  
[1] 7.319729
```

```
> cat("ran Metropolis algorithm for", M, "iterations, with burn-in", B, "\n");  
ran Metropolis algorithm for 1e+05 iterations, with burn-in 10000  
> cat("acceptance rate =", num/M, "\n");  
acceptance rate = 0.23389
```

```
>  
> varf;  
[1] 14.7803  
> se;  
[1] 0.0654612  
> asjd;  
[1] 7.25605
```

```
> cat("ran Metropolis algorithm for", M, "iterations, with burn-in", B, "\n");  
ran Metropolis algorithm for 1e+05 iterations, with burn-in 10000  
> cat("acceptance rate =", num/M, "\n");  
acceptance rate = 0.23557
```

```
>  
> varf;  
[1] 13.29707  
> se;  
[1] 0.06180272  
> asjd;  
[1] 7.169893
```

2.2.6 varfact comparison

kernel function $K(x) = e^{-\frac{ x ^{\alpha_1}}{\alpha_2}}$										
α_1	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run	
1	1	2	1	$\frac{1}{(n+5)^{0.5}}$	17.69815	17.96696	16.85364	17.94989	17.14759	
2					14.95411	13.80018	13.74683	14.68709	13.98678	
10					14.46429	15.19155	14.90729	14.72928	15.06675	
0.1					14.34042	13.87193	13.79645	13.24493	13.59459	
0.5					14.83536	15.16301	14.53647	13.99793	13.72507	
0.01					22.38718	22.21759	21.64512	21.04189	21.60776	
2	10	1	1	$\frac{1}{(n+5)^{0.5}}$	20.01951	18.42564	17.85715	18.41037	18.24566	
	0.1				10	13.7	13.29679	12.96888	13.27147	12.56142
					1	32.15388	32.82322	33.58812	32.00728	33.06702
					0.1	13.00467	14.39601	13.2234	13.0975	12.76278
	2	0.1	2	$\frac{1}{n^{0.2}}$	10	13.76117	14.83305	15.0663	14.10183	14.24509
					0.1	12.86394	12.7031	11.99687	12.00228	12.88139
					0.1	15.77916	14.91464	14.67844	16.82218	15.5557
					10	16.43819	16.60408	17.4054	17.26619	17.61966
			10	$\frac{1}{(n+5)^{0.8}}$	13.23106	13.0639	13.65704	13.23585	13.18471	

The best case is;

case 78 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth $b_n = 10$

kernel function $K(x) = \frac{1}{1 + \alpha_1 x ^{\alpha_2}}$									
α_1	γ	C	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
1	2	1	1	$\frac{1}{(n+5)^{0.5}}$	20.27012	20.11195	21.12319	19.69325	19.49482
10					15.69775	16.31847	17.38448	15.9035	16.85428
0.1					17.99677	19.78633	17.97754	19.07744	18.48608
12					19.31375	18.98969	18.15367	19.02709	19.10133
5					20.26718	19.14768	20.01333	19.97645	19.09234
10					10	55.52678	52.85685	52.491	54.99053
	0.1	10	13.12142	12.64089	13.28427	12.47632	12.47803		
		0.1	13.58733	12.41142	12.40737	13.24543	12.94998		
		0.1	13.04691	13.63237	13.14097	12.45919	13.93196		
		10	15.32114	14.14721	14.81707	14.93572	14.33295		
	0.1	18.64611	17.79232	19.85046	18.25231	18.55894			

			$\frac{1}{n^{0.2}}$		13.61764	13.98172	13.41386	13.11681	14.00296
			1	$\frac{1}{(n+5)^{0.8}}$	18.34272	18.0786	17.18455	19.03875	18.03951

The best case is :

case 97 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 10, \gamma = 0.1$ with fixed bandwidth $b_n = 1$

$$\text{kernel function } K(x) = \begin{cases} 0, & |x| \geq 2 * \text{width} \\ -1 * \text{height}, & \text{width} < |x| < 2 * \text{width} \\ 1 * \text{height}, & |x| \leq \text{width} \end{cases}$$

C	γ	height	width	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
1	2	0.5	0.5	1	$\frac{1}{(n+5)^{0.5}}$	15.50201	16.26951	17.4331	15.55692	15.87749
10						17.98869	19.55673	19.11706	19.4903	18.30191
0.1	10	0.5	0.5	1	$\frac{1}{(n+5)^{0.5}}$	13.16841	12.91911	14.08071	13.82063	13.42696
	0.1					36.04216	36.61575	35.55663	36.17935	36.67233
	2	1	0.5	1	$\frac{1}{(n+5)^{0.5}}$	13.99116	14.12284	15.72336	13.55838	13.54641
		5				12.50317	12.30035	13.56912	12.80086	13.20776
	0.1	1	0.1	1	$\frac{1}{(n+5)^{0.5}}$	18.81126	18.54136	18.27606	19.26981	19.00901
						0.1	14.13331	14.61382	14.34998	13.46336
	0.1	1	0.1	1	$\frac{1}{(n+5)^{0.5}}$	15.09972	14.44022	14.08979	14.83034	14.21126
						5	12.90002	13.21733	13.23861	13.22283
	0.1	1	0.1	1	$\frac{1}{(n+5)^{0.5}}$	12.57327	12.491	13.2023	12.02869	12.13842
						10	13.50934	14.19841	14.90362	14.71978
0.1	1	0.1	1	$\frac{1}{(n+5)^{0.5}}$	12.42918	12.50971	12.60511	13.22798	11.9384	
					0.1	11.79056	12.93844	12.33559	12.7613	11.16328
					$\frac{1}{(n+5)^{0.8}}$	12.55904	12.68916	12.20365	12.05565	12.90081

The best case is:

case 116 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{height} = 1, \text{width} = 0.1,$ with decreasing

bandwidth $b_n = \frac{1}{n^{0.2}}$

$$\text{kernel function } K(x) = \begin{cases} 0, & |x| \geq 2 * \text{width} \text{ or } |x| \leq \text{width} \\ 1, & \text{width} < |x| < 2 * \text{width} \end{cases}$$

C	γ	width	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run	
1	2	0.5	1	$\frac{1}{(n+5)^{0.5}}$	16.51565	18.22744	15.92406	17.40298	17.38122	
0.1					12.6270	12.55610	14.12581	14.04699	13.80102	
10					22.08531	22.36662	24.28318	22.38431	22.79518	
0.1	10	0.1	1		46.47284	48.2707	47.34358	46.03923	48.46781	
					13.11484	13.85565	12.77984	13.13842	12.94547	
					13.23159	14.77552	13.67518	15.07019	14.42627	
					15.42502	14.14825	14.85676	14.78062	14.49698	
					14.72672	14.49256	12.60517	13.93011	14.63965	
					14.26320	14.07368	15.16668	15.36069	15.07854	
					14.10879	13.49518	13.22538	13.95147	13.37783	
					10	13.29121	13.61542	14.84861	13.48883	13.83392
					0.1	13.37948	13.37175	13.69730	13.51921	14.64450
		$\frac{1}{n^{0.2}}$								

The best case is:

case 122 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{width} = 0.5$, with fixed bandwidth $b_n = 1$

constant $\sigma(x) = C$				
First run	Second run	Third run	Fourth run	Fifth run
13.13618	13.87016	13.78088	13.15203	13.29707

2.2.7 variance comparison

kernel function $K(x) = e^{-\frac{ x ^{\alpha_1}}{\alpha_2}}$										
α_1	γ	C	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run	
1	1	2	1	$\frac{1}{(n+5)^{0.5}}$	0.07154074	0.07193655	0.06989788	0.07191396	0.07038708	
2					0.06550641	0.06316496	0.0626794	0.06511746	0.06355741	
10					0.06475452	0.06649223	0.06553578	0.0652558	0.06591678	
0.1					0.06437798	0.0632377	0.06322152	0.06182315	0.06266335	
0.5					0.06575282	0.06612688	0.06453477	0.06354389	0.06299655	
0.01					0.08035613	0.07999806	0.07908512	0.07824674	0.0791383	
2	10	1	1	$\frac{1}{(n+5)^{0.5}}$	0.07581159	0.07303472	0.07170715	0.07310784	0.07269454	
	0.1				0.06287379	0.0619756	0.06102925	0.0619696	0.06021042	
					10	0.09599056	0.09769438	0.09826665	0.09655463	0.09774311
					1	0.0613665	0.06454725	0.06190249	0.06136325	0.06078702
	0.1	0.06305008	0.06538476	0.06595366	0.06393927	0.06419357				
	2	0.1	2	$\frac{1}{n^{0.2}}$	10	0.06090368	0.06061328	0.05894096	0.05876169	0.06114331
					0.1	0.06755124	0.06559679	0.06504136	0.0696462	0.06697404
					$\frac{1}{n^{0.2}}$	0.06887529	0.06929928	0.07082739	0.07069858	0.0711586
					10	0.06171668	0.06159626	0.0628181	0.06180789	0.06168104
					$\frac{1}{(n+5)^{0.8}}$					

The best case is:

case 78 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth $b_n = 10$

kernel function $K(x) = \frac{1}{1 + \alpha_1 x ^{\alpha_2}}$										
α_1	γ	C	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run	
1	2	1	1	$\frac{1}{(n+5)^{0.5}}$	0.07629325	0.07587907	0.0781154	0.07529194	0.07497625	
10					0.06719478	0.06871731	0.07076993	0.06748606	0.06995134	
0.1					0.07226338	0.07567992	0.07210705	0.07443589	0.07306009	
12					0.07443621	0.07443067	0.07245077	0.07427455	0.07426885	
5					0.07666722	0.07458284	0.07591355	0.07602797	0.07416466	
10	10	1	1	$\frac{1}{(n+5)^{0.5}}$	0.1277001	0.1222414	0.1220896	0.1253721	0.1244969	
	0.1				0.06150226	0.06049887	0.06188916	0.05988082	0.05992151	
					10	0.06273084	0.05980796	0.05994844	0.06195356	0.06111524
					0.1	0.06129223	0.06265302	0.06158764	0.06001449	0.06357011
					10	0.06658314	0.06392398	0.06548828	0.06572278	0.06422718
					0.1	0.07344185	0.07158091	0.07582998	0.07245237	0.07316876

			$\frac{1}{n^{0.2}}$		0.06273164	0.06365028	0.06226108	0.06163139	0.06365483
			1	$\frac{1}{(n+5)^{0.8}}$	0.07275788	0.07213117	0.07042167	0.07417965	0.07210694

The best case is :

case 97 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 10, \gamma = 0.1$ with fixed bandwidth $b_n = 1$

$$\text{kernel function } K(x) = \begin{cases} 0, & |x| \geq 2 * \text{width} \\ -1 * \text{height}, & \text{width} < |x| < 2 * \text{width} \\ 1 * \text{height}, & |x| \leq \text{width} \end{cases}$$

C	γ	height	width	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run	
1	2	0.5	0.5	1	$\frac{1}{(n+5)^{0.5}}$	0.06687103	0.06847918	0.07115063	0.06699158	0.06777017	
10						0.07202369	0.07508933	0.07414543	0.07515094	0.07264643	
0.1	10	0.5	0.5	1		0.06166654	0.060983	0.0637165	0.06336811	0.06233687	
						0.1019297	0.102977	0.1014364	0.1026182	0.1030286	
	0.1	1	0.5	1		0.06356368	0.06403037	0.06759348	0.06273767	0.06246479	
						0.06018968	0.05974201	0.06253642	0.060799	0.06187482	
	2	1	0.5	1		0.07375515	0.07327441	0.07266018	0.07462279	0.07394524	
						0.06394895	0.06489215	0.0642523	0.06229267	0.0653481	
	1	1	0.1	0.1		$\frac{1}{n^{0.2}}$	0.06595247	0.06471726	0.06365214	0.0653969	0.0639442
							0.06086061	0.06180042	0.06187954	0.06189745	0.06167256
2	1	0.1	0.1	$\frac{1}{n^{0.2}}$	0.06029126	0.05995545	0.06172432	0.05899454	0.05919573		
					0.06261301	0.06407868	0.06556438	0.06525447	0.06225008		
1	1	0.1	0.1	$\frac{1}{n^{0.2}}$	0.05999715	0.06028388	0.06027195	0.06199946	0.05869727		
					0.05833108	0.06115153	0.05970294	0.06067416	0.05691963		
					$\frac{1}{(n+5)^{0.8}}$	0.06024648	0.06057204	0.05938889	0.05899644	0.0611555	

The best case is:

case 116 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{height} = 1, \text{width} = 0.1,$ with decreasing

bandwidth $b_n = \frac{1}{n^{0.2}}$

$$\text{kernel function } K(x) = \begin{cases} 0, & |x| \geq 2 * \text{width} \text{ or } |x| \leq \text{width} \\ 1, & \text{width} < |x| < 2 * \text{width} \end{cases}$$

C	γ	width	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
1	2	0.5	1	$\frac{1}{(n+5)^{0.5}}$	0.0688377	0.07281504	0.06764052	0.07086825	0.07095952
0.1					0.06047511	0.0601648	0.06383409	0.06352232	0.0632373
10					0.07988052	0.08018424	0.0835769	0.08041703	0.08128286
0.1	10	1	0.1156726		0.1176081	0.1167444	0.1153350	0.1181587	
			0.06155224		0.06305464	0.06067722	0.06163425	0.06114334	
	0.1	1	0.06183885		0.06549107	0.06257762	0.0660431	0.06452843	
		2	0.0667545		0.06391155	0.0653105	0.06523758	0.06464175	
		5	0.06525439		0.06470269	0.0602786	0.06347932	0.06480795	
		10	0.06396429		0.06371747	0.06614052	0.06661003	0.06592749	
		0.2	0.0637883		0.06256611	0.06178781	0.06346684	0.06227059	
0.1	0.06208175	0.06271901	0.06542974	0.06230577	0.06320622				
$\frac{1}{n^{0.2}}$	0.06218174	0.06223508	0.06291217	0.06254374	0.0651862				

The best case is:

case 127 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{width} = 0.2$, with decreasing bandwidth

$$b_n = \frac{1}{n^{0.2}}$$

constant $\sigma(x) = C$				
First run	Second run	Third run	Fourth run	Fifth run
0.061665	0.06330728	0.06301751	0.0615862	0.0654612

2.2.8 comparison of average squared jump distance

kernel function $K(x) = e^{-\frac{ x ^{\alpha_1}}{\alpha_2}}$										
α_1	γ	C	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run	
1	1	2	1	$\frac{1}{(n+5)^{0.5}}$	5.873551	5.901538	5.852935	5.774491	5.77809	
2					6.773307	6.938589	6.937717	7.121168	6.943634	
10					6.928128	6.721215	6.860596	6.818162	6.664103	
0.1					7.004704	6.809467	6.970135	7.051681	7.059283	
0.5					6.972854	6.879271	6.854267	6.893609	6.884881	
0.01					5.091557	4.989655	4.981934	5.225652	4.975623	
2	10	1	1	$\frac{1}{(n+5)^{0.5}}$	5.651396	5.739741	5.687458	5.634909	5.745729	
	0.1				7.69529	7.737276	7.478679	7.668143	7.484434	
					10	3.69852	3.628897	3.603881	3.616932	3.609716
					1	7.389716	7.380399	7.403763	7.493079	7.467558
	0.1	7.01781	6.925817	7.223606	7.042545	6.900112				
	0.1	2	10	7.728795	7.719727	8.015229	7.980781	7.709572		
			0.1	6.412002	6.535136	6.507305	6.503781	6.533062		
			$\frac{1}{n^{0.2}}$	6.213535	6.22061	6.262421	6.301681	6.218763		
			10	$\frac{1}{(n+5)^{0.8}}$	7.503375	7.499092	7.287635	7.384808	7.440597	

The best case is;

case 78 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth $b_n = 10$

kernel function $K(x) = \frac{1}{1 + \alpha_1 x ^{\alpha_2}}$									
α_1	γ	C	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
1	2	1	1	$\frac{1}{(n+5)^{0.5}}$	5.308739	5.376076	5.25213	5.306378	5.323529
10					6.192003	6.254055	5.980946	6.28541	6.095268
0.1					5.777566	5.582482	5.701381	5.649991	5.840868
12					5.630077	5.722548	5.749735	5.689602	5.761007
5					5.512693	5.530929	5.461332	5.455003	5.474942
10	10	1	1	$\frac{1}{(n+5)^{0.5}}$	1.660918	1.65942	1.720822	1.617675	1.709541
	0.1				7.655875	7.656696	7.482752	7.638246	7.639173
		7.445668	7.493031	7.48323	7.579445	7.64341			
		7.437534	7.532984	7.525821	7.588561	7.406249			
		10	6.988029	6.857484	6.945544	6.965335	7.005803		
	0.1	5.491011	5.335033	5.349837	5.463103	5.515589			

			$\frac{1}{n^{0.2}}$		7.379925	7.319542	7.527431	7.500853	7.400967
		1	$\frac{1}{(n+5)^{0.8}}$		5.593592	5.552727	5.602003	5.673047	5.518752

The best case is :

case 97 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 10, \gamma = 0.1$ with fixed bandwidth $b_n = 1$

$$\text{kernel function } K(x) = \begin{cases} 0, & |x| \geq 2 * \text{width} \\ -1 * \text{height}, & \text{width} < |x| < 2 * \text{width} \\ 1 * \text{height}, & |x| \leq \text{width} \end{cases}$$

C	γ	height	width	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run	
1	2	0.5	0.5	1	$\frac{1}{(n+5)^{0.5}}$	6.344871	6.382293	6.453518	6.396776	6.794295	
10						5.634184	5.595427	5.579323	5.695321	5.623555	
0.1	10	0.5	0.5	1		7.445216	7.253714	7.196647	7.182623	7.217294	
						3.294306	3.369713	3.355714	3.43006	3.271804	
	0.1	1	0.5	1		7.065596	6.907671	7.017294	6.967323	7.10335	
						7.621703	7.488763	7.694096	7.716375	7.630405	
	5	1	0.5	1		6.122762	5.888783	6.063521	5.941985	6.026763	
						6.942994	7.18058	7.090891	7.165429	6.995348	
	0.1	1	0.5	1		1	7.100944	7.212488	7.00521	7.118056	7.098321
							7.628372	7.578396	7.483249	7.48983	7.480724
10	2	1	0.1	1	8.049105	7.920465	7.715893	7.935231	7.954234		
					7.23596	7.043965	6.929782	6.959583	6.997632		
0.1	2	1	0.1	1	7.776327	7.678879	7.621687	7.649541	7.548351		
					8.03459	8.031316	7.766907	7.8188	8.158163		
					$\frac{1}{(n+5)^{0.8}}$	7.752874	8.032417	8.022584	8.001408	7.84211	

The best case is:

case 116 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{height} = 1, \text{width} = 0.1$, with decreasing

bandwidth $b_n = \frac{1}{n^{0.2}}$

$$\text{kernel function } K(x) = \begin{cases} 0, & |x| \geq 2 * \text{width} \text{ or } |x| \leq \text{width} \\ 1, & \text{width} < |x| < 2 * \text{width} \end{cases}$$

C	γ	width	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
1	2	0.5	1	$\frac{1}{(n+5)^{0.5}}$	6.012644	5.993335	6.183591	5.966074	6.096523
0.1					7.403707	7.4661	7.376348	7.236378	7.232841
10					5.024682	4.924248	4.869332	4.788359	4.885462
0.1	0.1	1	10		2.656734	2.535808	2.508755	2.621832	2.552771
			1		7.522012	7.63438	7.592666	7.63681	7.74818
			2		6.954202	6.927666	7.030507	6.864217	7.019186
			5		6.956227	6.856488	6.83983	6.806807	6.8665
			0.2		6.7738	6.86222	6.809493	6.83525	6.796207
			10		6.944817	7.050115	7.056753	7.206524	7.008607
			0.1		7.253909	7.351082	7.209034	7.0977	7.294676
			0.1		7.361709	7.091562	7.160905	7.246703	7.1248
			$\frac{1}{n^{0.2}}$		7.598452	7.649363	7.587748	7.615007	7.411176

The best case is:

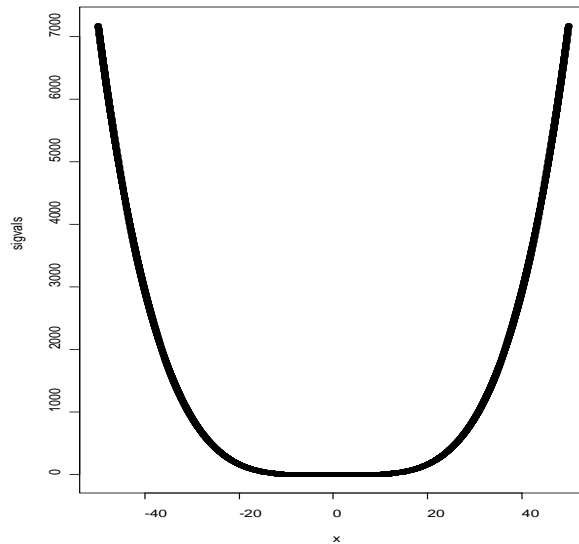
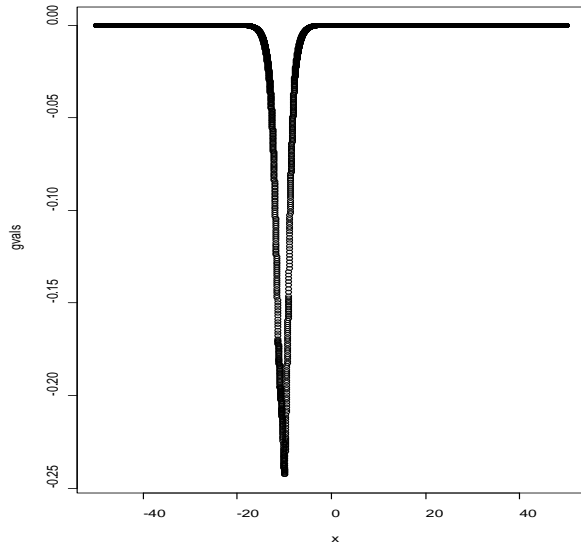
case 122 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $C = 0.1, \gamma = 0.1, \text{width} = 0.5$, with fixed bandwidth $b_n = 1$

constant $\sigma(x) = C$				
First run	Second run	Third run	Fourth run	Fifth run
7.204595	7.282846	7.396178	7.31972	7.25605

2.3 Example 3: mixture of three normal distributions in R^1

2.3.1 kernel function $K(x) = e^{-\frac{|x|^{\alpha_1}}{\alpha_2}}$

2.3.1.1 case 129 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 76483 out of 100000 (76.483%).

final beta = -6.748936

alpha(0.000000) is 0.765200

alpha(2.000000) is 0.727800

alpha(5.000000) is 0.958900

alpha(8.000000) is 0.590400

alpha(10.000000) is 0.155000

alpha(13.000000) is 0.121000

alpha(15.000000) is 0.100400

alpha(20.000000) is 0.058200

alpha(30.000000) is 0.018300

alpha(50.000000) is 0.004300

it takes 447.440000 seconds to run the adaptation algorithm

it takes 198.950000 seconds to compute g and sigma

it takes 166.460000 seconds to generate the first Markov Chain

it takes 166.820000 seconds to generate the second Markov Chain

it takes 168.250000 seconds to generate the third Markov Chain

it takes 169.860000 seconds to generate the fourth Markov Chain

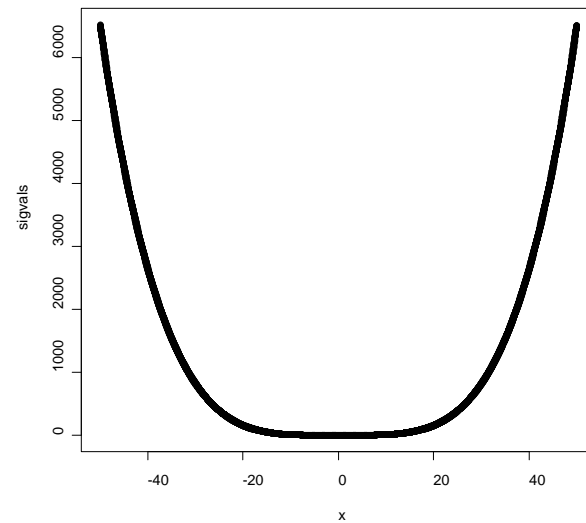
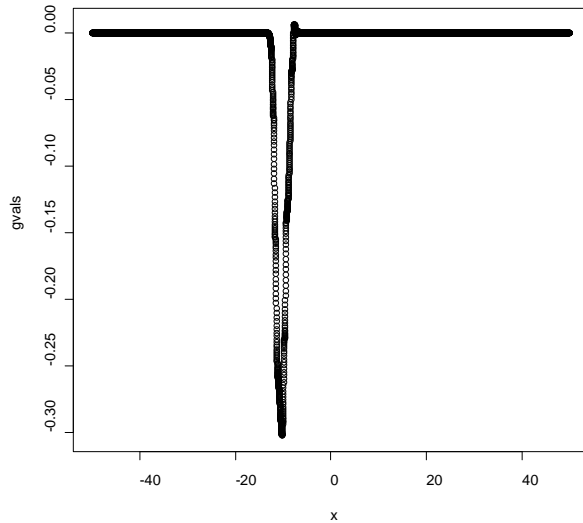
it takes 166.760000 seconds to generate the fifth Markov Chain

it takes 1317.690000 seconds to test the local acceptance

1

[1] 0.2709634

2.3.1.2 case 130 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 23986 out of 100000 (23.986%).

final beta = -6.847073

alpha(0.000000) is 0.786900

alpha(2.000000) is 0.745000

alpha(5.000000) is 0.953800

alpha(8.000000) is 0.605300

alpha(10.000000) is 0.166700

alpha(13.000000) is 0.119100

alpha(15.000000) is 0.105400

alpha(20.000000) is 0.064500

alpha(30.000000) is 0.021300

alpha(50.000000) is 0.005200

it takes 770.470000 seconds to run the adaptation algorithm

it takes 353.150000 seconds to compute g and sigma

it takes 167.060000 seconds to generate the first Markov Chain

it takes 167.030000 seconds to generate the second Markov Chain

it takes 165.370000 seconds to generate the third Markov Chain

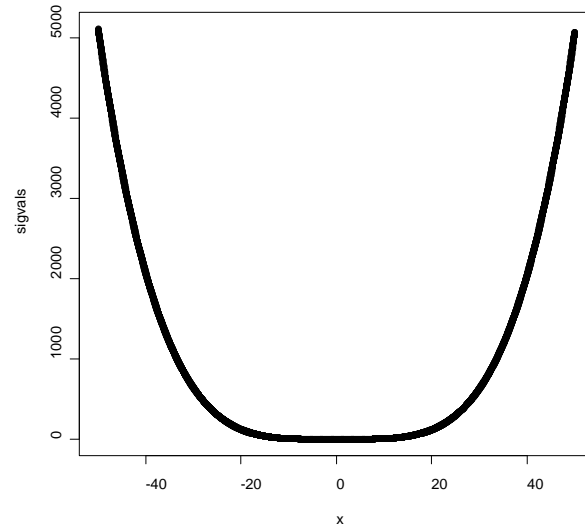
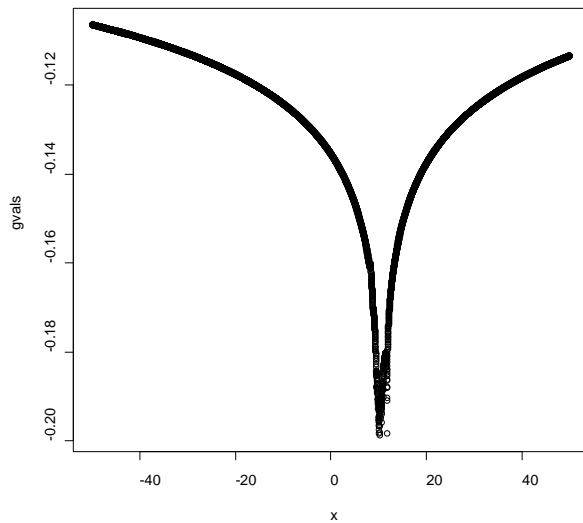
it takes 170.350000 seconds to generate the fourth Markov Chain

it takes 164.040000 seconds to generate the fifth Markov Chain

it takes 1752.270000 seconds to test the local acceptance

1

2.3.1.3 case 131 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 83273 out of 100000 (83.273%).

final beta = -6.981961

alpha(0.000000) is 0.855400

alpha(2.000000) is 0.781100

alpha(5.000000) is 0.956300

alpha(8.000000) is 0.638800

alpha(10.000000) is 0.224100

alpha(13.000000) is 0.139900

alpha(15.000000) is 0.134600

alpha(20.000000) is 0.079600

alpha(30.000000) is 0.028900

alpha(50.000000) is 0.005400

it takes 648.690000 seconds to run the adaptation algorithm

it takes 283.420000 seconds to compute g and sigma

it takes 165.590000 seconds to generate the first Markov Chain

it takes 169.070000 seconds to generate the second Markov Chain

it takes 165.930000 seconds to generate the third Markov Chain

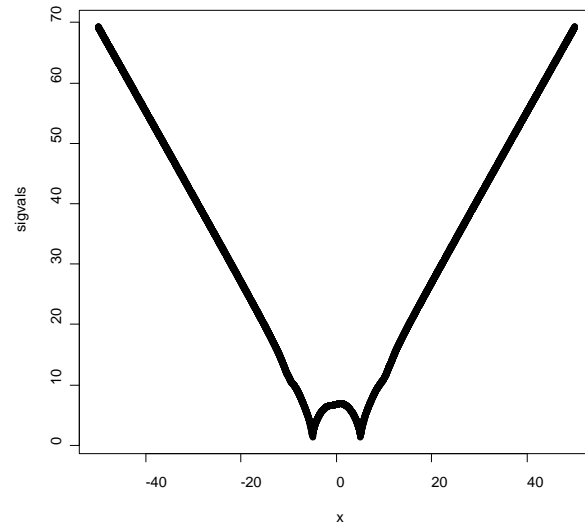
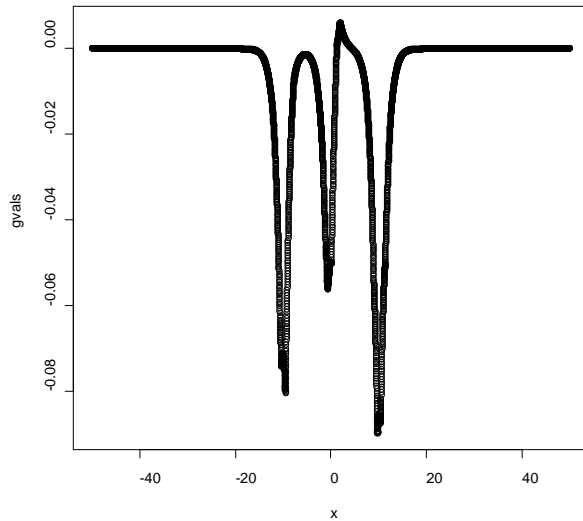
it takes 167.700000 seconds to generate the fourth Markov Chain

it takes 166.860000 seconds to generate the fifth Markov Chain

it takes 1386.410000 seconds to test the local acceptance

1

2.3.1.4 case 132 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 0.5$ with fixed bandwidth $b_n = 1$



Accepted 24965 out of 100000 (24.965%).

final beta = 0.330946

alpha(0.000000) is 0.238200

alpha(2.000000) is 0.473400

alpha(5.000000) is 0.976900

alpha(8.000000) is 0.389100

alpha(10.000000) is 0.174500

alpha(13.000000) is 0.311900

alpha(15.000000) is 0.397100

alpha(20.000000) is 0.426900

alpha(30.000000) is 0.431100

alpha(50.000000) is 0.425900

it takes 446.820000 seconds to run the adaptation algorithm

it takes 197.800000 seconds to compute g and sigma

it takes 166.480000 seconds to generate the first Markov Chain

it takes 166.300000 seconds to generate the second Markov Chain

it takes 167.630000 seconds to generate the third Markov Chain

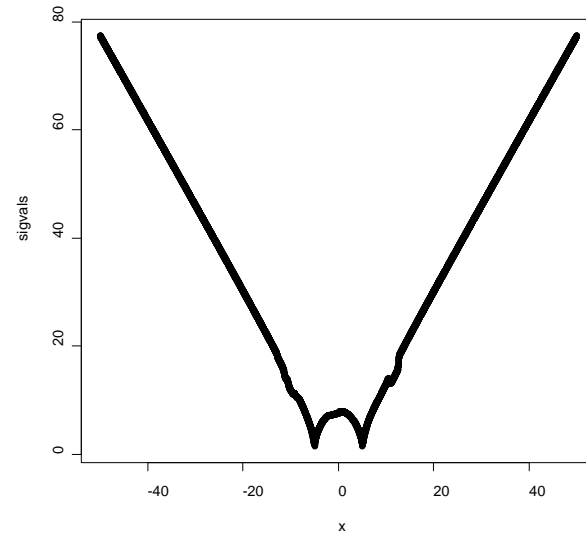
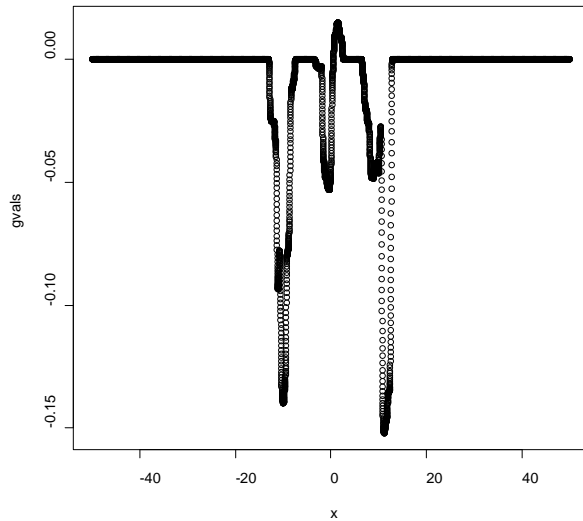
it takes 170.040000 seconds to generate the fourth Markov Chain

it takes 167.520000 seconds to generate the fifth Markov Chain

it takes 701.980000 seconds to test the local acceptance

1

2.3.1.5 case 131 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 1, \gamma = 0.5$ with fixed bandwidth $b_n = 1$



Accepted 24286 out of 100000 (24.286%).

final beta = 0.441691

alpha(0.000000) is 0.218800

alpha(2.000000) is 0.458700

alpha(5.000000) is 0.977800

alpha(8.000000) is 0.373500

alpha(10.000000) is 0.168400

alpha(13.000000) is 0.313600

alpha(15.000000) is 0.386900

alpha(20.000000) is 0.409000

alpha(30.000000) is 0.406700

alpha(50.000000) is 0.398200

it takes 776.670000 seconds to run the adaptation algorithm

it takes 347.250000 seconds to compute g and sigma

it takes 168.790000 seconds to generate the first Markov Chain

it takes 169.200000 seconds to generate the second Markov Chain

it takes 169.140000 seconds to generate the third Markov Chain

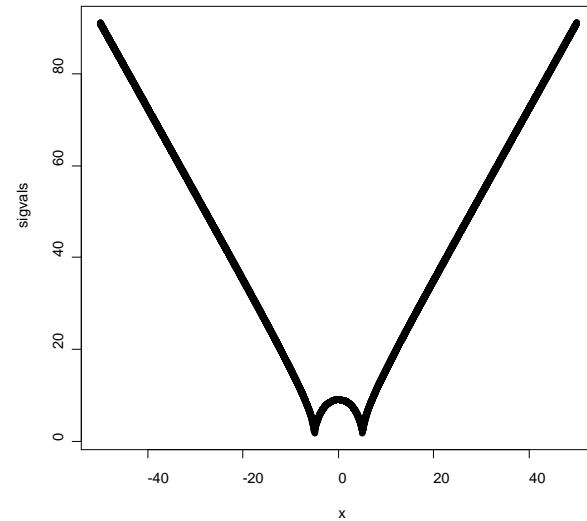
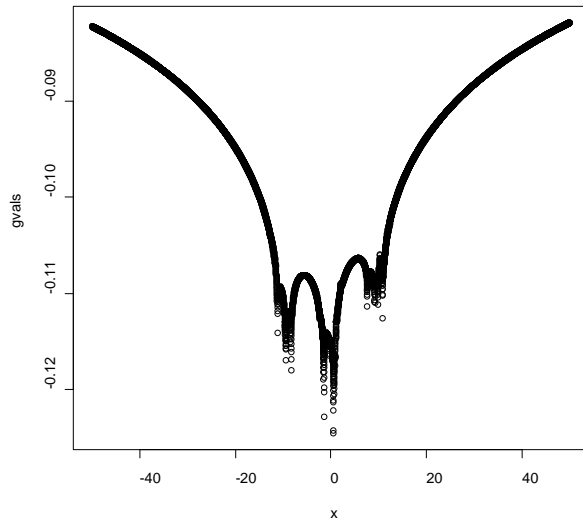
it takes 170.260000 seconds to generate the fourth Markov Chain

it takes 170.010000 seconds to generate the fifth Markov Chain

it takes 1136.300000 seconds to test the local acceptance

1

2.3.1.6 case 132 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 1, \gamma = 0.5$ with fixed bandwidth $b_n = 1$



Accepted 22621 out of 100000 (22.621%).

final beta = 0.687387

alpha(0.000000) is 0.187300

alpha(2.000000) is 0.435400

alpha(5.000000) is 0.983100

alpha(8.000000) is 0.348400

alpha(10.000000) is 0.155500

alpha(13.000000) is 0.290400

alpha(15.000000) is 0.359100

alpha(20.000000) is 0.373600

alpha(30.000000) is 0.361100

alpha(50.000000) is 0.370800

it takes 650.950000 seconds to run the adaptation algorithm

it takes 282.750000 seconds to compute g and sigma

it takes 177.640000 seconds to generate the first Markov Chain

it takes 178.130000 seconds to generate the second Markov Chain

it takes 178.750000 seconds to generate the third Markov Chain

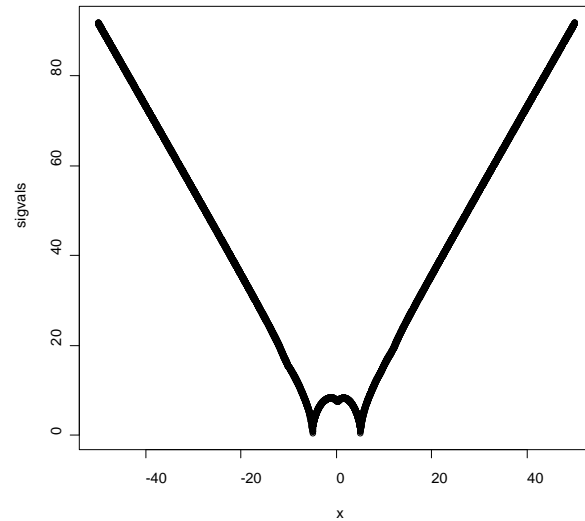
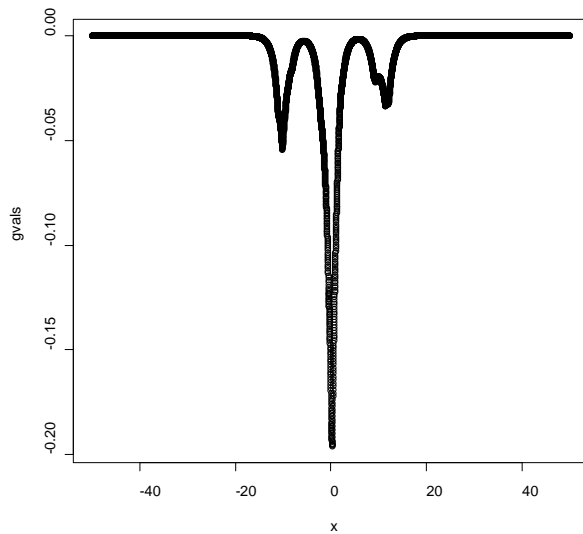
it takes 178.560000 seconds to generate the fourth Markov Chain

it takes 178.550000 seconds to generate the fifth Markov Chain

it takes 1000.330000 seconds to test the local acceptance

1

2.3.1.7 case 133 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 10, \gamma = 0.5$ with fixed bandwidth $b_n = 1$



Accepted 22575 out of 100000 (22.575%).

final beta = -0.538530

alpha(0.000000) is 0.207800

alpha(2.000000) is 0.433300

alpha(5.000000) is 0.696900

alpha(8.000000) is 0.341900

alpha(10.000000) is 0.166300

alpha(13.000000) is 0.286300

alpha(15.000000) is 0.354600

alpha(20.000000) is 0.365400

alpha(30.000000) is 0.367900

alpha(50.000000) is 0.357700

it takes 447.840000 seconds to run the adaptation algorithm

it takes 200.430000 seconds to compute g and sigma

it takes 175.050000 seconds to generate the first Markov Chain

it takes 174.760000 seconds to generate the second Markov Chain

it takes 174.250000 seconds to generate the third Markov Chain

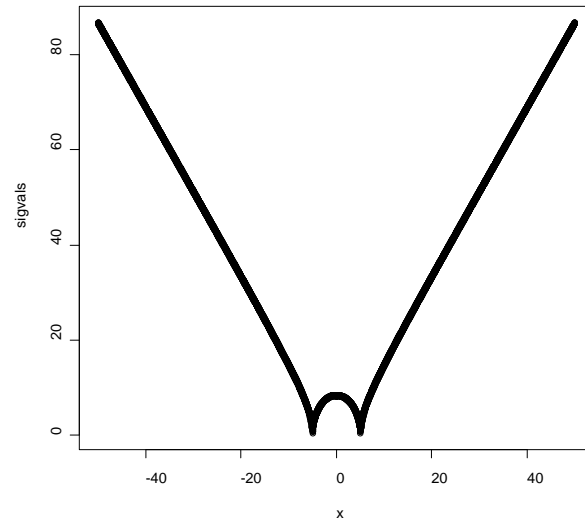
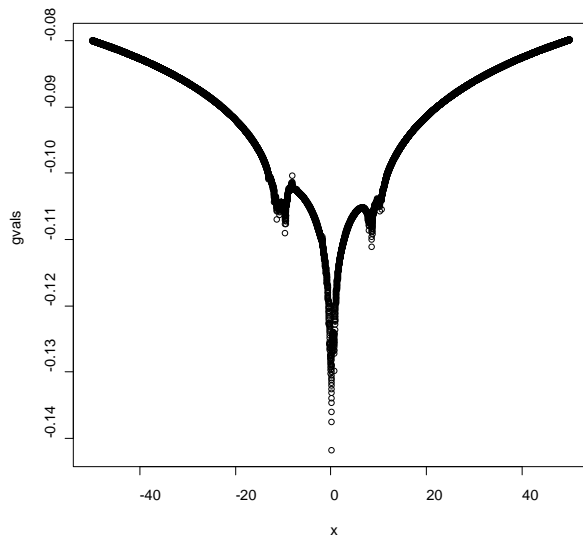
it takes 174.060000 seconds to generate the fourth Markov Chain

it takes 174.670000 seconds to generate the fifth Markov Chain

it takes 761.780000 seconds to test the local acceptance

1

2.3.1.8 case 134 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 10, \gamma = 0.5$ with fixed bandwidth $b_n = 1$



Accepted 22849 out of 100000 (22.849%).

final beta = -0.517135

alpha(0.000000) is 0.203900

alpha(2.000000) is 0.448400

alpha(5.000000) is 0.684000

alpha(8.000000) is 0.364200

alpha(10.000000) is 0.161600

alpha(13.000000) is 0.296000

alpha(15.000000) is 0.367600

alpha(20.000000) is 0.380500

alpha(30.000000) is 0.377800

alpha(50.000000) is 0.370000

it takes 649.150000 seconds to run the adaptation algorithm

it takes 283.370000 seconds to compute g and sigma

it takes 174.430000 seconds to generate the first Markov Chain

it takes 174.900000 seconds to generate the second Markov Chain

it takes 174.820000 seconds to generate the third Markov Chain

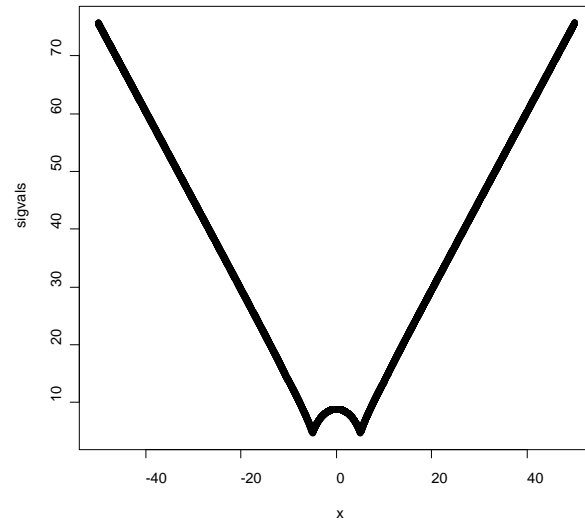
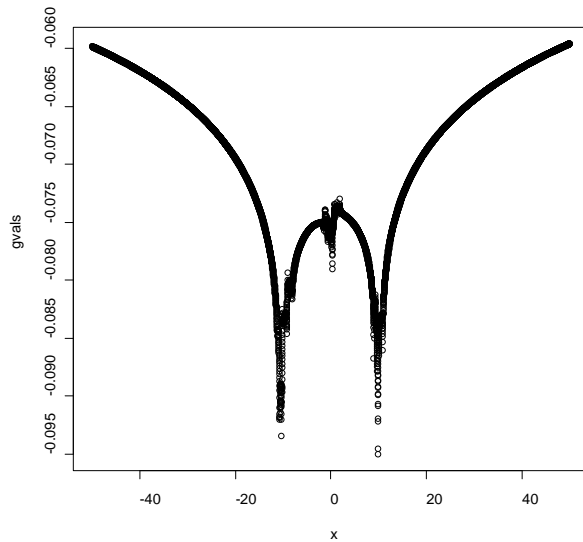
it takes 176.090000 seconds to generate the fourth Markov Chain

it takes 176.120000 seconds to generate the fifth Markov Chain

it takes 989.210000 seconds to test the local acceptance

1

2.3.1.9 case 135 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 0.1, \gamma = 0.5$ with fixed bandwidth $b_n = 1$



Accepted 23337 out of 100000 (23.337%).

final beta = 1.628756

alpha(0.000000) is 0.206800

alpha(2.000000) is 0.429500

alpha(5.000000) is 0.983000

alpha(8.000000) is 0.358700

alpha(10.000000) is 0.175500

alpha(13.000000) is 0.313000

alpha(15.000000) is 0.411500

alpha(20.000000) is 0.411400

alpha(30.000000) is 0.407100

alpha(50.000000) is 0.409500

it takes 232.112000 seconds to run the adaptation algorithm

it takes 102.358000 seconds to compute g and sigma

it takes 21.231000 seconds to generate the first Markov Chain

it takes 20.655000 seconds to generate the second Markov Chain

it takes 21.185000 seconds to generate the third Markov Chain

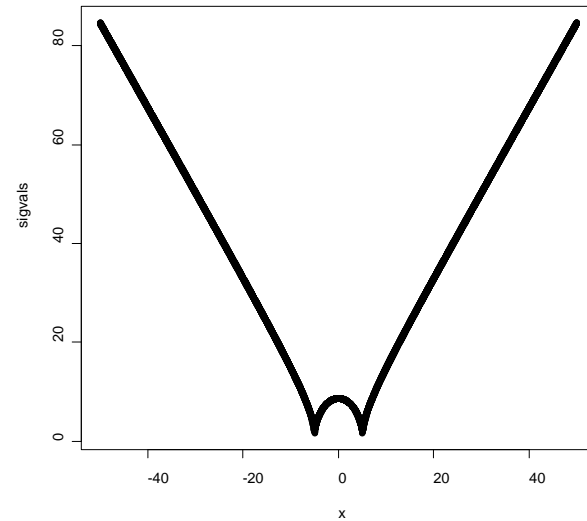
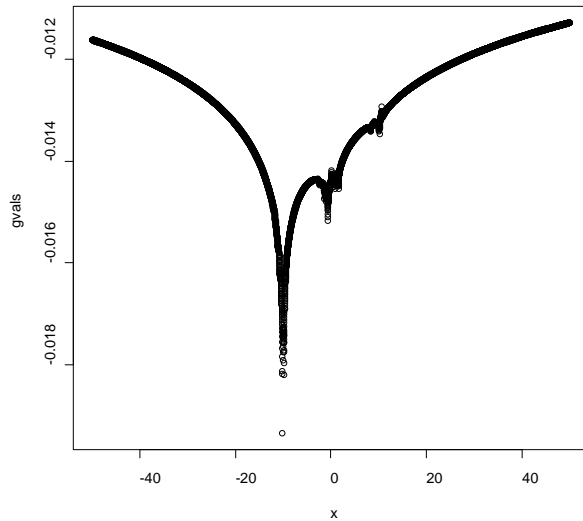
it takes 22.052000 seconds to generate the fourth Markov Chain

it takes 22.464000 seconds to generate the fifth Markov Chain

it takes 302.099000 seconds to test the local acceptance

1

2.3.1.10 case 136 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 0.1, \gamma = 0.5$ with fixed bandwidth $b_n = 10$



Accepted 22834 out of 100000 (22.834%).

final beta = 0.542365

alpha(0.000000) is 0.203200

alpha(2.000000) is 0.442500

alpha(5.000000) is 0.984500

alpha(8.000000) is 0.351700

alpha(10.000000) is 0.167100

alpha(13.000000) is 0.296200

alpha(15.000000) is 0.366500

alpha(20.000000) is 0.392700

alpha(30.000000) is 0.379800

alpha(50.000000) is 0.378700

it takes 640.290000 seconds to run the adaptation algorithm

it takes 283.020000 seconds to compute g and sigma

it takes 175.850000 seconds to generate the first Markov Chain

it takes 177.050000 seconds to generate the second Markov Chain

it takes 175.730000 seconds to generate the third Markov Chain

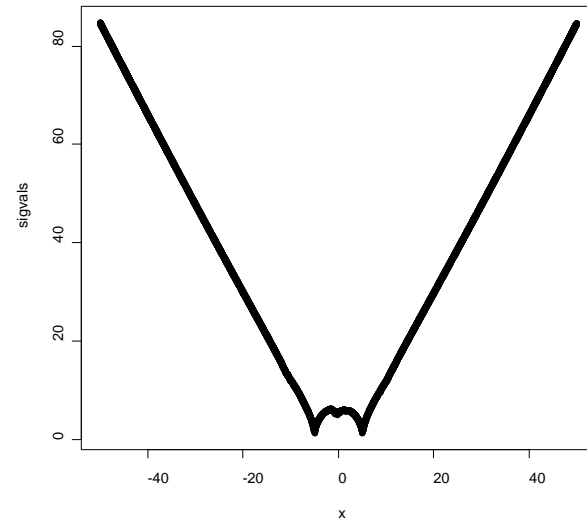
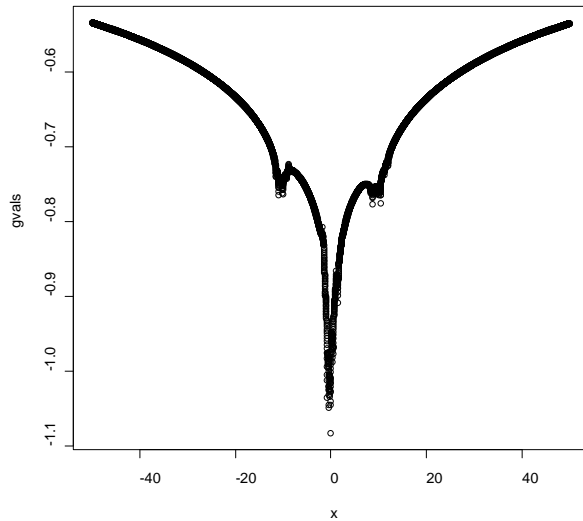
it takes 176.160000 seconds to generate the fourth Markov Chain

it takes 175.780000 seconds to generate the fifth Markov Chain

it takes 984.570000 seconds to test the local acceptance

1

2.3.1.11 case 137 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 0.1, \gamma = 0.5$ with fixed bandwidth $b_n = 0.1$



Accepted 24776 out of 100000 (24.776%).

final beta = 1.066797

alpha(0.000000) is 0.255000

alpha(2.000000) is 0.473500

alpha(5.000000) is 0.983600

alpha(8.000000) is 0.387300

alpha(10.000000) is 0.153900

alpha(13.000000) is 0.305800

alpha(15.000000) is 0.392600

alpha(20.000000) is 0.409300

alpha(30.000000) is 0.385600

alpha(50.000000) is 0.380900

it takes 235.762000 seconds to run the adaptation algorithm

it takes 101.070000 seconds to compute g and sigma

it takes 20.240000 seconds to generate the first Markov Chain

it takes 20.960000 seconds to generate the second Markov Chain

it takes 20.410000 seconds to generate the third Markov Chain

it takes 20.560000 seconds to generate the fourth Markov Chain

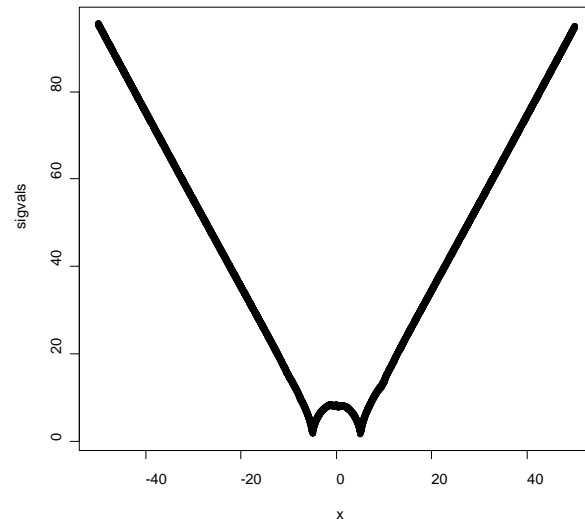
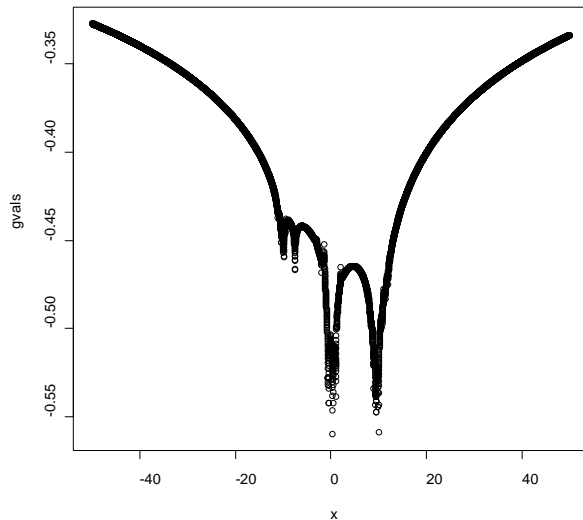
it takes 20.140000 seconds to generate the fifth Markov Chain

it takes 300.521000 seconds to test the local acceptance

1

2.3.1.12 case 138 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 0.1, \gamma = 0.5$ with decreasing bandwidth

$$b_n = \frac{1}{n^{0.2}}$$



Accepted 23303 out of 100000 (23.303%).

final beta = 0.979695

alpha(0.000000) is 0.207000

alpha(2.000000) is 0.447200

alpha(5.000000) is 0.986800

alpha(8.000000) is 0.363500

alpha(10.000000) is 0.163200

alpha(13.000000) is 0.295000

alpha(15.000000) is 0.365900

alpha(20.000000) is 0.375900

alpha(30.000000) is 0.371600

alpha(50.000000) is 0.346100

it takes 240.848000 seconds to run the adaptation algorithm

it takes 109.387000 seconds to compute g and sigma

it takes 24.340000 seconds to generate the first Markov Chain

it takes 24.380000 seconds to generate the second Markov Chain

it takes 24.550000 seconds to generate the third Markov Chain

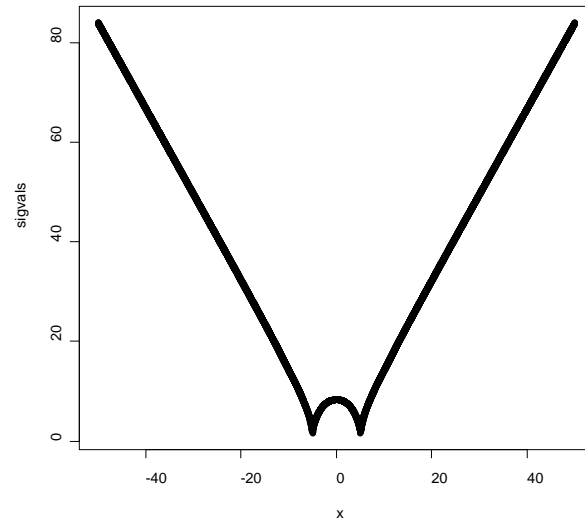
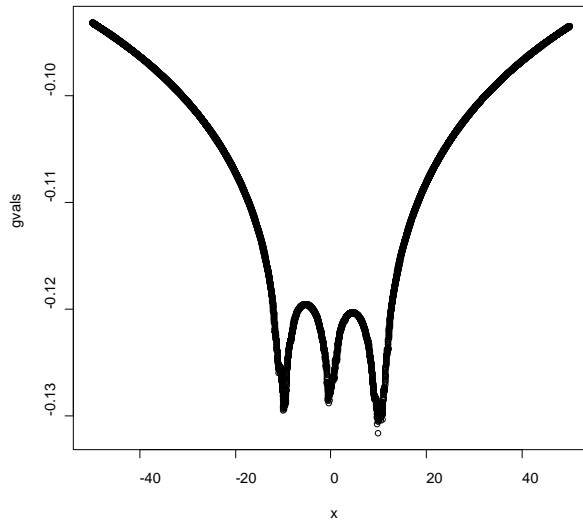
it takes 24.620000 seconds to generate the fourth Markov Chain

it takes 24.690000 seconds to generate the fifth Markov Chain

it takes 336.289000 seconds to test the local acceptance

1

2.3.1.13 case 139 $\eta_n = \frac{1}{(n+5)^{0.8}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 1, \gamma = 0.5$ with fixed bandwidth $b_n = 1$



Accepted 23368 out of 100000 (23.368%).

final beta = 0.616456

alpha(0.000000) is 0.203600

alpha(2.000000) is 0.443700

alpha(5.000000) is 0.986100

alpha(8.000000) is 0.365900

alpha(10.000000) is 0.164400

alpha(13.000000) is 0.301400

alpha(15.000000) is 0.384300

alpha(20.000000) is 0.399100

alpha(30.000000) is 0.388300

alpha(50.000000) is 0.382800

it takes 232.327000 seconds to run the adaptation algorithm

it takes 100.786000 seconds to compute g and sigma

it takes 24.283000 seconds to generate the first Markov Chain

it takes 21.371000 seconds to generate the second Markov Chain

it takes 21.644000 seconds to generate the third Markov Chain

it takes 22.590000 seconds to generate the fourth Markov Chain

it takes 21.119000 seconds to generate the fifth Markov Chain

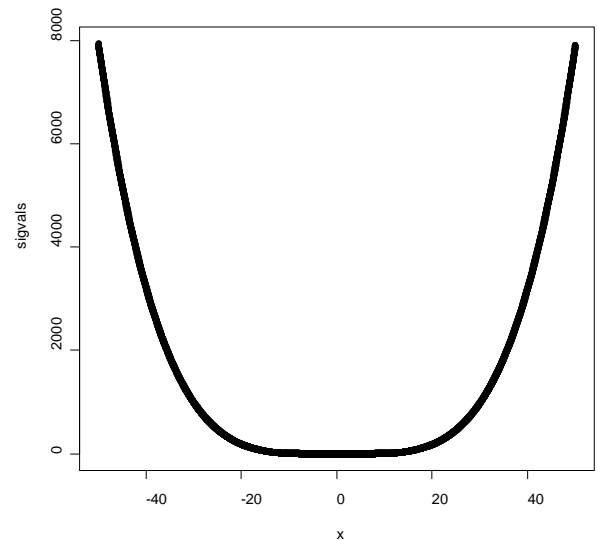
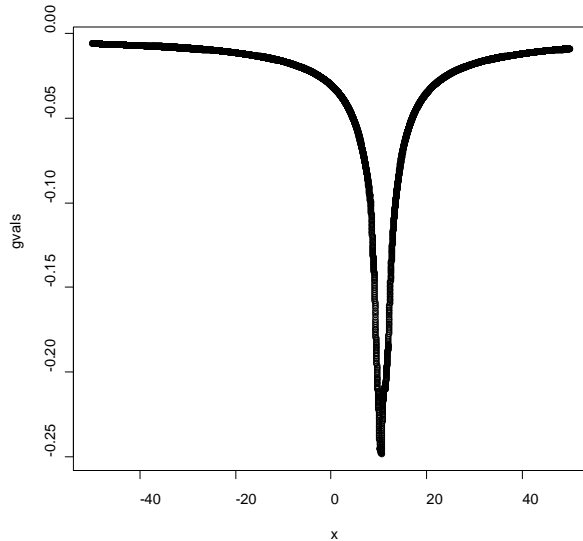
it takes 290.380000 seconds to test the local acceptance

1

[1] 13.34282
[1] 0.09514207
[1] 17.27245

2.3.2 kernel function $K(x) = \frac{1}{1 + \alpha_1 |x|^{\alpha_2}}$

2.3.2.1 case 140 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 74753 out of 100000 (74.753%).

final beta = -6.643285

alpha(0.000000) is 0.751500

alpha(2.000000) is 0.723000

alpha(5.000000) is 0.956800

alpha(8.000000) is 0.597100

alpha(10.000000) is 0.175300

alpha(13.000000) is 0.129200

alpha(15.000000) is 0.103600

alpha(20.000000) is 0.056700

alpha(30.000000) is 0.016700

alpha(50.000000) is 0.003300

it takes 357.200000 seconds to run the adaptation algorithm

it takes 156.500000 seconds to compute g and sigma

it takes 168.160000 seconds to generate the first Markov Chain

it takes 168.450000 seconds to generate the second Markov Chain

it takes 166.270000 seconds to generate the third Markov Chain

it takes 167.860000 seconds to generate the fourth Markov Chain

it takes 166.480000 seconds to generate the fifth Markov Chain

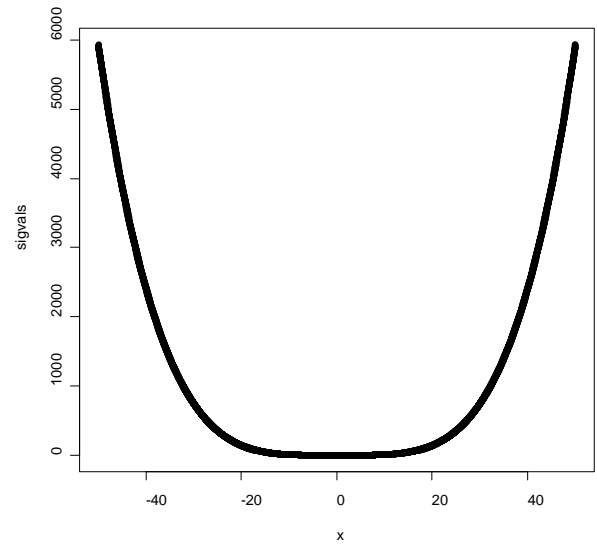
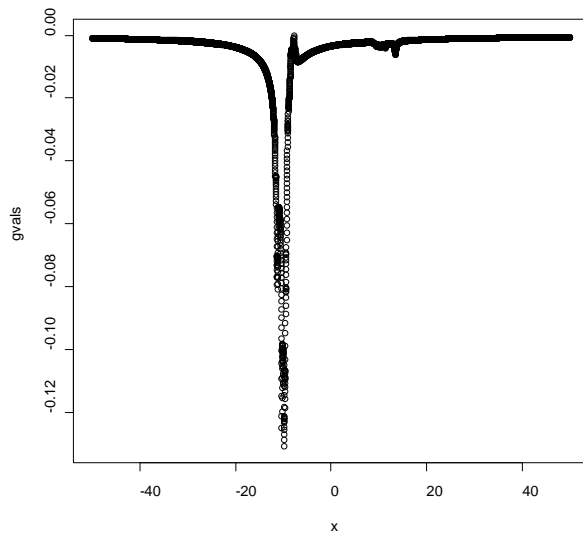
it takes 893.900000 seconds to test the local acceptance

1

[1] 13.66704
[1] 0.01207831
[1] 0.3014526

2.3.2.2 case 141 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth

$b_n = 1$



Accepted 24059 out of 100000 (24.059%).

final beta = -6.939904

alpha(0.000000) is 0.813200

alpha(2.000000) is 0.753900

alpha(5.000000) is 0.954500

alpha(8.000000) is 0.617100

alpha(10.000000) is 0.191500

alpha(13.000000) is 0.134500

alpha(15.000000) is 0.126900

alpha(20.000000) is 0.065300

alpha(30.000000) is 0.023900

alpha(50.000000) is 0.005600

it takes 357.490000 seconds to run the adaptation algorithm

it takes 156.390000 seconds to compute g and sigma

it takes 171.120000 seconds to generate the first Markov Chain

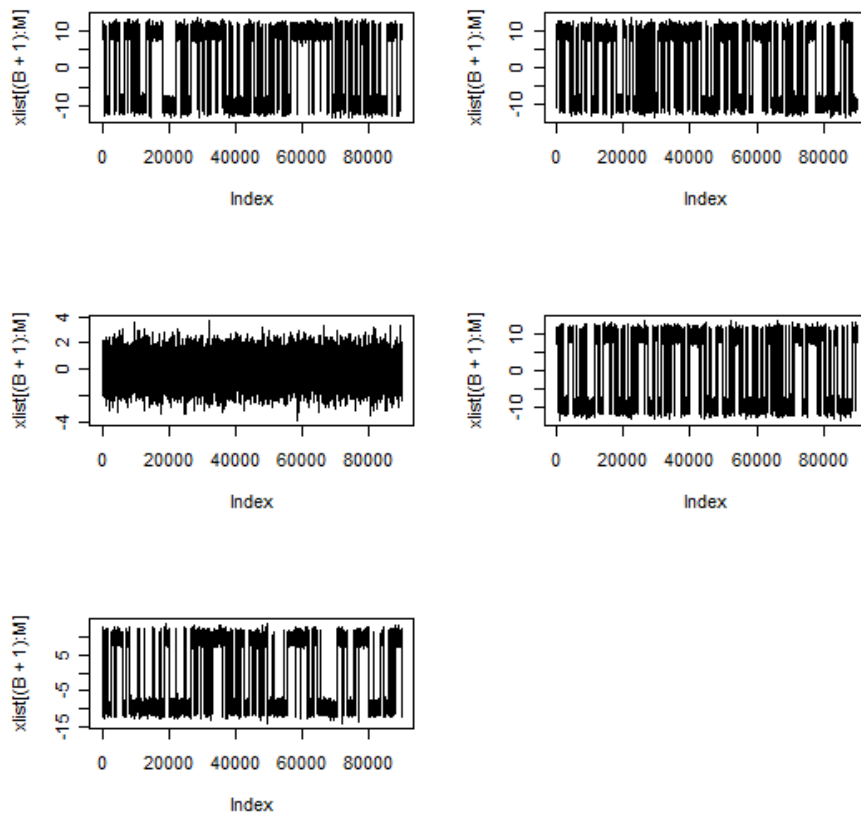
it takes 166.660000 seconds to generate the second Markov Chain

it takes 166.270000 seconds to generate the third Markov Chain

it takes 167.590000 seconds to generate the fourth Markov Chain

it takes 164.220000 seconds to generate the fifth Markov Chain

it takes 862.580000 seconds to test the local acceptance



```

> source("xlist1");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 90.40186
[1] 0.3162226
[1] 1.229918
> source("xlist2");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 89.71504
[1] 0.3175898
[1] 1.441011
> source("xlist3");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 19.61744
[1] 0.01470637
[1] 0.2134324
> source("xlist4");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 90.32034
[1] 0.3185251
[1] 1.313225
> source("xlist5");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /

```

```
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
```

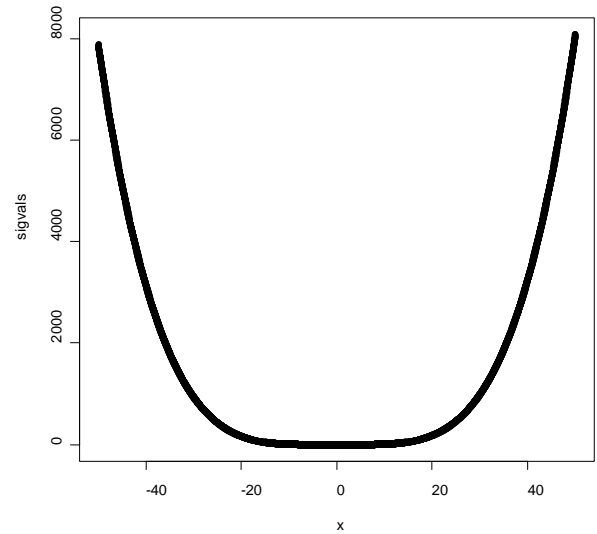
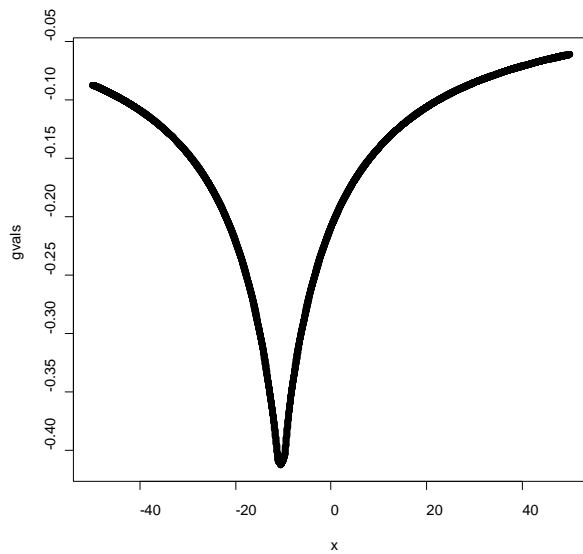
```
[1] 91.49129
```

```
[1] 0.3193592
```

```
[1] 1.163729
```

2.3.2.3 case 142 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth

$b_n = 1$



Accepted 21928 out of 100000 (21.928%).

final beta = -6.569201

alpha(0.000000) is 0.776600

alpha(2.000000) is 0.722100

alpha(5.000000) is 0.956800

alpha(8.000000) is 0.590700

alpha(10.000000) is 0.151900

alpha(13.000000) is 0.113300

alpha(15.000000) is 0.104100

alpha(20.000000) is 0.050200

alpha(30.000000) is 0.018000

alpha(50.000000) is 0.003600

it takes 350.290000 seconds to run the adaptation algorithm

it takes 154.400000 seconds to compute g and sigma

it takes 167.000000 seconds to generate the first Markov Chain

it takes 165.600000 seconds to generate the second Markov Chain

it takes 163.820000 seconds to generate the third Markov Chain

it takes 166.220000 seconds to generate the fourth Markov Chain

it takes 169.510000 seconds to generate the fifth Markov Chain

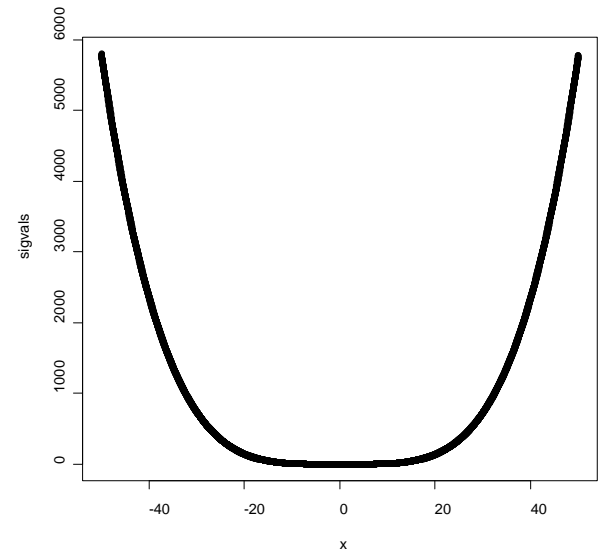
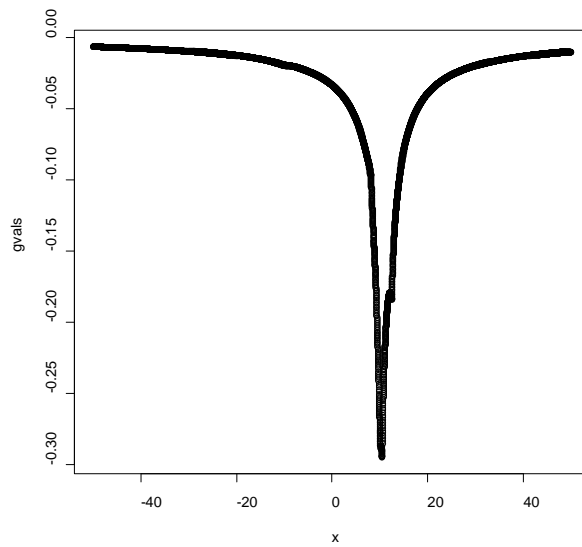
it takes 886.600000 seconds to test the local acceptance

1

[1] 88.28712
[1] 0.3145201
[1] 1.458424

2.3.2.4 case 143 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$b_n = 1$



Accepted 21960 out of 100000 (21.960%).

final beta = -2.358082

alpha(0.000000) is 0.653400

alpha(2.000000) is 0.683000

alpha(5.000000) is 0.981500

alpha(8.000000) is 0.573800

alpha(10.000000) is 0.187400

alpha(13.000000) is 0.148500

alpha(15.000000) is 0.124500

alpha(20.000000) is 0.071500

alpha(30.000000) is 0.023900

alpha(50.000000) is 0.006600

it takes 350.510000 seconds to run the adaptation algorithm

it takes 154.900000 seconds to compute g and sigma

it takes 164.410000 seconds to generate the first Markov Chain

it takes 166.610000 seconds to generate the second Markov Chain

it takes 167.720000 seconds to generate the third Markov Chain

it takes 166.330000 seconds to generate the fourth Markov Chain

it takes 168.090000 seconds to generate the fifth Markov Chain

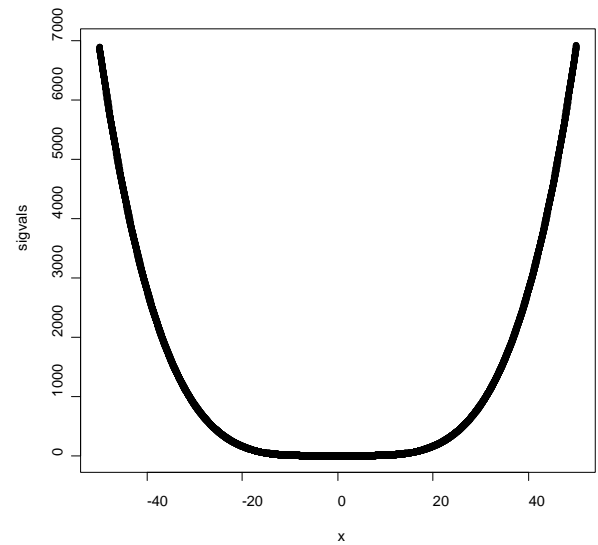
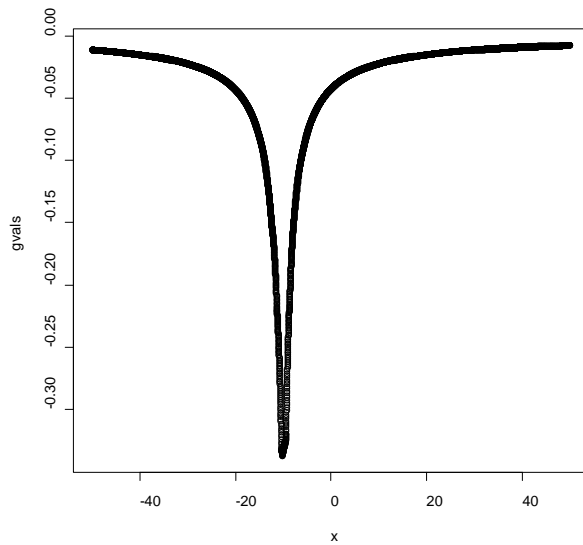
it takes 851.800000 seconds to test the local acceptance

1

[1] 90.71062
[1] 0.3180162
[1] 1.260599

2.3.2.5 case 144 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 10, \gamma = 2$ with fixed bandwidth

$b_n = 1$



Accepted 23476 out of 100000 (23.476%).

final beta = -11.382114

alpha(0.000000) is 0.806700

alpha(2.000000) is 0.745700

alpha(5.000000) is 0.713100

alpha(8.000000) is 0.611800

alpha(10.000000) is 0.161700

alpha(13.000000) is 0.118300

alpha(15.000000) is 0.104900

alpha(20.000000) is 0.057000

alpha(30.000000) is 0.021400

alpha(50.000000) is 0.004700

it takes 356.180000 seconds to run the adaptation algorithm

it takes 156.340000 seconds to compute g and sigma

it takes 163.020000 seconds to generate the first Markov Chain

it takes 164.080000 seconds to generate the second Markov Chain

it takes 161.600000 seconds to generate the third Markov Chain

it takes 164.910000 seconds to generate the fourth Markov Chain

it takes 168.950000 seconds to generate the fifth Markov Chain

it takes 884.960000 seconds to test the local acceptance

1

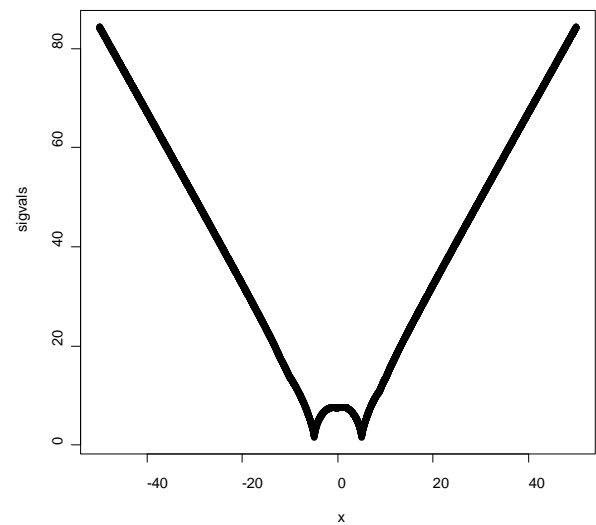
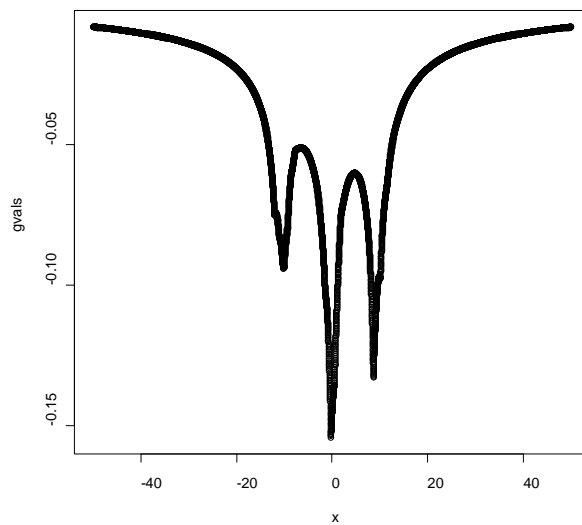
```

> source("xlist5");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 89.95243
[1] 0.3179866
[1] 1.358456

```

2.3.2.6 case 145 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 0.5$ with fixed bandwidth

$b_n = 1$



Accepted 23749 out of 100000 (23.749%).

final beta = 0.535915

alpha(0.000000) is 0.215100

alpha(2.000000) is 0.457000

alpha(5.000000) is 0.980300

alpha(8.000000) is 0.371700

alpha(10.000000) is 0.161000

alpha(13.000000) is 0.310200

alpha(15.000000) is 0.366000

alpha(20.000000) is 0.391400

alpha(30.000000) is 0.383000

alpha(50.000000) is 0.372500

it takes 356.300000 seconds to run the adaptation algorithm

it takes 156.880000 seconds to compute g and sigma

it takes 170.430000 seconds to generate the first Markov Chain

it takes 169.350000 seconds to generate the second Markov Chain

it takes 168.660000 seconds to generate the third Markov Chain

it takes 169.640000 seconds to generate the fourth Markov Chain

it takes 168.940000 seconds to generate the fifth Markov Chain

it takes 624.960000 seconds to test the local acceptance

|

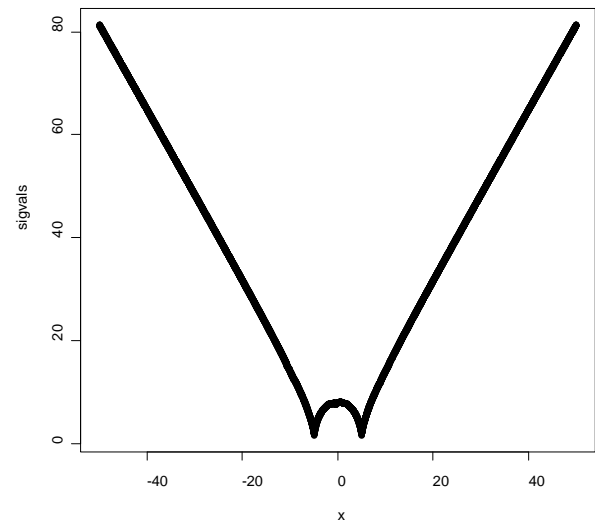
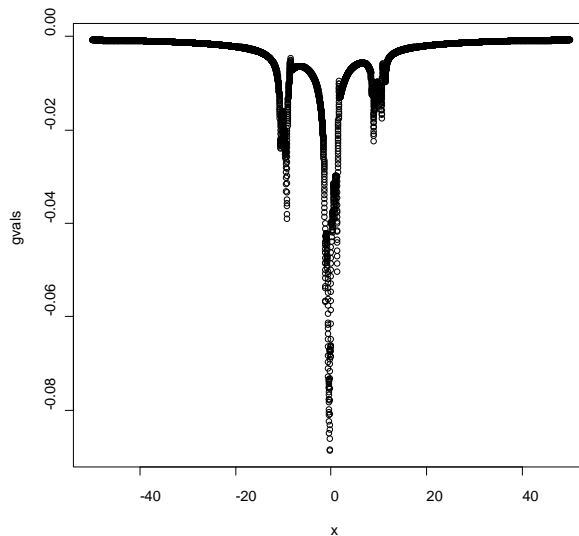
```

> source("xlist5");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 14.27748
[1] 0.09757993
[1] 16.54765

```

2.3.2.7 case 146 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 1, \gamma = 0.5$ with fixed bandwidth

$b_n = 1$



Accepted 23602 out of 100000 (23.602%).

final beta = 0.491872

alpha(0.000000) is 0.205200

alpha(2.000000) is 0.461500

alpha(5.000000) is 0.981800

alpha(8.000000) is 0.360800

alpha(10.000000) is 0.163000

alpha(13.000000) is 0.301700

alpha(15.000000) is 0.375700

alpha(20.000000) is 0.390900

alpha(30.000000) is 0.383200

alpha(50.000000) is 0.380400

it takes 356.260000 seconds to run the adaptation algorithm

it takes 157.310000 seconds to compute g and sigma

it takes 170.510000 seconds to generate the first Markov Chain

it takes 169.670000 seconds to generate the second Markov Chain

it takes 169.950000 seconds to generate the third Markov Chain

it takes 170.300000 seconds to generate the fourth Markov Chain

it takes 169.670000 seconds to generate the fifth Markov Chain

it takes 619.850000 seconds to test the local acceptance

|

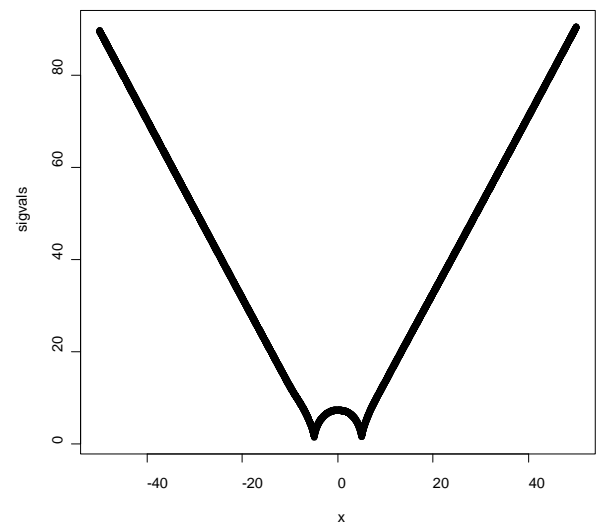
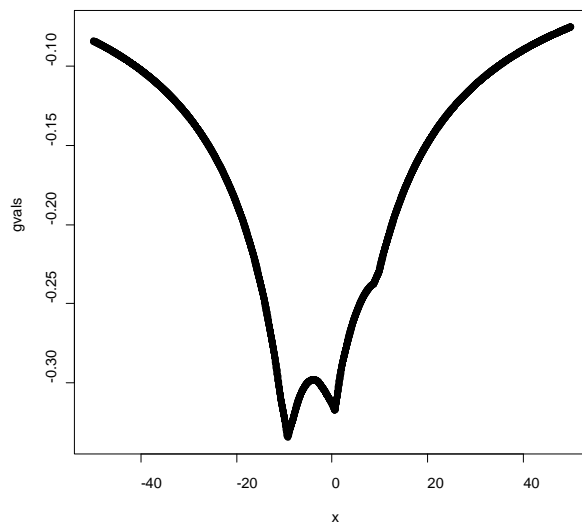
```

> source("xlist5");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 12.43203
[1] 0.09186996
[1] 17.23872

```

2.3.2.8 case 147 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.1, \alpha_2 = 1, C = 1, \gamma = 0.5$ with fixed bandwidth

$b_n = 1$



Accepted 24104 out of 100000 (24.104%).

final beta = 0.672420

alpha(0.000000) is 0.219700

alpha(2.000000) is 0.474000

alpha(5.000000) is 0.985900

alpha(8.000000) is 0.374900

alpha(10.000000) is 0.157300

alpha(13.000000) is 0.307600

alpha(15.000000) is 0.369800

alpha(20.000000) is 0.379100

alpha(30.000000) is 0.373500

alpha(50.000000) is 0.361500

it takes 187.283000 seconds to run the adaptation algorithm

it takes 82.121000 seconds to compute g and sigma

it takes 20.090000 seconds to generate the first Markov Chain

it takes 20.182000 seconds to generate the second Markov Chain

it takes 20.524000 seconds to generate the third Markov Chain

it takes 20.467000 seconds to generate the fourth Markov Chain

it takes 20.692000 seconds to generate the fifth Markov Chain

it takes 249.071000 seconds to test the local acceptance

|

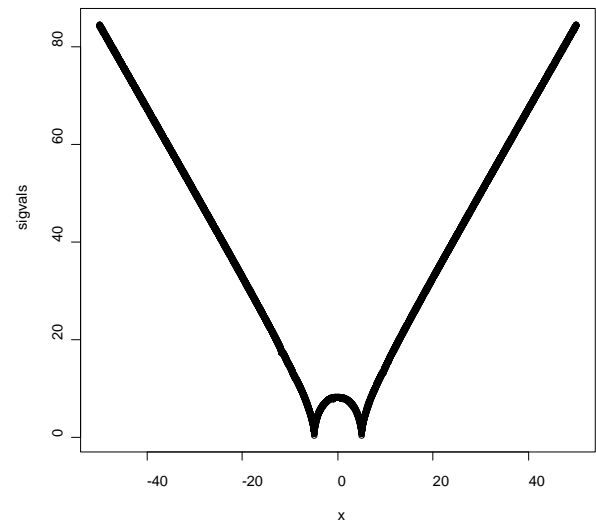
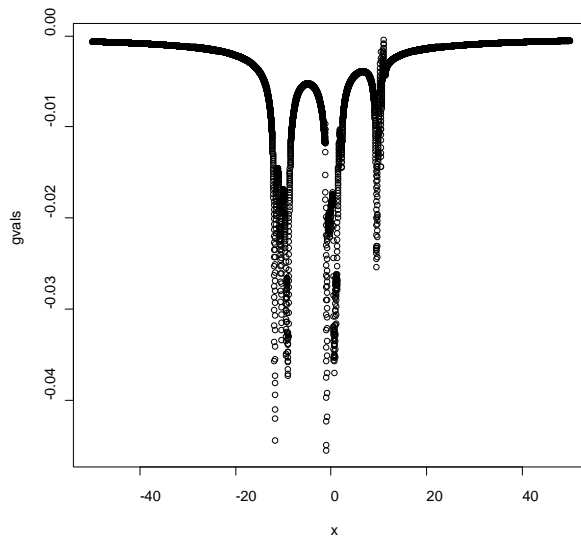
```

> source("xlist5");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 14.78932
[1] 0.09995486
[1] 16.03785

```

2.3.2.9 case 148 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 10, \gamma = 0.5$ with fixed bandwidth

$b_n = 1$



Accepted 22987 out of 100000 (22.987%).

final beta = -0.620667

alpha(0.000000) is 0.209300

alpha(2.000000) is 0.449600

alpha(5.000000) is 0.679100

alpha(8.000000) is 0.361700

alpha(10.000000) is 0.167800

alpha(13.000000) is 0.298600

alpha(15.000000) is 0.364600

alpha(20.000000) is 0.388100

alpha(30.000000) is 0.380300

alpha(50.000000) is 0.387100

it takes 357.170000 seconds to run the adaptation algorithm

it takes 156.510000 seconds to compute g and sigma

it takes 170.650000 seconds to generate the first Markov Chain

it takes 170.480000 seconds to generate the second Markov Chain

it takes 170.280000 seconds to generate the third Markov Chain

it takes 171.030000 seconds to generate the fourth Markov Chain

it takes 170.120000 seconds to generate the fifth Markov Chain

it takes 621.790000 seconds to test the local acceptance

|

```
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M] ) );asjd(xlist[(B+1):M]);
```

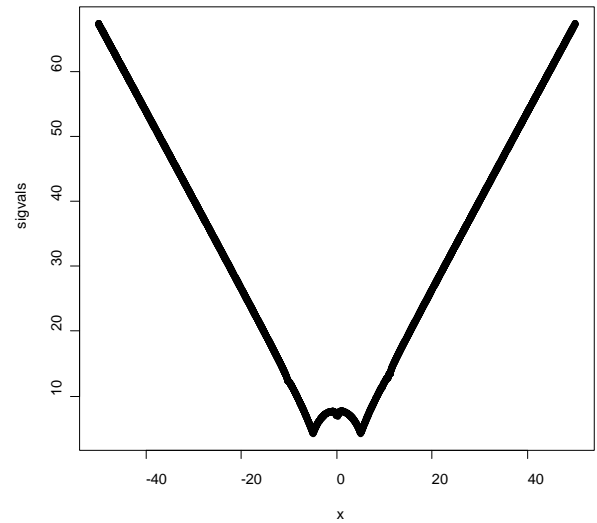
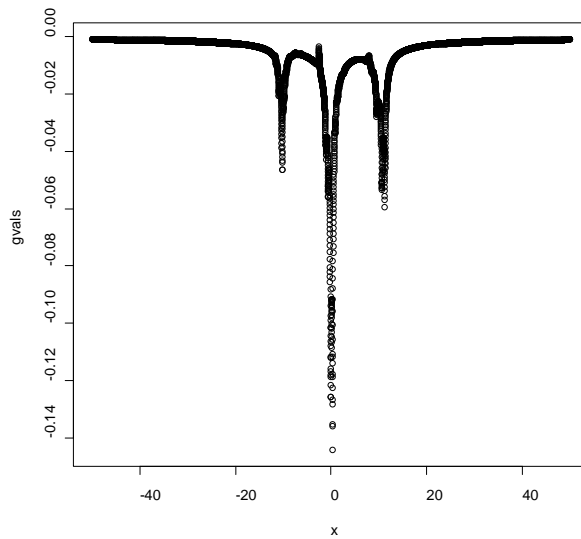
```
[1] 13.72235
```

```
[1] 0.09650097
```

```
[1] 17.49019
```

2.3.2.10 case 149 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 0.1, \gamma = 0.5$ with fixed bandwidth

$b_n = 1$



Accepted 24399 out of 100000 (24.399%).

final beta = 1.453206

alpha(0.000000) is 0.224300

alpha(2.000000) is 0.455900

alpha(5.000000) is 0.993000

alpha(8.000000) is 0.378800

alpha(10.000000) is 0.174700

alpha(13.000000) is 0.326800

alpha(15.000000) is 0.426700

alpha(20.000000) is 0.438900

alpha(30.000000) is 0.429700

alpha(50.000000) is 0.440100

it takes 352.330000 seconds to run the adaptation algorithm

it takes 154.950000 seconds to compute g and sigma

it takes 167.720000 seconds to generate the first Markov Chain

it takes 167.820000 seconds to generate the second Markov Chain

it takes 167.570000 seconds to generate the third Markov Chain

it takes 166.890000 seconds to generate the fourth Markov Chain

it takes 166.760000 seconds to generate the fifth Markov Chain

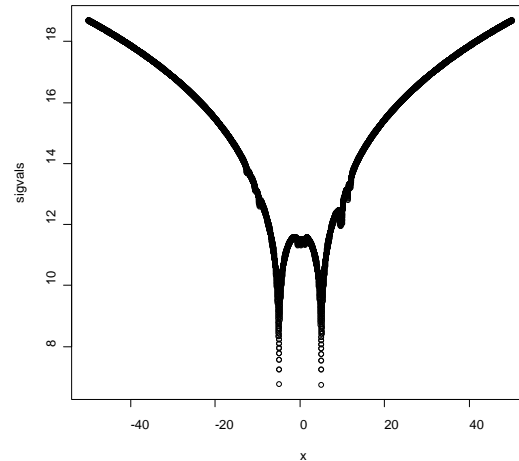
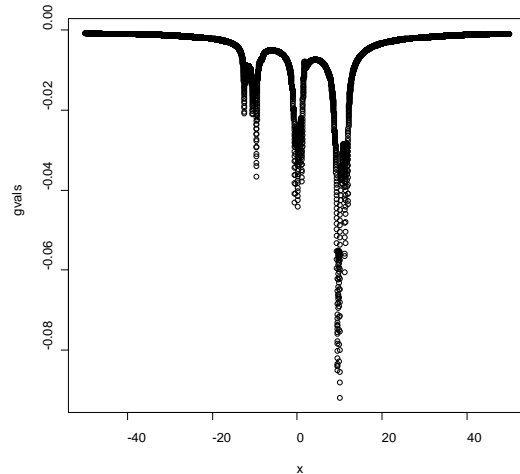
it takes 580.080000 seconds to test the local acceptance

1

[1] 14.91846
 [1] 0.1007374
 [1] 15.86291

2.3.2.11 case 150 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 10, \gamma = 0.1$ with fixed bandwidth

$b_n = 1$



Accepted 22156 out of 100000 (22.156%).

final beta = 1.917426

alpha(0.000000) is 0.170300

alpha(2.000000) is 0.378600

alpha(5.000000) is 0.930700

alpha(8.000000) is 0.344400

alpha(10.000000) is 0.172300

alpha(13.000000) is 0.358100

alpha(15.000000) is 0.487300

alpha(20.000000) is 0.500900

alpha(30.000000) is 0.501700

alpha(50.000000) is 0.493700

it takes 353.150000 seconds to run the adaptation algorithm

it takes 155.440000 seconds to compute g and sigma

it takes 167.430000 seconds to generate the first Markov Chain

it takes 167.340000 seconds to generate the second Markov Chain

it takes 168.300000 seconds to generate the third Markov Chain

it takes 168.280000 seconds to generate the fourth Markov Chain

it takes 168.090000 seconds to generate the fifth Markov Chain

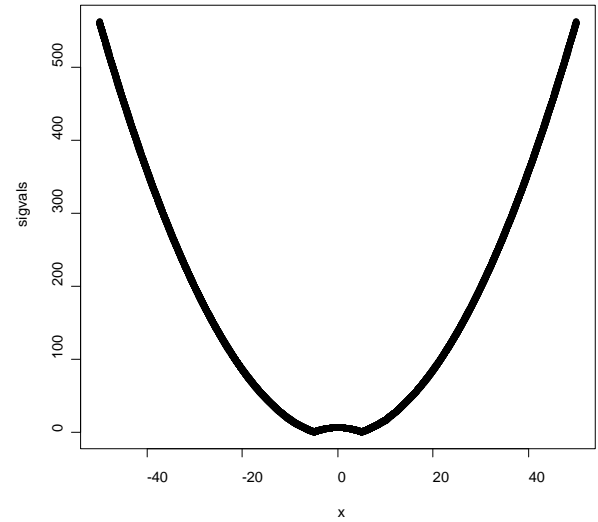
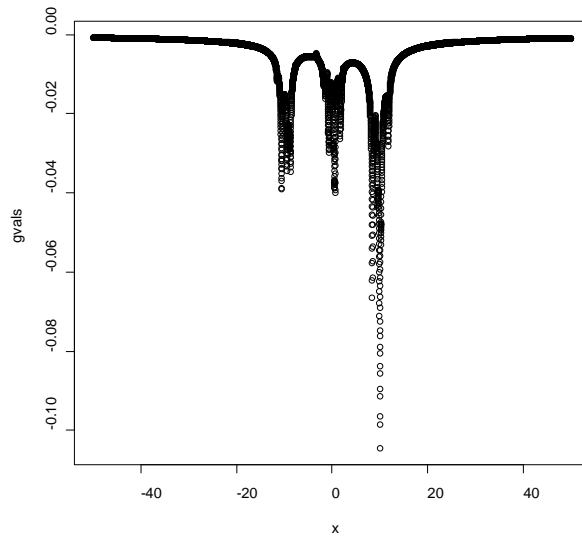
it takes 525.460000 seconds to test the local acceptance

1

[1] 13.31069
[1] 0.09509448
[1] 17.21339

2.3.2.12 case 151 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 10, \gamma = 1$ with fixed bandwidth

$b_n = 1$



Accepted 23422 out of 100000 (23.422%).

final beta = -3.783332

alpha(0.000000) is 0.253600

alpha(2.000000) is 0.486500

alpha(5.000000) is 0.645400

alpha(8.000000) is 0.368100

alpha(10.000000) is 0.137900

alpha(13.000000) is 0.200000

alpha(15.000000) is 0.203000

alpha(20.000000) is 0.171300

alpha(30.000000) is 0.113100

alpha(50.000000) is 0.067000

it takes 358.220000 seconds to run the adaptation algorithm

it takes 157.160000 seconds to compute g and sigma

it takes 182.650000 seconds to generate the first Markov Chain

it takes 184.390000 seconds to generate the second Markov Chain

it takes 182.440000 seconds to generate the third Markov Chain

it takes 182.340000 seconds to generate the fourth Markov Chain

it takes 181.730000 seconds to generate the fifth Markov Chain

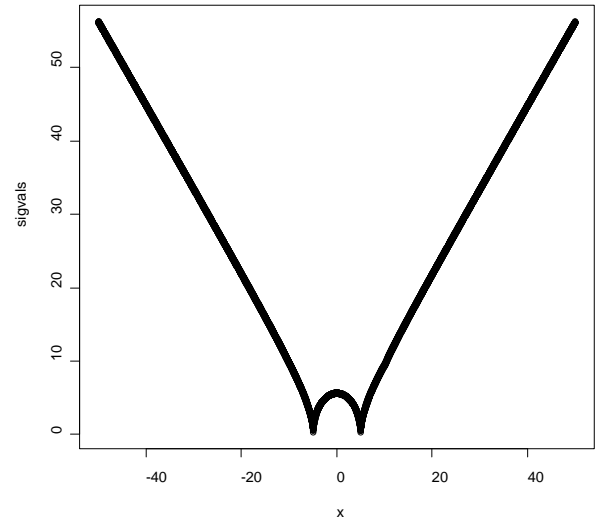
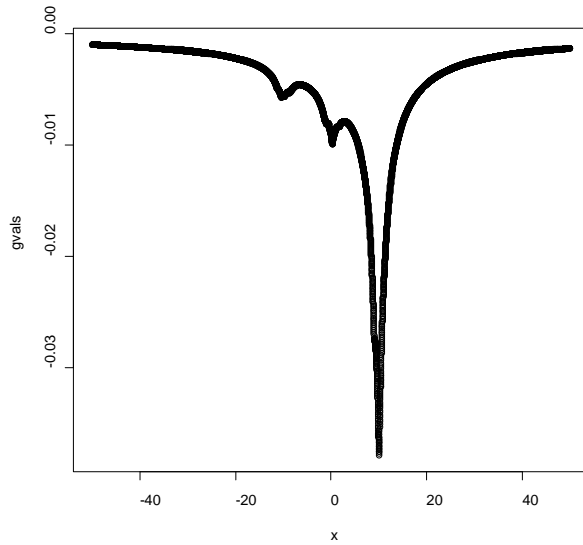
it takes 837.150000 seconds to test the local acceptance

|

[1] 16.61734
[1] 0.1063952
[1] 14.43249

2.3.2.13 case 152 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 10, \gamma = 0.5$ with fixed bandwidth

$b_n = 10$



Accepted 25983 out of 100000 (25.983%).

final beta = -1.028352

alpha(0.000000) is 0.259200

alpha(2.000000) is 0.476600

alpha(5.000000) is 0.779900

alpha(8.000000) is 0.416200

alpha(10.000000) is 0.164800

alpha(13.000000) is 0.326700

alpha(15.000000) is 0.421800

alpha(20.000000) is 0.451900

alpha(30.000000) is 0.460200

alpha(50.000000) is 0.465600

it takes 193.936000 seconds to run the adaptation algorithm

it takes 85.283000 seconds to compute g and sigma

it takes 19.154000 seconds to generate the first Markov Chain

it takes 18.866000 seconds to generate the second Markov Chain

it takes 20.767000 seconds to generate the third Markov Chain

it takes 20.124000 seconds to generate the fourth Markov Chain

it takes 21.762000 seconds to generate the fifth Markov Chain

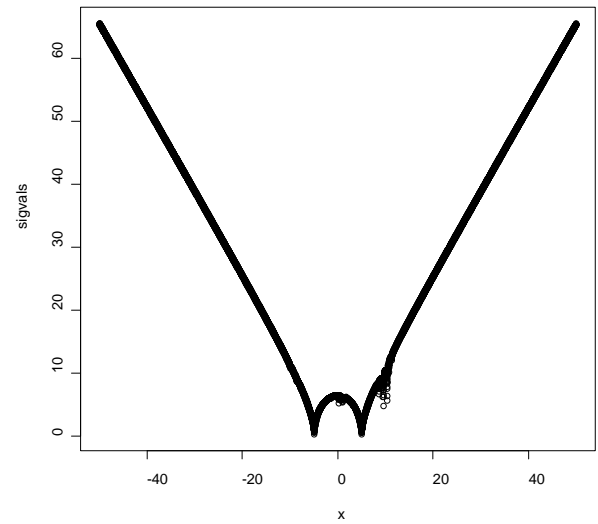
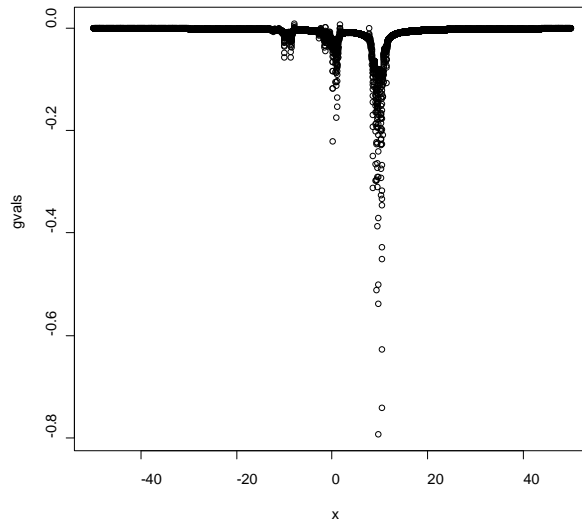
it takes 222.388000 seconds to test the local acceptance

1

[1] 21.61043
 [1] 0.1214091
 [1] 10.9672

2.3.2.14 case 153 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 10, \gamma = 0.5$ with fixed bandwidth

$b_n = 0.1$



Accepted 25310 out of 100000 (25.310%).

final beta = -0.875086

alpha(0.000000) is 0.237000

alpha(2.000000) is 0.485000

alpha(5.000000) is 0.802500

alpha(8.000000) is 0.398100

alpha(10.000000) is 0.171400

alpha(13.000000) is 0.324000

alpha(15.000000) is 0.399000

alpha(20.000000) is 0.435900

alpha(30.000000) is 0.436800

alpha(50.000000) is 0.447100

it takes 189.983000 seconds to run the adaptation algorithm

it takes 85.461000 seconds to compute g and sigma

it takes 24.926000 seconds to generate the first Markov Chain

it takes 23.326000 seconds to generate the second Markov Chain

it takes 23.988000 seconds to generate the third Markov Chain

it takes 23.716000 seconds to generate the fourth Markov Chain

it takes 21.556000 seconds to generate the fifth Markov Chain

it takes 229.869000 seconds to test the local acceptance

1

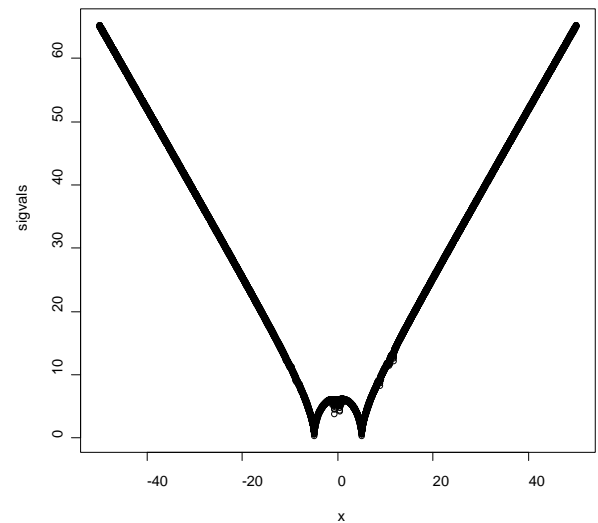
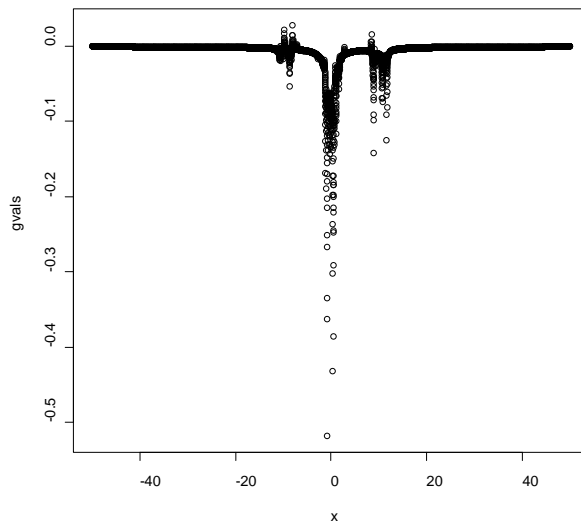
[1] 17.48015

[1] 0.108967

[1] 13.33216

2.3.2.15 case 154 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 10, \gamma = 0.5$ with decreasing

bandwidth $b_n = \frac{1}{n^{0.2}}$



Accepted 25287 out of 100000 (25.287%).

final beta = -0.880212

alpha(0.000000) is 0.254100

alpha(2.000000) is 0.477500

alpha(5.000000) is 0.794300

alpha(8.000000) is 0.402300

alpha(10.000000) is 0.168100

alpha(13.000000) is 0.317600

alpha(15.000000) is 0.402900

alpha(20.000000) is 0.435400

alpha(30.000000) is 0.436600

alpha(50.000000) is 0.436100

it takes 188.427000 seconds to run the adaptation algorithm

it takes 82.681000 seconds to compute g and sigma

it takes 20.371000 seconds to generate the first Markov Chain

it takes 20.669000 seconds to generate the second Markov Chain

it takes 20.434000 seconds to generate the third Markov Chain

it takes 20.132000 seconds to generate the fourth Markov Chain

it takes 19.589000 seconds to generate the fifth Markov Chain

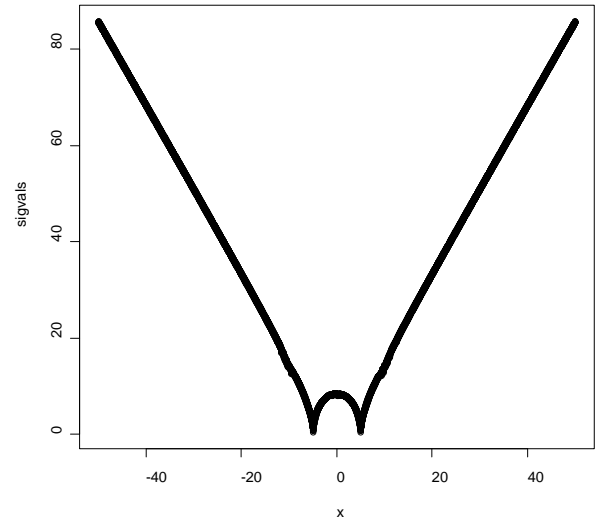
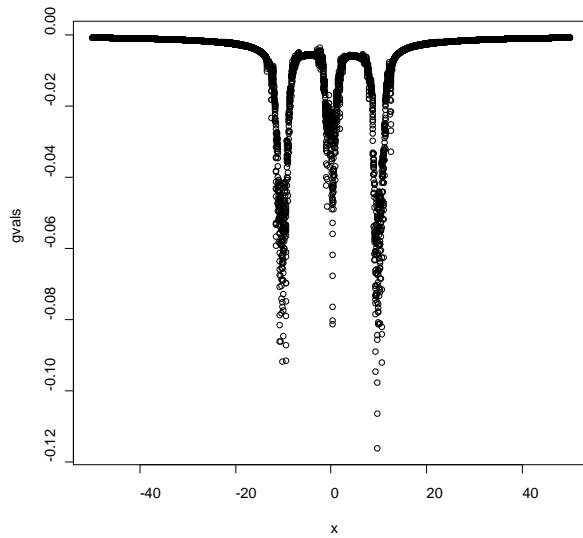
it takes 236.470000 seconds to test the local acceptance

1

[1] 17.77595
 [1] 0.1097439
 [1] 13.55263

2.3.2.16 case 155 $\eta_n = \frac{1}{(n+5)^{0.8}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 10, \gamma = 0.5$ fixed bandwidth

$b_n = 1$



Accepted 23144 out of 100000 (23.144%).

final beta = -0.606829

alpha(0.000000) is 0.202900

alpha(2.000000) is 0.448100

alpha(5.000000) is 0.840800

alpha(8.000000) is 0.360600

alpha(10.000000) is 0.159400

alpha(13.000000) is 0.293900

alpha(15.000000) is 0.365500

alpha(20.000000) is 0.387600

alpha(30.000000) is 0.374600

alpha(50.000000) is 0.378500

it takes 187.910000 seconds to run the adaptation algorithm

it takes 83.228000 seconds to compute g and sigma

it takes 23.281000 seconds to generate the first Markov Chain

it takes 24.219000 seconds to generate the second Markov Chain

it takes 22.092000 seconds to generate the third Markov Chain

it takes 22.606000 seconds to generate the fourth Markov Chain

it takes 23.064000 seconds to generate the fifth Markov Chain

it takes 261.017000 seconds to test the local acceptance

1

[1] 12.96691

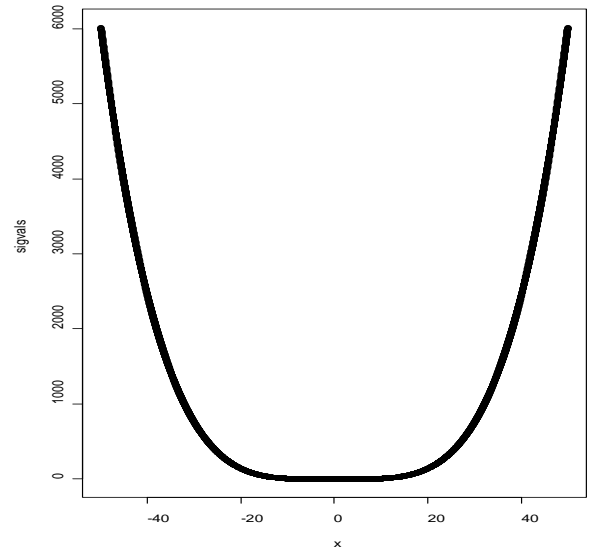
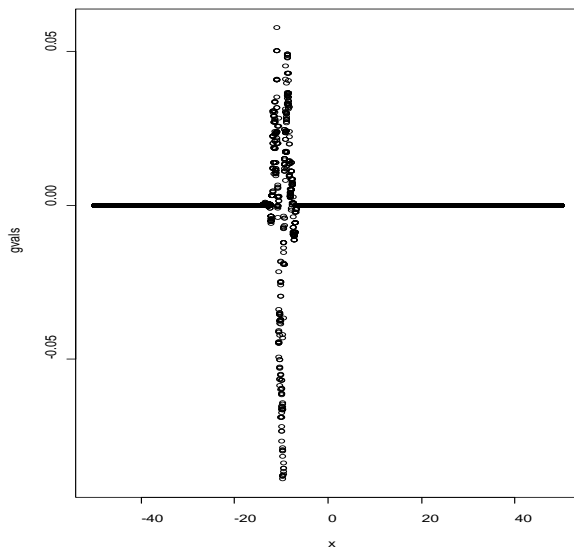
[1] 0.09388677

[1] 17.26632

2.3.3 kernel function
$$K(x) = \begin{cases} 0, & |x| \geq 2 * width \\ -1 * height, & width < |x| < 2 * width \\ 1 * height, & |x| \leq width \end{cases}$$

2.3.3.1 case 149 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 0.1, \gamma = 0.5$ with fixed bandwidth

$b_n = 1$



Accepted 23385 out of 100000 (23.385%).

final beta = -6.925807

alpha(0.000000) is 0.811400

alpha(2.000000) is 0.742800

alpha(5.000000) is 0.952600

alpha(8.000000) is 0.614000

alpha(10.000000) is 0.182200

alpha(13.000000) is 0.132100

alpha(15.000000) is 0.114700

alpha(20.000000) is 0.063800

alpha(30.000000) is 0.025300

alpha(50.000000) is 0.005000

it takes 346.490000 seconds to run the adaptation algorithm

it takes 152.520000 seconds to compute g and sigma

it takes 166.510000 seconds to generate the first Markov Chain

it takes 172.820000 seconds to generate the second Markov Chain

it takes 163.730000 seconds to generate the third Markov Chain

it takes 164.330000 seconds to generate the fourth Markov Chain

it takes 169.000000 seconds to generate the fifth Markov Chain

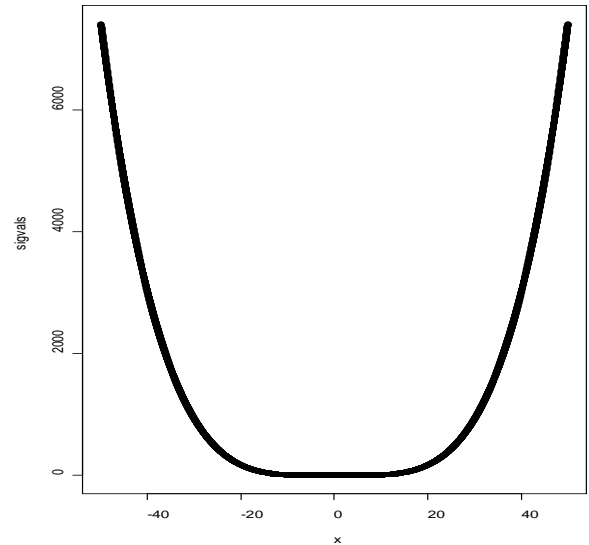
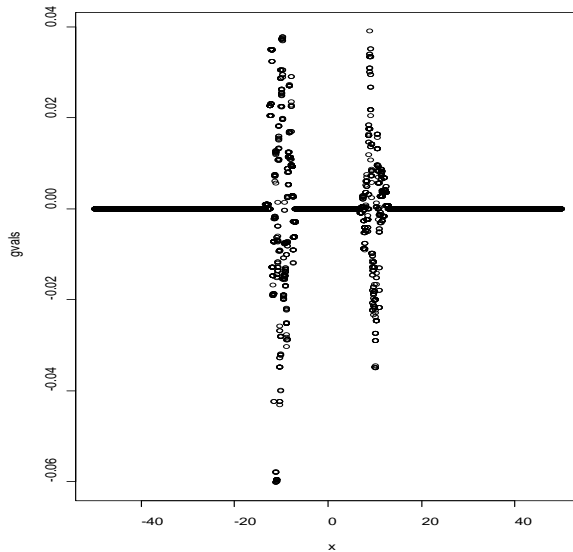
it takes 840.990000 seconds to test the local acceptance

1

[1] 90.39445
 [1] 0.3176161
 [1] 1.277381

2.3.3.2 case 157 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.5, width = 0.5, $C = 10, \gamma = 2$ with fixed

bandwidth $b_n = 1$



Accepted 20323 out of 100000 (20.323%).

final beta = -11.322095

alpha(0.000000) is 0.782200

alpha(2.000000) is 0.738500

alpha(5.000000) is 0.712800

alpha(8.000000) is 0.590300

alpha(10.000000) is 0.155300

alpha(13.000000) is 0.124000

alpha(15.000000) is 0.107600

alpha(20.000000) is 0.057300

alpha(30.000000) is 0.020600

alpha(50.000000) is 0.004700

it takes 346.640000 seconds to run the adaptation algorithm

it takes 152.770000 seconds to compute g and sigma

it takes 167.790000 seconds to generate the first Markov Chain

it takes 166.350000 seconds to generate the second Markov Chain

it takes 166.360000 seconds to generate the third Markov Chain

it takes 167.700000 seconds to generate the fourth Markov Chain

it takes 168.230000 seconds to generate the fifth Markov Chain

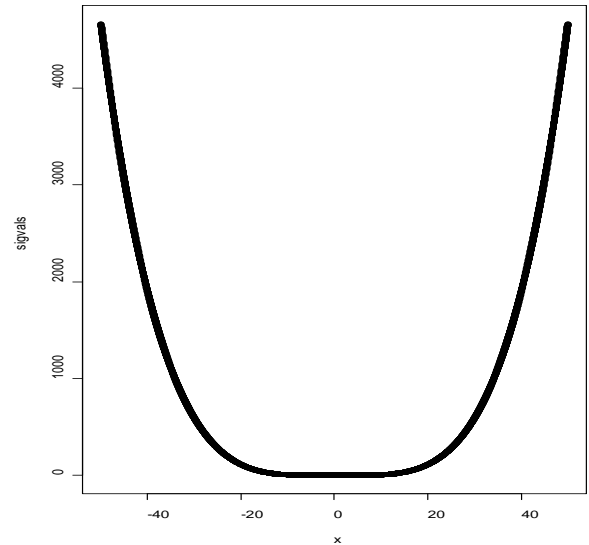
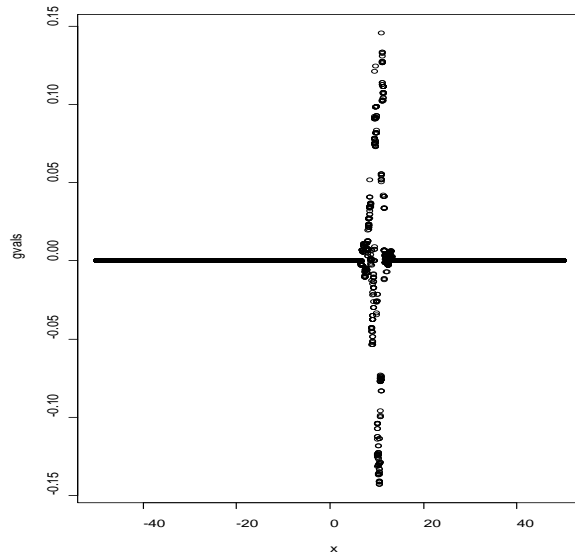
it takes 865.340000 seconds to test the local acceptance

1

[1] 82.33719
 [1] 0.3038594
 [1] 2.291764

2.3.3.3 case 158 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.5, width = 0.5, $C = 0.1, \gamma = 2$ with fixed

bandwidth $b_n = 1$



Accepted 23903 out of 100000 (23.903%).

final beta = -2.583150

alpha(0.000000) is 0.722500

alpha(2.000000) is 0.700400

alpha(5.000000) is 0.981800

alpha(8.000000) is 0.596600

alpha(10.000000) is 0.195900

alpha(13.000000) is 0.150100

alpha(15.000000) is 0.134500

alpha(20.000000) is 0.085400

alpha(30.000000) is 0.029800

alpha(50.000000) is 0.006800

it takes 347.020000 seconds to run the adaptation algorithm

it takes 152.780000 seconds to compute g and sigma

it takes 168.540000 seconds to generate the first Markov Chain

it takes 167.300000 seconds to generate the second Markov Chain

it takes 166.200000 seconds to generate the third Markov Chain

it takes 171.660000 seconds to generate the fourth Markov Chain

it takes 166.300000 seconds to generate the fifth Markov Chain

it takes 817.780000 seconds to test the local acceptance

1

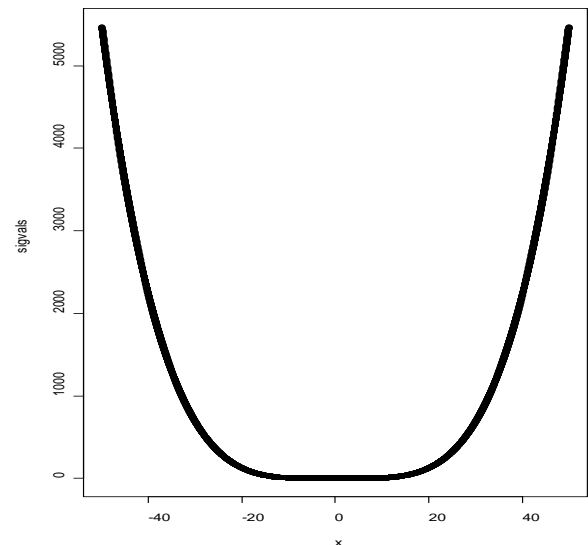
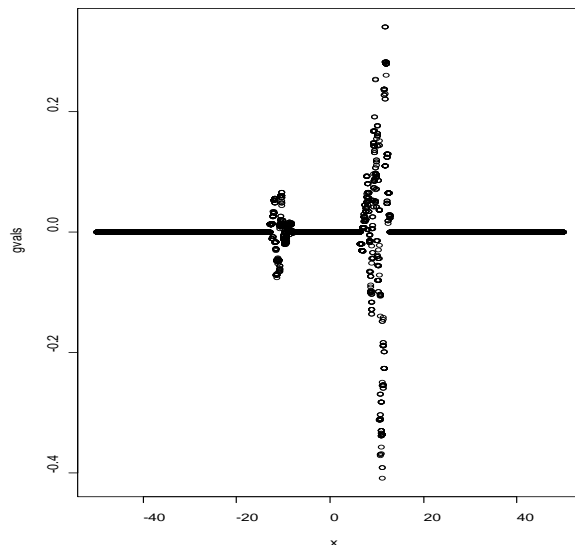
[1] 91.6572

[1] 0.3206371

[1] 1.161233

2.3.3.4 case 159 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 2, width = 0.5, $C = 0.1, \gamma = 2$ with fixed

bandwidth $b_n = 1$



Accepted 81480 out of 100000 (81.480%).

final beta = -7.021089

alpha(0.000000) is 0.839500

alpha(2.000000) is 0.759000

alpha(5.000000) is 0.955800

alpha(8.000000) is 0.628500

alpha(10.000000) is 0.194600

alpha(13.000000) is 0.135300

alpha(15.000000) is 0.129300

alpha(20.000000) is 0.068600

alpha(30.000000) is 0.021900

alpha(50.000000) is 0.005500

it takes 346.280000 seconds to run the adaptation algorithm

it takes 152.760000 seconds to compute g and sigma

it takes 163.380000 seconds to generate the first Markov Chain

it takes 168.860000 seconds to generate the second Markov Chain

it takes 171.100000 seconds to generate the third Markov Chain

it takes 166.650000 seconds to generate the fourth Markov Chain

it takes 166.330000 seconds to generate the fifth Markov Chain

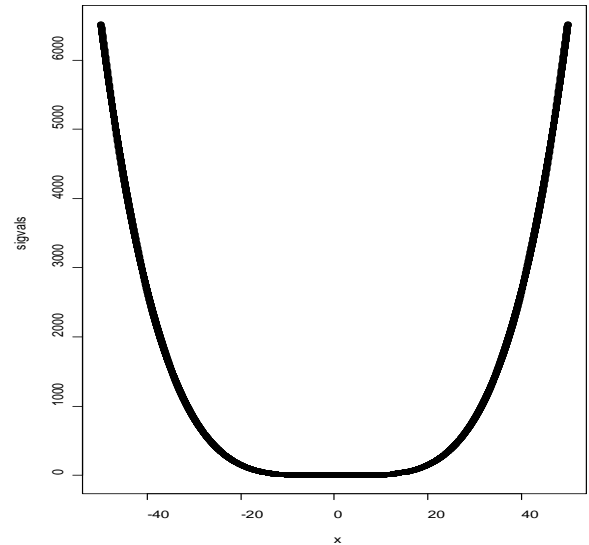
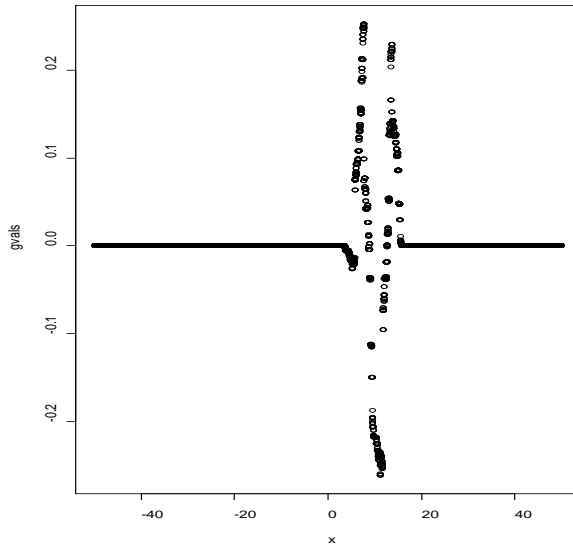
it takes 829.620000 seconds to test the local acceptance

1

[1] 21.36030
 [1] 0.01514145
 [1] 0.1902173

2.3.3.5 case 160 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.5, width = 2, $C = 0.1, \gamma = 2$ with fixed

bandwidth $b_n = 1$



Accepted 22930 out of 100000 (22.930%).

final beta = -6.845094

alpha(0.000000) is 0.788500

alpha(2.000000) is 0.738200

alpha(5.000000) is 0.955200

alpha(8.000000) is 0.590000

alpha(10.000000) is 0.195100

alpha(13.000000) is 0.119600

alpha(15.000000) is 0.102500

alpha(20.000000) is 0.060000

alpha(30.000000) is 0.023800

alpha(50.000000) is 0.004400

it takes 340.490000 seconds to run the adaptation algorithm

it takes 152.290000 seconds to compute g and sigma

it takes 166.240000 seconds to generate the first Markov Chain

it takes 166.180000 seconds to generate the second Markov Chain

it takes 172.370000 seconds to generate the third Markov Chain

it takes 166.020000 seconds to generate the fourth Markov Chain

it takes 166.830000 seconds to generate the fifth Markov Chain

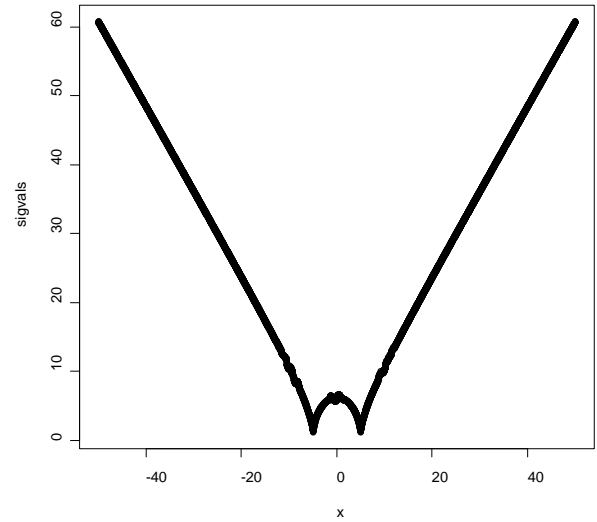
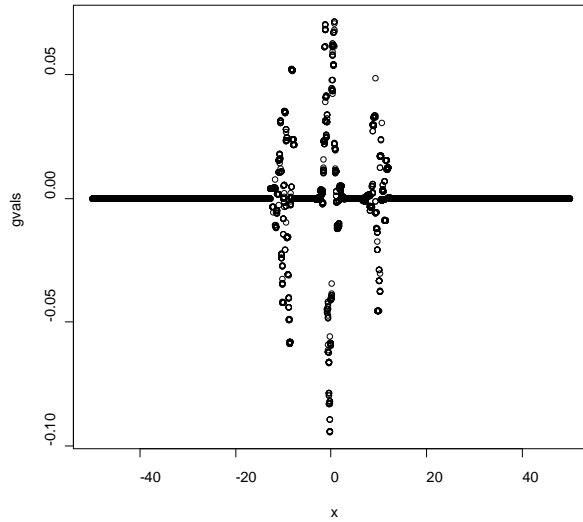
it takes 857.250000 seconds to test the local acceptance

1

[1] 91.28385
[1] 0.3193566
[1] 1.143155

2.3.3.6 case 161 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.5, width = 0.5, $C = 1, \gamma = 0.5$ with fixed

bandwidth $b_n = 1$



Accepted 25782 out of 100000 (25.782%).

final beta = 0.199733

alpha(0.000000) is 0.251500

alpha(2.000000) is 0.478800

alpha(5.000000) is 0.974700

alpha(8.000000) is 0.393500

alpha(10.000000) is 0.162700

alpha(13.000000) is 0.315100

alpha(15.000000) is 0.416800

alpha(20.000000) is 0.452300

alpha(30.000000) is 0.442600

alpha(50.000000) is 0.449500

it takes 347.050000 seconds to run the adaptation algorithm

it takes 152.430000 seconds to compute g and sigma

it takes 166.980000 seconds to generate the first Markov Chain

it takes 166.170000 seconds to generate the second Markov Chain

it takes 166.680000 seconds to generate the third Markov Chain

it takes 167.440000 seconds to generate the fourth Markov Chain

it takes 165.880000 seconds to generate the fifth Markov Chain

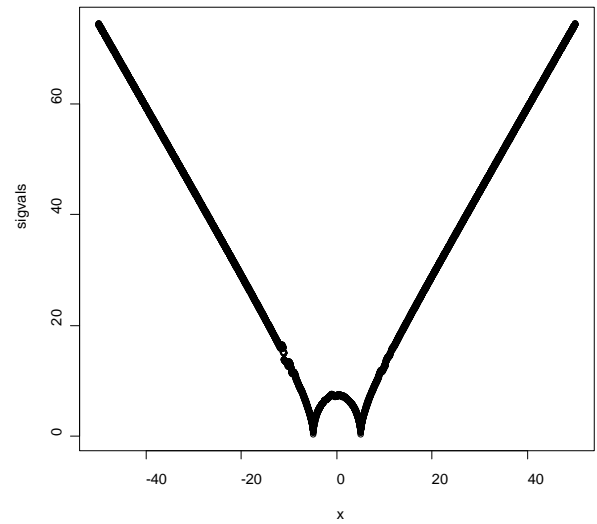
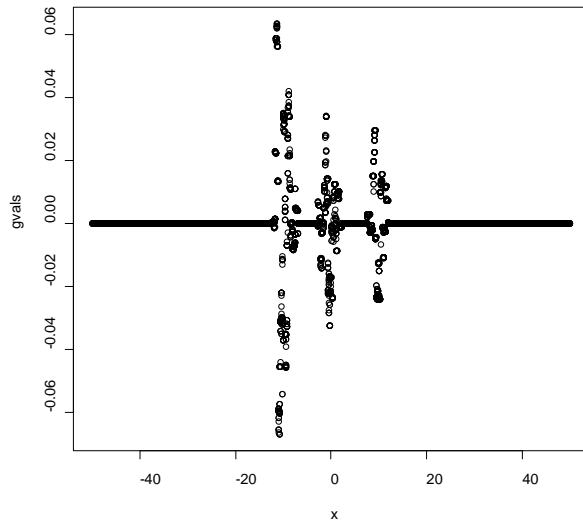
it takes 561.600000 seconds to test the local acceptance

1

[1] 17.85295
[1] 0.1088777
[1] 13.29712

2.3.3.7 case 162 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.5, width = 0.5, $C = 10$, $\gamma = 0.5$ with fixed

bandwidth $b_n = 1$



Accepted 24413 out of 100000 (24.413%).

final beta = -0.748534

alpha(0.000000) is 0.225100

alpha(2.000000) is 0.463600

alpha(5.000000) is 0.665100

alpha(8.000000) is 0.384400

alpha(10.000000) is 0.169500

alpha(13.000000) is 0.307900

alpha(15.000000) is 0.385300

alpha(20.000000) is 0.420700

alpha(30.000000) is 0.418600

alpha(50.000000) is 0.408900

it takes 347.780000 seconds to run the adaptation algorithm

it takes 152.450000 seconds to compute g and sigma

it takes 168.000000 seconds to generate the first Markov Chain

it takes 168.100000 seconds to generate the second Markov Chain

it takes 167.180000 seconds to generate the third Markov Chain

it takes 168.710000 seconds to generate the fourth Markov Chain

it takes 167.550000 seconds to generate the fifth Markov Chain

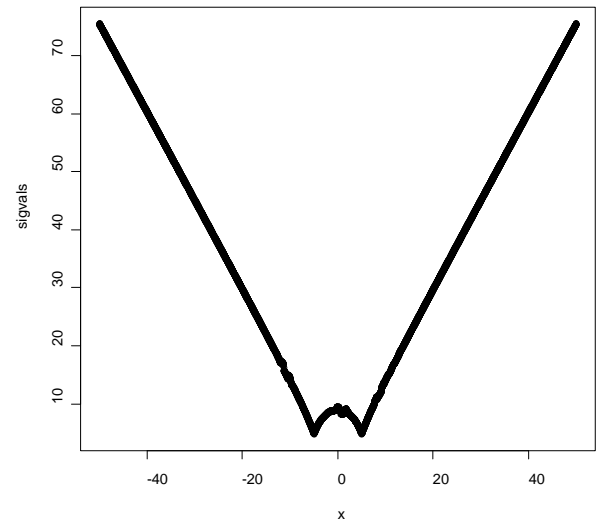
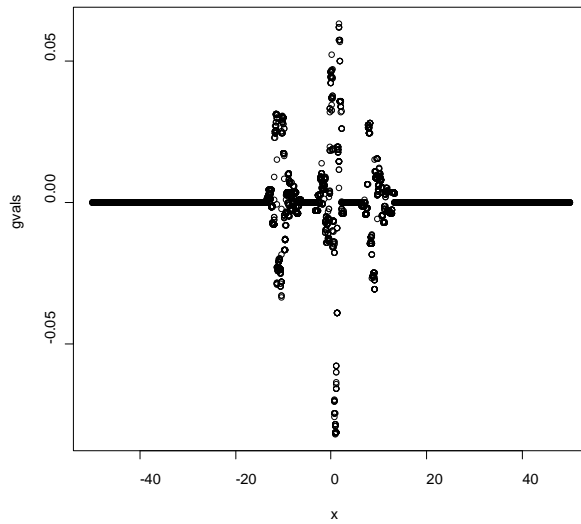
it takes 585.160000 seconds to test the local acceptance

1

[1] 13.60182
[1] 0.09651798
[1] 16.46537

2.3.3.8 case 163 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.5, width = 0.5, $C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 1$



Accepted 23030 out of 100000 (23.030%).

final beta = 1.566764

alpha(0.000000) is 0.196400

alpha(2.000000) is 0.438500

alpha(5.000000) is 0.984500

alpha(8.000000) is 0.361400

alpha(10.000000) is 0.169300

alpha(13.000000) is 0.303900

alpha(15.000000) is 0.397200

alpha(20.000000) is 0.406300

alpha(30.000000) is 0.407600

alpha(50.000000) is 0.404800

it takes 347.430000 seconds to run the adaptation algorithm

it takes 152.300000 seconds to compute g and sigma

it takes 169.060000 seconds to generate the first Markov Chain

it takes 169.210000 seconds to generate the second Markov Chain

it takes 169.940000 seconds to generate the third Markov Chain

it takes 168.840000 seconds to generate the fourth Markov Chain

it takes 168.600000 seconds to generate the fifth Markov Chain

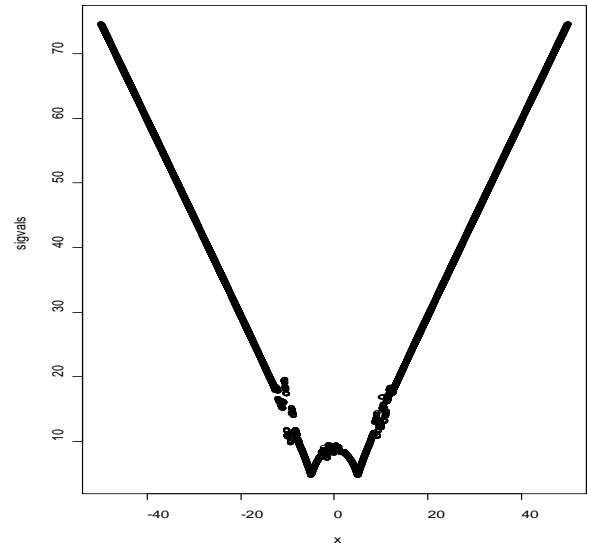
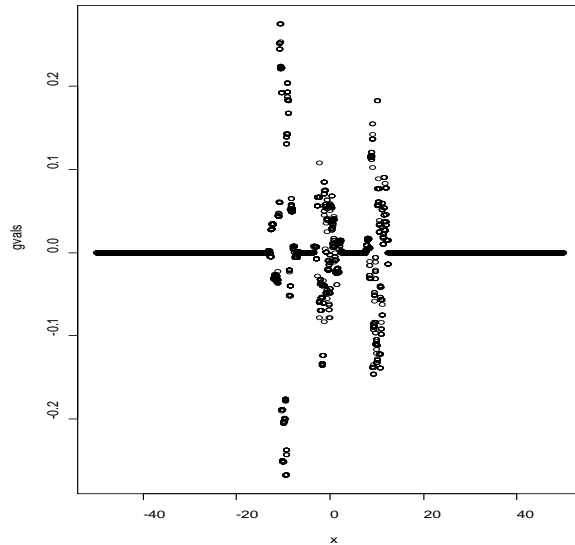
it takes 593.080000 seconds to test the local acceptance

1

[1] 12.99476
[1] 0.09387773
[1] 17.25407

2.3.3.9 case 164 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 2, width = 0.5, $C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 1$



Accepted 23148 out of 100000 (23.148%).

final beta = 1.555008

alpha(0.000000) is 0.197200

alpha(2.000000) is 0.436800

alpha(5.000000) is 0.985200

alpha(8.000000) is 0.354100

alpha(10.000000) is 0.163900

alpha(13.000000) is 0.315100

alpha(15.000000) is 0.414400

alpha(20.000000) is 0.416100

alpha(30.000000) is 0.405600

alpha(50.000000) is 0.405300

it takes 346.860000 seconds to run the adaptation algorithm

it takes 152.730000 seconds to compute g and sigma

it takes 169.540000 seconds to generate the first Markov Chain

it takes 170.330000 seconds to generate the second Markov Chain

it takes 169.700000 seconds to generate the third Markov Chain

it takes 170.450000 seconds to generate the fourth Markov Chain

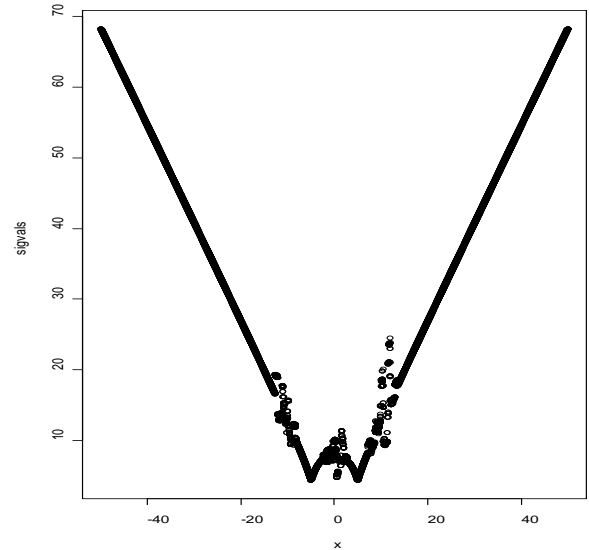
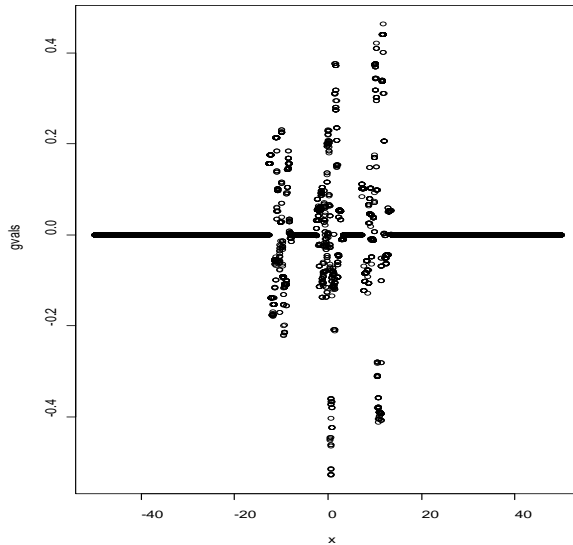
it takes 169.770000 seconds to generate the fifth Markov Chain

it takes 590.270000 seconds to test the local acceptance

1

[1] 13.87151
 [1] 0.09678516
 [1] 17.20643

2.3.3.10 case 165 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 5, width = 0.5, $C = 0.1, \gamma = 0.5$ with fixed bandwidth $b_n = 1$



Accepted 23545 out of 100000 (23.545%).

final beta = 1.465999

alpha(0.000000) is 0.197500

alpha(2.000000) is 0.460100

alpha(5.000000) is 0.990300

alpha(8.000000) is 0.384100

alpha(10.000000) is 0.161600

alpha(13.000000) is 0.315100

alpha(15.000000) is 0.423100

alpha(20.000000) is 0.435000

alpha(30.000000) is 0.436200

alpha(50.000000) is 0.425000

it takes 346.630000 seconds to run the adaptation algorithm

it takes 152.570000 seconds to compute g and sigma

it takes 169.800000 seconds to generate the first Markov Chain

it takes 169.690000 seconds to generate the second Markov Chain

it takes 169.740000 seconds to generate the third Markov Chain

it takes 169.530000 seconds to generate the fourth Markov Chain

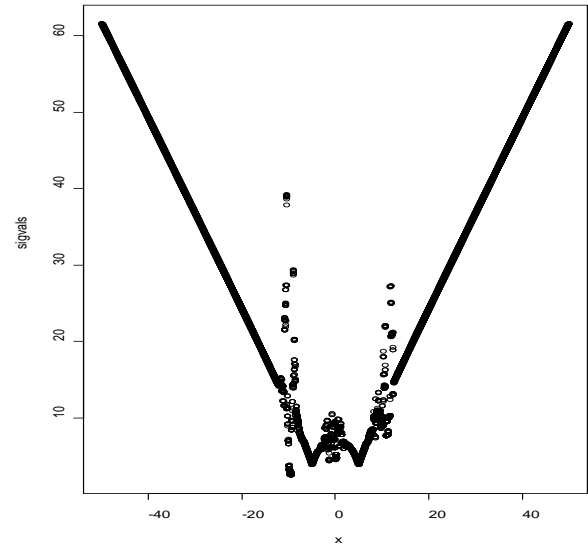
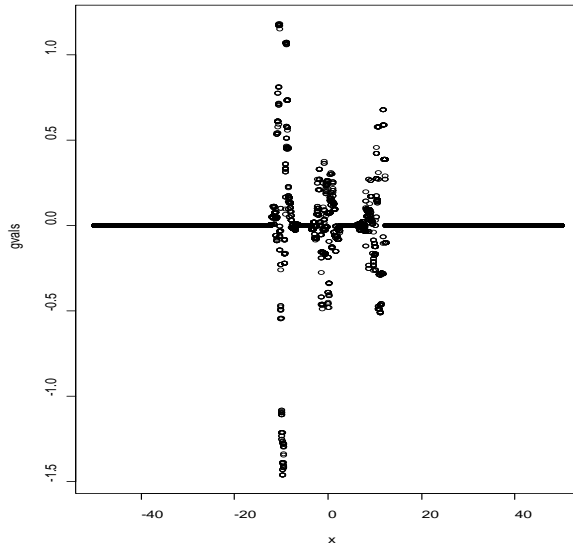
it takes 168.990000 seconds to generate the fifth Markov Chain

it takes 577.110000 seconds to test the local acceptance rate

1

2.3.3.11 case 166 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 10, width = 0.5, $C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 1$



Accepted 22643 out of 100000 (22.643%).

final beta = 1.363053

alpha(0.000000) is 0.212000

alpha(2.000000) is 0.456200

alpha(5.000000) is 0.994700

alpha(8.000000) is 0.386900

alpha(10.000000) is 0.169600

alpha(13.000000) is 0.329200

alpha(15.000000) is 0.430400

alpha(20.000000) is 0.446300

alpha(30.000000) is 0.447600

alpha(50.000000) is 0.443200

it takes 346.650000 seconds to run the adaptation algorithm

it takes 152.580000 seconds to compute g and sigma

it takes 177.310000 seconds to generate the first Markov Chain

it takes 177.070000 seconds to generate the second Markov Chain

it takes 176.700000 seconds to generate the third Markov Chain

it takes 176.140000 seconds to generate the fourth Markov Chain

it takes 177.500000 seconds to generate the fifth Markov Chain

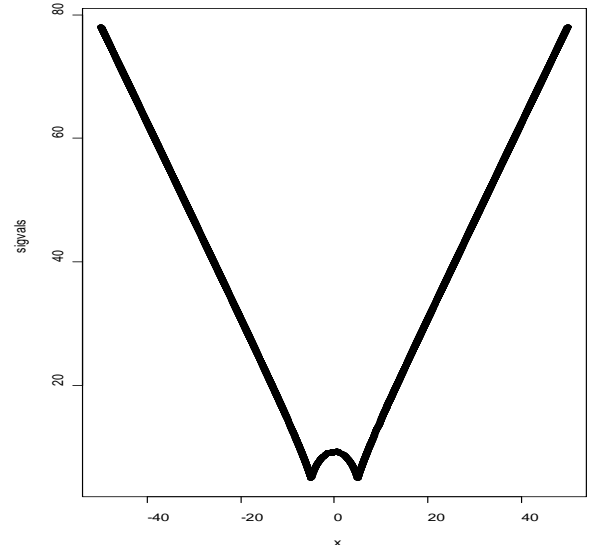
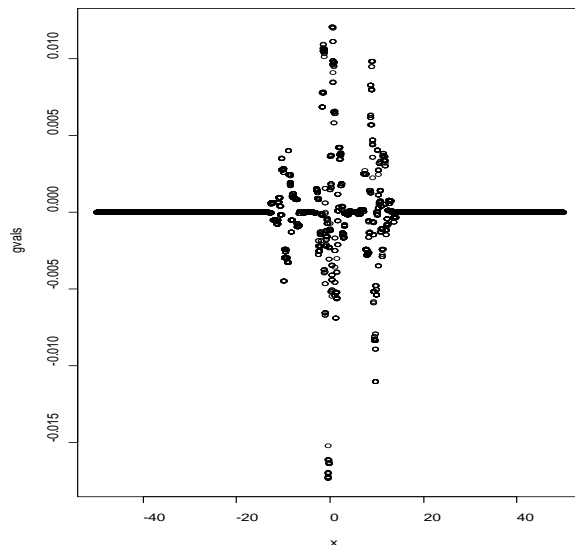
it takes 563.200000 seconds to test the local acceptance

1

[1] 21.28494
[1] 0.1196420
[1] 12.15185

2.3.3.12 case 167 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.1, width = 0.5, $C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 1$



Accepted 22697 out of 100000 (22.697%).

final beta = 1.599916

alpha(0.000000) is 0.185500

alpha(2.000000) is 0.432600

alpha(5.000000) is 0.980600

alpha(8.000000) is 0.360300

alpha(10.000000) is 0.157000

alpha(13.000000) is 0.309100

alpha(15.000000) is 0.398400

alpha(20.000000) is 0.410200

alpha(30.000000) is 0.395600

alpha(50.000000) is 0.392800

it takes 347.310000 seconds to run the adaptation algorithm

it takes 152.460000 seconds to compute g and sigma

it takes 169.840000 seconds to generate the first Markov Chain

it takes 169.340000 seconds to generate the second Markov Chain

it takes 170.130000 seconds to generate the third Markov Chain

it takes 169.930000 seconds to generate the fourth Markov Chain

it takes 170.120000 seconds to generate the fifth Markov Chain

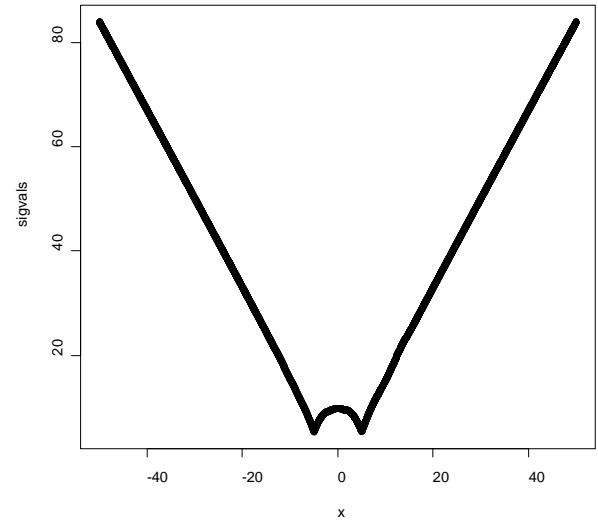
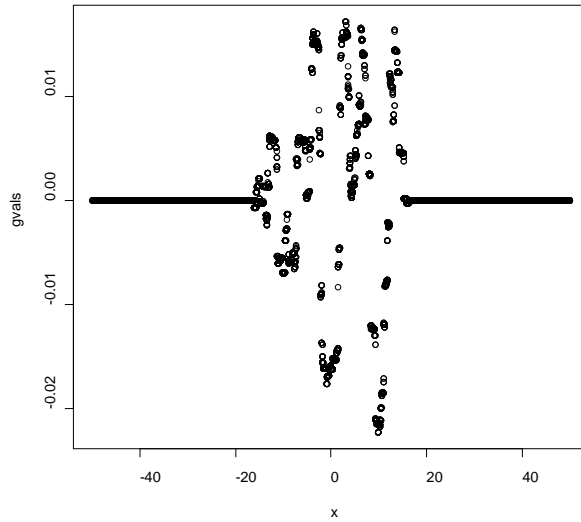
it takes 597.480000 seconds to test the local acceptance

1

[1] 13.29028
[1] 0.09469267
[1] 17.58271

2.3.3.13 case 168 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.1, width = 2, $C = 0.1$, $\gamma = 0.5$ with fixed

bandwidth $b_n = 1$



Accepted 21952 out of 100000 (21.952%).

final beta = 1.672013

alpha(0.000000) is 0.184000

alpha(2.000000) is 0.418100

alpha(5.000000) is 0.968800

alpha(8.000000) is 0.343500

alpha(10.000000) is 0.158900

alpha(13.000000) is 0.300400

alpha(15.000000) is 0.388000

alpha(20.000000) is 0.388200

alpha(30.000000) is 0.379900

alpha(50.000000) is 0.380900

it takes 344.410000 seconds to run the adaptation algorithm

it takes 152.050000 seconds to compute g and sigma

it takes 172.150000 seconds to generate the first Markov Chain

it takes 173.150000 seconds to generate the second Markov Chain

it takes 170.720000 seconds to generate the third Markov Chain

it takes 171.580000 seconds to generate the fourth Markov Chain

it takes 171.530000 seconds to generate the fifth Markov Chain

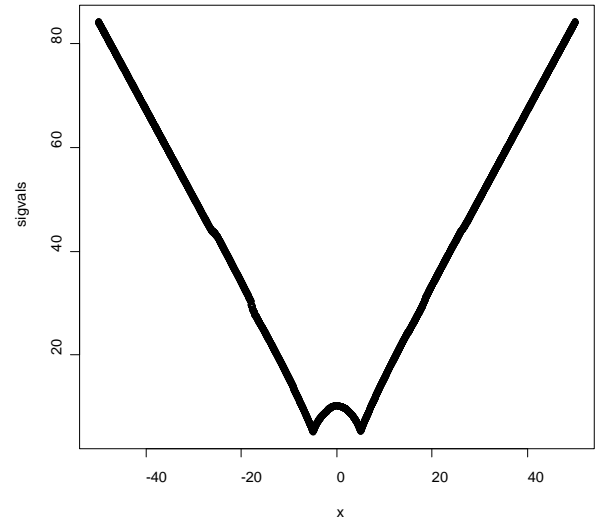
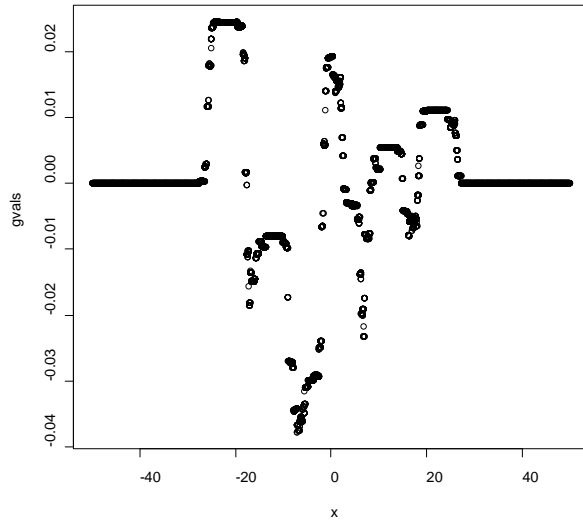
it takes 609.770000 seconds to test the local acceptance

1

[1] 13.51672
[1] 0.09560705
[1] 17.78677

2.3.3.14 case 169 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.1, width = 8, $C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 1$



Accepted 21813 out of 100000 (21.813%).

final beta = 1.675306

alpha(0.000000) is 0.176600

alpha(2.000000) is 0.413300

alpha(5.000000) is 0.969100

alpha(8.000000) is 0.342100

alpha(10.000000) is 0.154200

alpha(13.000000) is 0.297700

alpha(15.000000) is 0.386400

alpha(20.000000) is 0.385700

alpha(30.000000) is 0.384000

alpha(50.000000) is 0.385500

it takes 336.020000 seconds to run the adaptation algorithm

it takes 150.700000 seconds to compute g and sigma

it takes 172.710000 seconds to generate the first Markov Chain

it takes 172.260000 seconds to generate the second Markov Chain

it takes 171.770000 seconds to generate the third Markov Chain

it takes 173.580000 seconds to generate the fourth Markov Chain

it takes 172.910000 seconds to generate the fifth Markov Chain

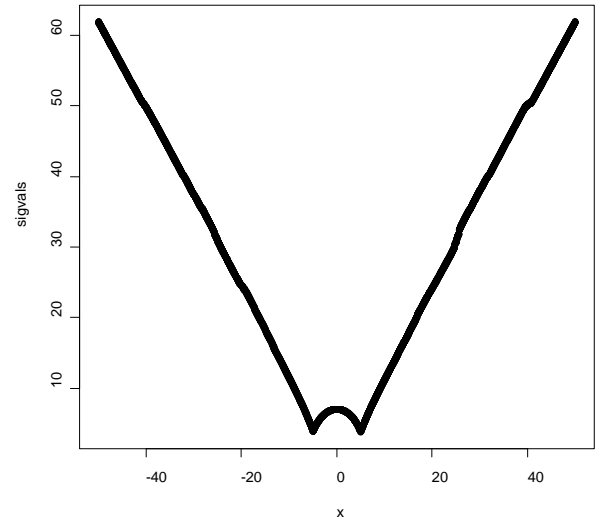
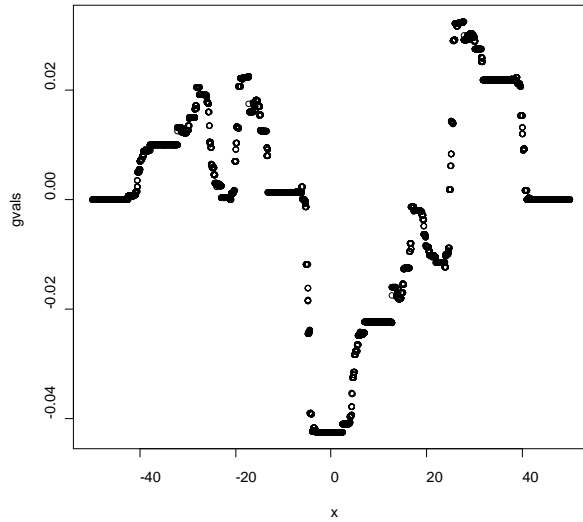
it takes 609.330000 seconds to test the local acceptance

1

[1] 13.63757
[1] 0.09651497
[1] 17.84017

2.3.3.15 case 170 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.1, width = 15, $C = 0.1$, $\gamma = 0.5$ with fixed

bandwidth $b_n = 1$



Accepted 24968 out of 100000 (24.968%).

final beta = 1.368241

alpha(0.000000) is 0.237200

alpha(2.000000) is 0.467000

alpha(5.000000) is 0.996200

alpha(8.000000) is 0.390800

alpha(10.000000) is 0.173500

alpha(13.000000) is 0.325900

alpha(15.000000) is 0.432200

alpha(20.000000) is 0.452500

alpha(30.000000) is 0.452300

alpha(50.000000) is 0.439200

it takes 330.360000 seconds to run the adaptation algorithm

it takes 148.840000 seconds to compute g and sigma

it takes 166.510000 seconds to generate the first Markov Chain

it takes 166.620000 seconds to generate the second Markov Chain

it takes 166.570000 seconds to generate the third Markov Chain

it takes 167.160000 seconds to generate the fourth Markov Chain

it takes 166.690000 seconds to generate the fifth Markov Chain

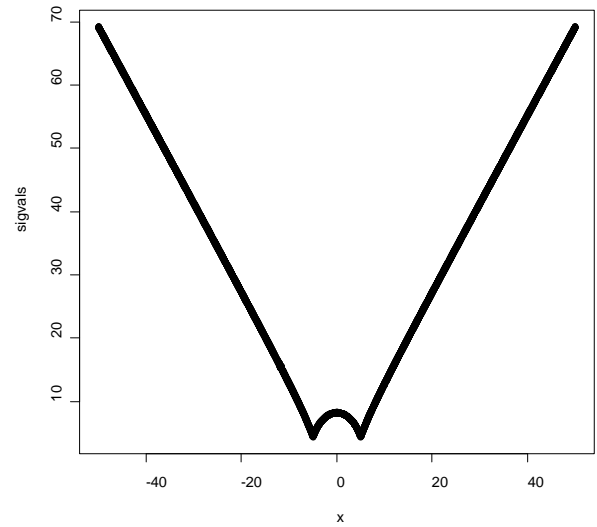
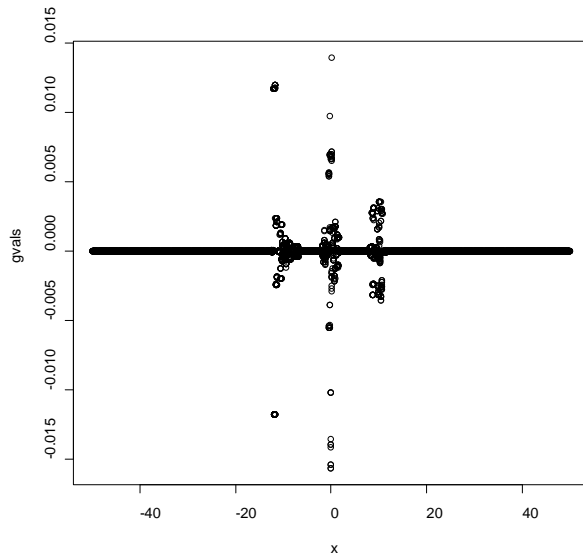
it takes 563.370000 seconds to test the local acceptance

1

[1] 15.62307
[1] 0.1033918
[1] 14.97829

2.3.3.16 case 171 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.1, width = 0.1, $C = 0.1$, $\gamma = 0.5$ with fixed

bandwidth $b_n = 1$



Accepted 24069 out of 100000 (24.069%).

final beta = 1.479692

alpha(0.000000) is 0.205700

alpha(2.000000) is 0.444900

alpha(5.000000) is 0.989800

alpha(8.000000) is 0.365500

alpha(10.000000) is 0.167200

alpha(13.000000) is 0.322200

alpha(15.000000) is 0.422300

alpha(20.000000) is 0.426700

alpha(30.000000) is 0.419800

alpha(50.000000) is 0.428600

it takes 348.040000 seconds to run the adaptation algorithm

it takes 152.510000 seconds to compute g and sigma

it takes 167.270000 seconds to generate the first Markov Chain

it takes 167.570000 seconds to generate the second Markov Chain

it takes 167.280000 seconds to generate the third Markov Chain

it takes 167.430000 seconds to generate the fourth Markov Chain

it takes 167.320000 seconds to generate the fifth Markov Chain

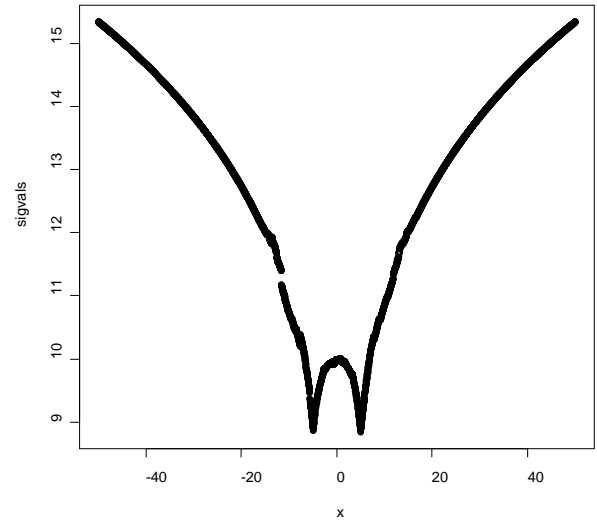
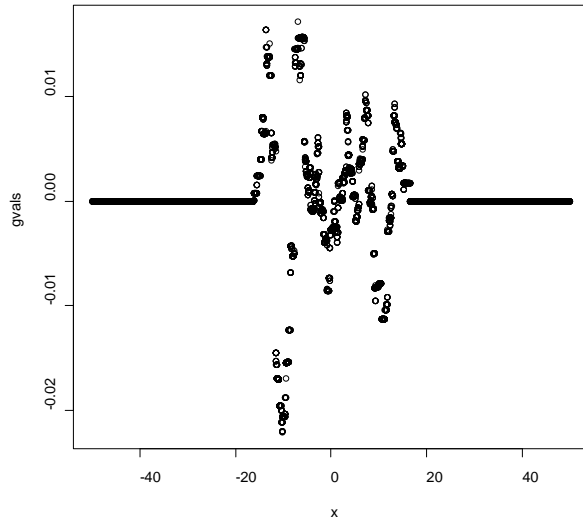
it takes 576.120000 seconds to test the local acceptance

|

[1] 13.0853
[1] 0.09413097
[1] 16.67941

2.3.3.17 case 172 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.1, width = 2, $C = 0.1, \gamma = 0.1$ with fixed

bandwidth $b_n = 1$



Accepted 23706 out of 100000 (23.706%).

final beta = 2.179023

alpha(0.000000) is 0.189700

alpha(2.000000) is 0.407500

alpha(5.000000) is 0.867700

alpha(8.000000) is 0.363500

alpha(10.000000) is 0.178000

alpha(13.000000) is 0.375300

alpha(15.000000) is 0.498500

alpha(20.000000) is 0.508500

alpha(30.000000) is 0.499000

alpha(50.000000) is 0.503400

it takes 131.989000 seconds to run the adaptation algorithm

it takes 56.976000 seconds to compute g and sigma

it takes 19.196000 seconds to generate the first Markov Chain

it takes 19.213000 seconds to generate the second Markov Chain

it takes 19.843000 seconds to generate the third Markov Chain

it takes 19.346000 seconds to generate the fourth Markov Chain

it takes 20.059000 seconds to generate the fifth Markov Chain

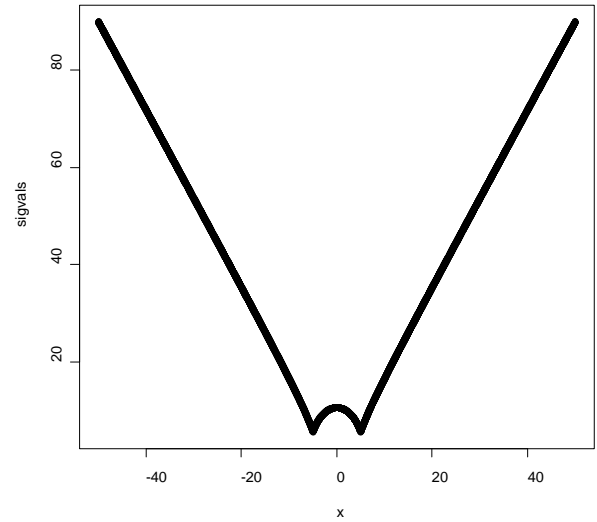
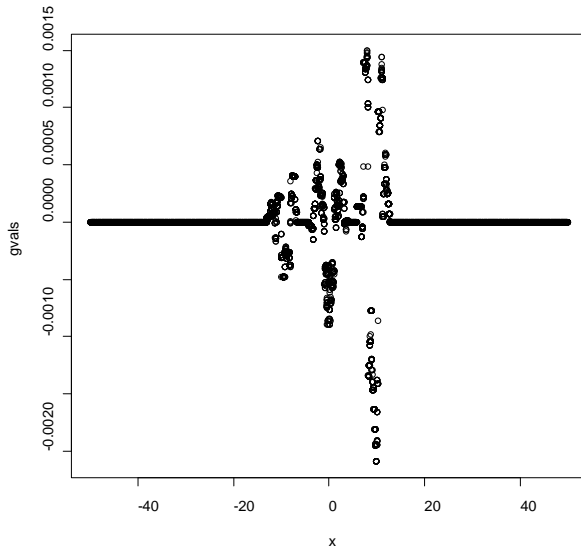
it takes 143.342000 seconds to test the local acceptance

1

[1] 14.62442
 [1] 0.09965965
 [1] 15.71839

2.3.3.18 case 173 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.1, width = 2, $C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 10$



Accepted 21044 out of 100000 (21.044%).

final beta = 1.740088

alpha(0.000000) is 0.167200

alpha(2.000000) is 0.396400

alpha(5.000000) is 0.960700

alpha(8.000000) is 0.323100

alpha(10.000000) is 0.158800

alpha(13.000000) is 0.281300

alpha(15.000000) is 0.374900

alpha(20.000000) is 0.364600

alpha(30.000000) is 0.374800

alpha(50.000000) is 0.362200

it takes 345.360000 seconds to run the adaptation algorithm

it takes 151.990000 seconds to compute g and sigma

it takes 175.400000 seconds to generate the first Markov Chain

it takes 175.550000 seconds to generate the second Markov Chain

it takes 175.420000 seconds to generate the third Markov Chain

it takes 175.200000 seconds to generate the fourth Markov Chain

it takes 175.200000 seconds to generate the fifth Markov Chain

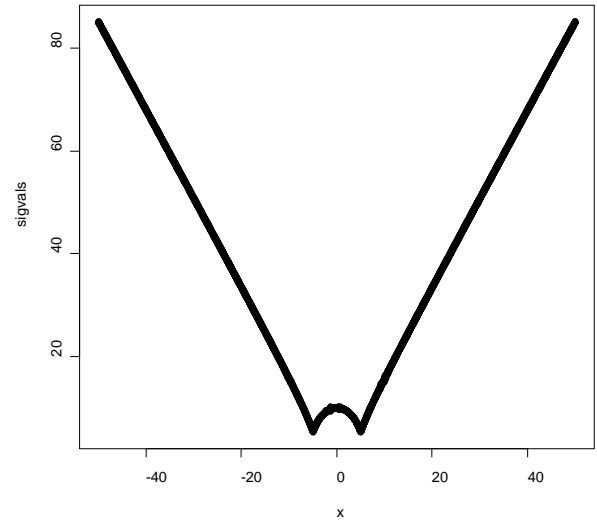
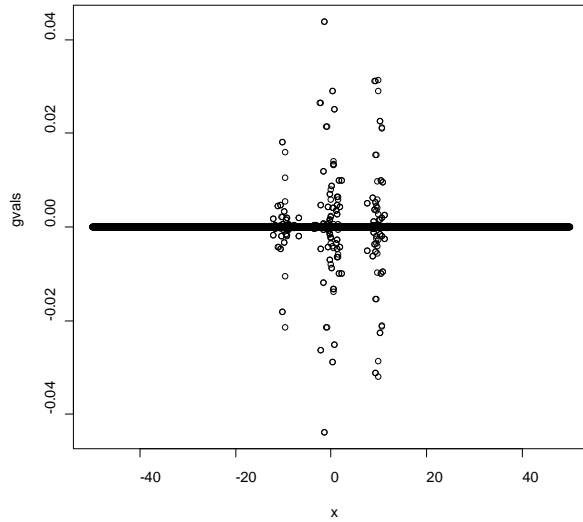
it takes 623.140000 seconds to test the local acceptance

|

[1] 12.96732
[1] 0.0933517
[1] 17.73759

2.3.3.19 case 174 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.1, width = 2, $C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 0.1$



Accepted 21641 out of 100000 (21.641%).

final beta = 1.685472

alpha(0.000000) is 0.176700

alpha(2.000000) is 0.411100

alpha(5.000000) is 0.969100

alpha(8.000000) is 0.340200

alpha(10.000000) is 0.158400

alpha(13.000000) is 0.295200

alpha(15.000000) is 0.388400

alpha(20.000000) is 0.386200

alpha(30.000000) is 0.389100

alpha(50.000000) is 0.378400

it takes 348.360000 seconds to run the adaptation algorithm

it takes 152.300000 seconds to compute g and sigma

it takes 173.130000 seconds to generate the first Markov Chain

it takes 173.530000 seconds to generate the second Markov Chain

it takes 172.380000 seconds to generate the third Markov Chain

it takes 171.800000 seconds to generate the fourth Markov Chain

it takes 172.980000 seconds to generate the fifth Markov Chain

it takes 612.070000 seconds to test the local acceptance

1

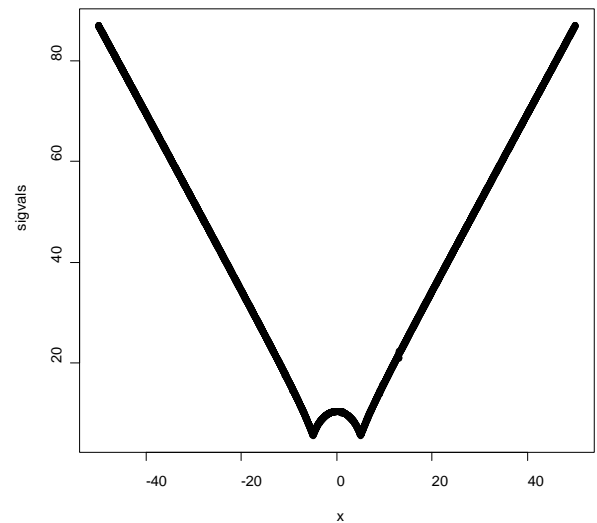
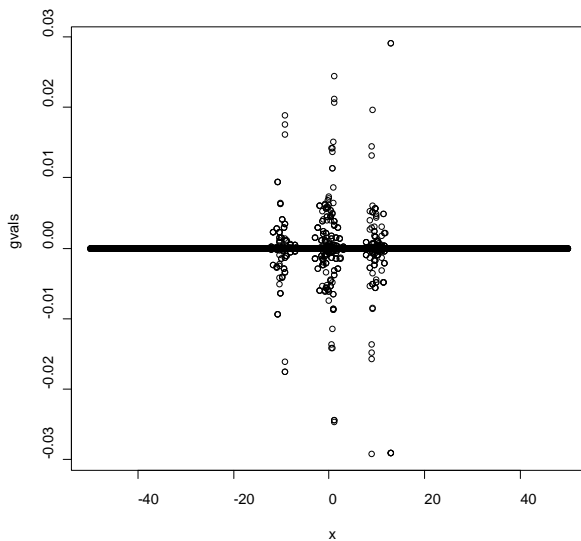
[1] 12.68868

[1] 0.09229896

[1] 17.97203

2.3.3.20 case 175 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.1, width = 2, $C = 0.1, \gamma = 0.5$ with

decreasing bandwidth $b_n = \frac{1}{n^{0.2}}$



Accepted 21390 out of 100000 (21.390%).

final beta = 1.708766

alpha(0.000000) is 0.163300

alpha(2.000000) is 0.404300

alpha(5.000000) is 0.966800

alpha(8.000000) is 0.344400

alpha(10.000000) is 0.157300

alpha(13.000000) is 0.298100

alpha(15.000000) is 0.369800

alpha(20.000000) is 0.371100

alpha(30.000000) is 0.378700

alpha(50.000000) is 0.382100

it takes 348.370000 seconds to run the adaptation algorithm

it takes 152.520000 seconds to compute g and sigma

it takes 173.190000 seconds to generate the first Markov Chain

it takes 174.010000 seconds to generate the second Markov Chain

it takes 173.840000 seconds to generate the third Markov Chain

it takes 172.650000 seconds to generate the fourth Markov Chain

it takes 173.240000 seconds to generate the fifth Markov Chain

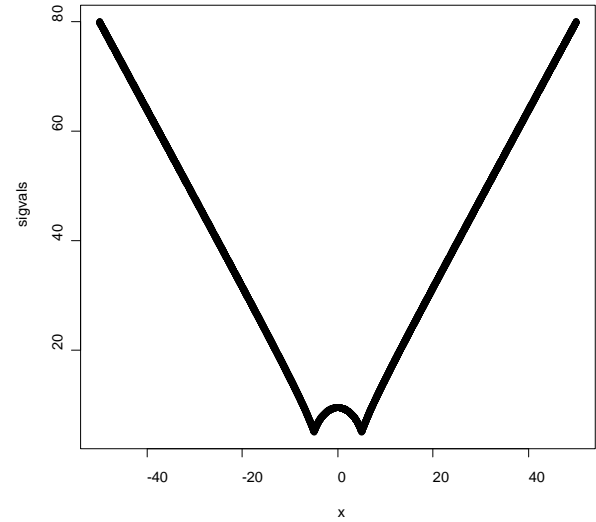
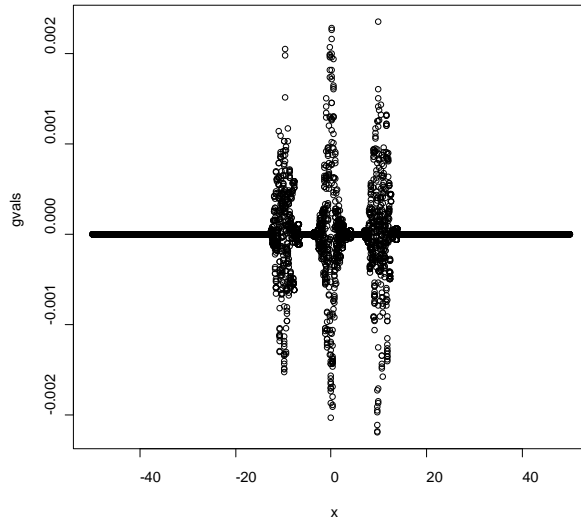
it takes 615.190000 seconds to test the local acceptance

1

[1] 12.13882
[1] 0.09072717
[1] 18.01603

2.3.3.21 case 176 $\eta_n = \frac{1}{(n+5)^{0.8}}$, height = 0.1, width = 2, $C = 0.1, \gamma = 0.5$ with fixed

bandwidth $b_n = 1$



Accepted 22542 out of 100000 (22.542%).

final beta = 1.624557

alpha(0.000000) is 0.194300

alpha(2.000000) is 0.423500

alpha(5.000000) is 0.975500

alpha(8.000000) is 0.349000

alpha(10.000000) is 0.161200

alpha(13.000000) is 0.310700

alpha(15.000000) is 0.401300

alpha(20.000000) is 0.394200

alpha(30.000000) is 0.396300

alpha(50.000000) is 0.403000

it takes 705.820000 seconds to run the adaptation algorithm

it takes 308.400000 seconds to compute g and sigma

it takes 175.690000 seconds to generate the first Markov Chain

it takes 175.800000 seconds to generate the second Markov Chain

it takes 175.520000 seconds to generate the third Markov Chain

it takes 175.250000 seconds to generate the fourth Markov Chain

it takes 175.900000 seconds to generate the fifth Markov Chain

it takes 1031.100000 seconds to test the local acceptance

1

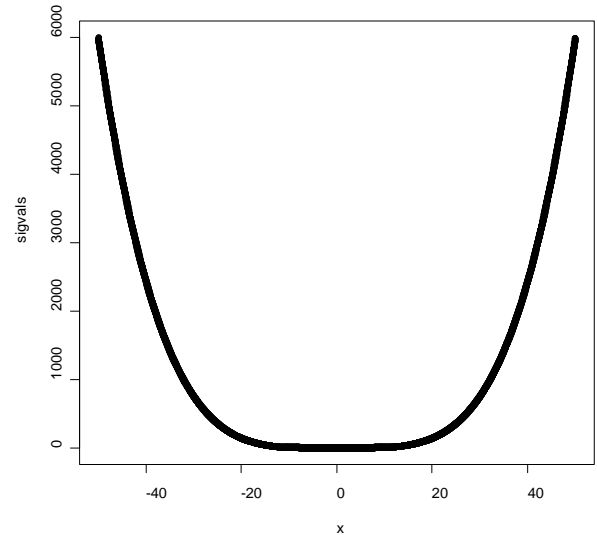
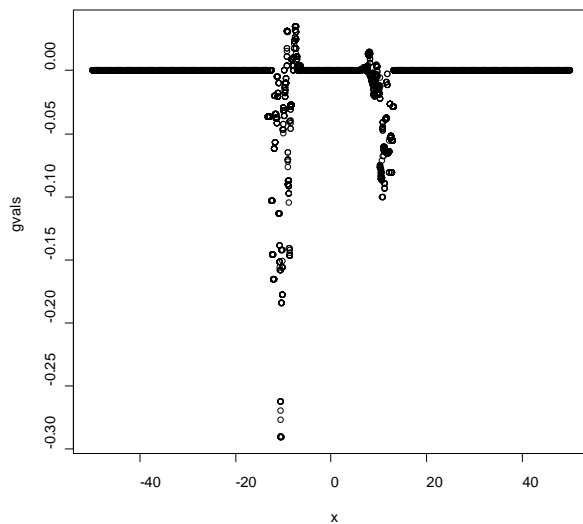
[1] 12.53176

[1] 0.09117011

[1] 17.39284

2.3.4 kernel function $K(x) = \begin{cases} 0, & |x| \geq 2 * width \text{ or } |x| \leq width \\ 1, & width < |x| < 2 * width \end{cases}$

2.3.4.1 case 177 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, C = 1, $\gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 24315 out of 100000 (24.315%).

final beta = -6.929724

alpha(0.000000) is 0.813800

alpha(2.000000) is 0.753800

alpha(5.000000) is 0.955900

alpha(8.000000) is 0.620100

alpha(10.000000) is 0.186500

alpha(13.000000) is 0.128900

alpha(15.000000) is 0.113300

alpha(20.000000) is 0.067100

alpha(30.000000) is 0.023400

alpha(50.000000) is 0.005600

it takes 125.482000 seconds to run the adaptation algorithm

it takes 55.504000 seconds to compute g and sigma

it takes 18.709000 seconds to generate the first Markov Chain

it takes 19.010000 seconds to generate the second Markov Chain

it takes 19.325000 seconds to generate the third Markov Chain

it takes 18.488000 seconds to generate the fourth Markov Chain

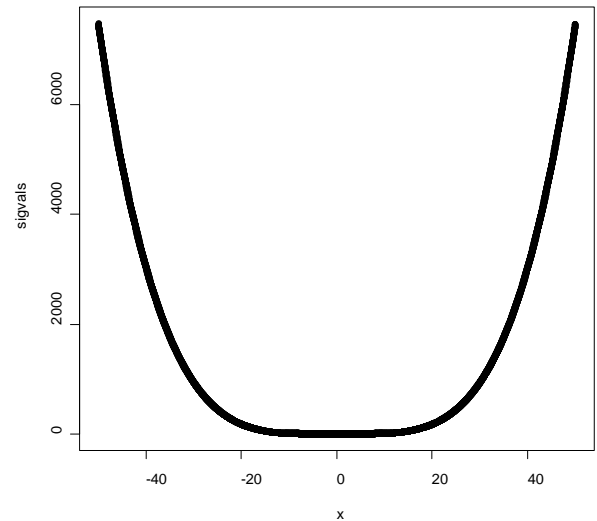
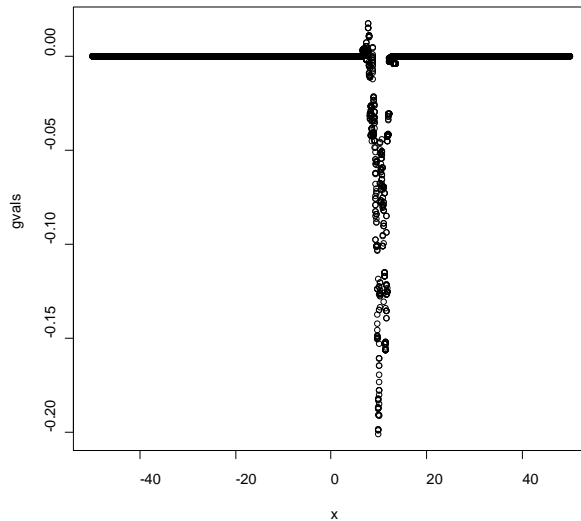
it takes 18.261000 seconds to generate the fifth Markov Chain

it takes 264.813000 seconds to test the local acceptance

1

[1] 91.28675
[1] 0.3161601
[1] 1.140038

2.3.4.2 case 178 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C = 10$, $\gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 77934 out of 100000 (77.934%).

final beta = -11.312342

alpha(0.000000) is 0.777300

alpha(2.000000) is 0.738200

alpha(5.000000) is 0.711200

alpha(8.000000) is 0.594200

alpha(10.000000) is 0.167200

alpha(13.000000) is 0.120000

alpha(15.000000) is 0.099900

alpha(20.000000) is 0.057700

alpha(30.000000) is 0.017300

alpha(50.000000) is 0.004100

it takes 124.417000 seconds to run the adaptation algorithm

it takes 55.553000 seconds to compute g and sigma

it takes 20.010000 seconds to generate the first Markov Chain

it takes 19.438000 seconds to generate the second Markov Chain

it takes 18.998000 seconds to generate the third Markov Chain

it takes 19.289000 seconds to generate the fourth Markov Chain

it takes 19.039000 seconds to generate the fifth Markov Chain

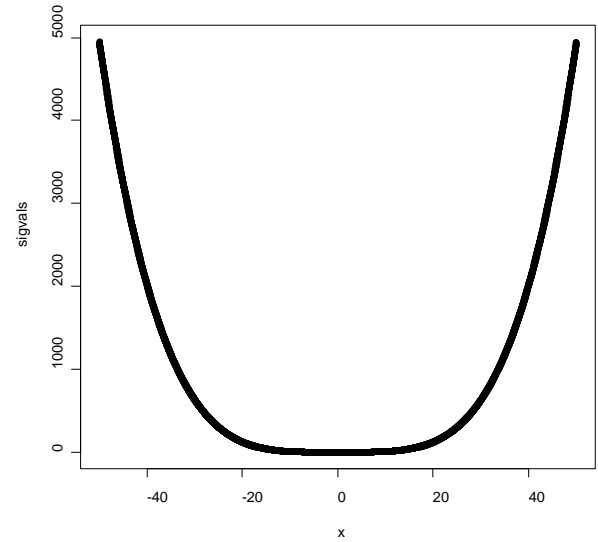
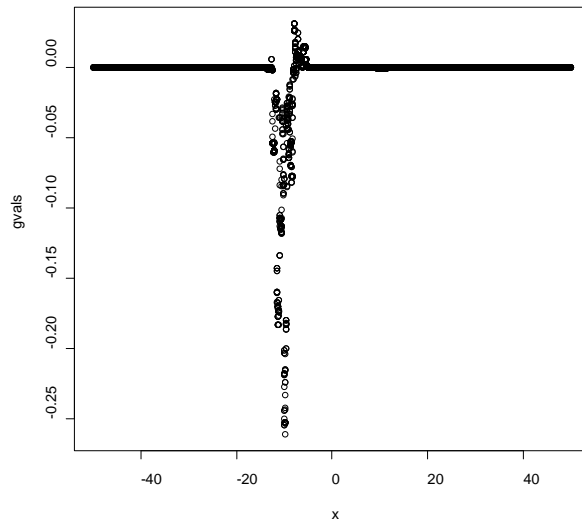
it takes 274.555000 seconds to test the local acceptance

1

[1] 17.12798
[1] 0.01378514
[1] 0.2614159

2.3.4.3 case 179 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C = 0.1, \gamma = 2$ with fixed bandwidth

$b_n = 1$



Accepted 23497 out of 100000 (23.497%).

final beta = -2.523769

alpha(0.000000) is 0.708600

alpha(2.000000) is 0.683200

alpha(5.000000) is 0.989400

alpha(8.000000) is 0.587200

alpha(10.000000) is 0.179800

alpha(13.000000) is 0.142000

alpha(15.000000) is 0.132400

alpha(20.000000) is 0.080800

alpha(30.000000) is 0.028700

alpha(50.000000) is 0.007200

it takes 124.323000 seconds to run the adaptation algorithm

it takes 55.545000 seconds to compute g and sigma

it takes 19.766000 seconds to generate the first Markov Chain

it takes 19.247000 seconds to generate the second Markov Chain

it takes 19.919000 seconds to generate the third Markov Chain

it takes 19.192000 seconds to generate the fourth Markov Chain

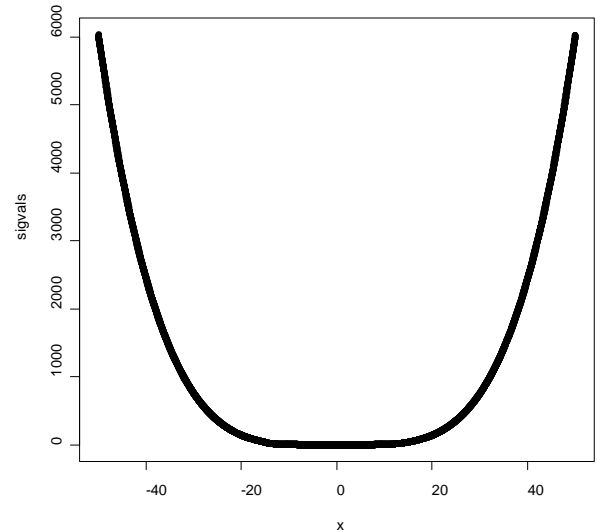
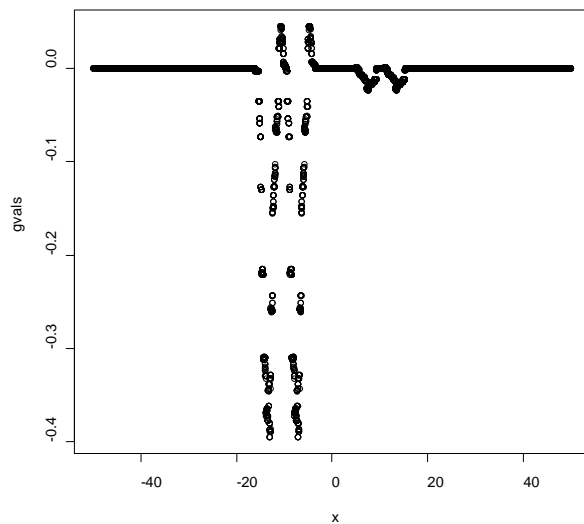
it takes 20.575000 seconds to generate the fifth Markov Chain

it takes 260.328000 seconds to test the local acceptance

1

[1] 91.63516
[1] 0.3196954
[1] 1.21477

2.3.4.4 case 180 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 2, $C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 23808 out of 100000 (23.808%).

final beta = -6.923705

alpha(0.000000) is 0.816100

alpha(2.000000) is 0.754200

alpha(5.000000) is 0.954400

alpha(8.000000) is 0.617700

alpha(10.000000) is 0.178500

alpha(13.000000) is 0.133000

alpha(15.000000) is 0.116000

alpha(20.000000) is 0.066300

alpha(30.000000) is 0.023700

alpha(50.000000) is 0.005400

it takes 124.565000 seconds to run the adaptation algorithm

it takes 55.222000 seconds to compute g and sigma

it takes 19.552000 seconds to generate the first Markov Chain

it takes 18.824000 seconds to generate the second Markov Chain

it takes 18.883000 seconds to generate the third Markov Chain

it takes 18.746000 seconds to generate the fourth Markov Chain

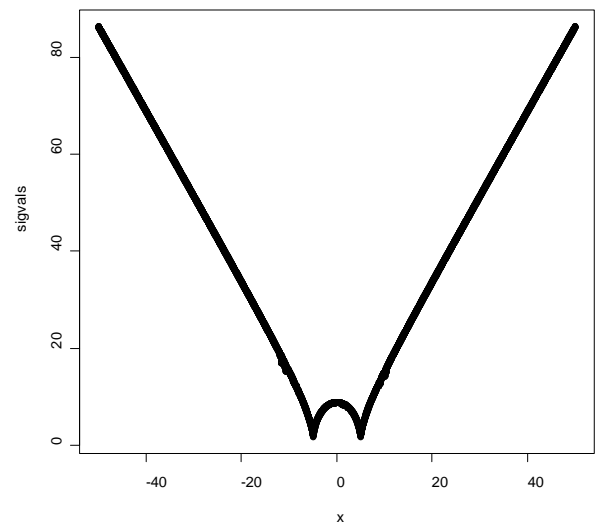
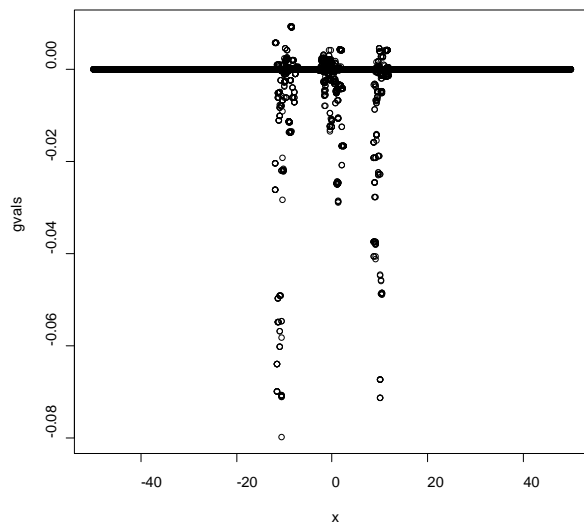
it takes 19.450000 seconds to generate the fifth Markov Chain

it takes 265.105000 seconds to test the local acceptance

1

[1] 88.68445
[1] 0.3080952
[1] 1.326619

2.3.4.5 case 181 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.1, $C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$



Accepted 22533 out of 100000 (22.533%).

final beta = 0.550883

alpha(0.000000) is 0.203900

alpha(2.000000) is 0.442800

alpha(5.000000) is 0.988000

alpha(8.000000) is 0.358500

alpha(10.000000) is 0.163500

alpha(13.000000) is 0.291900

alpha(15.000000) is 0.362400

alpha(20.000000) is 0.385800

alpha(30.000000) is 0.384800

alpha(50.000000) is 0.371000

it takes 124.380000 seconds to run the adaptation algorithm

it takes 55.442000 seconds to compute g and sigma

it takes 20.841000 seconds to generate the first Markov Chain

it takes 21.312000 seconds to generate the second Markov Chain

it takes 21.030000 seconds to generate the third Markov Chain

it takes 20.597000 seconds to generate the fourth Markov Chain

it takes 21.002000 seconds to generate the fifth Markov Chain

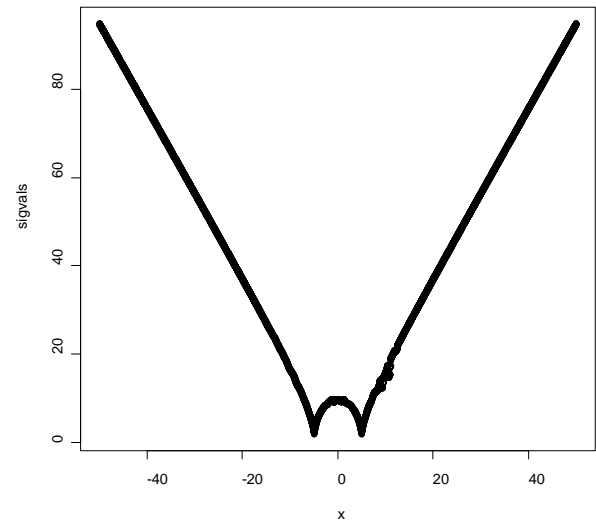
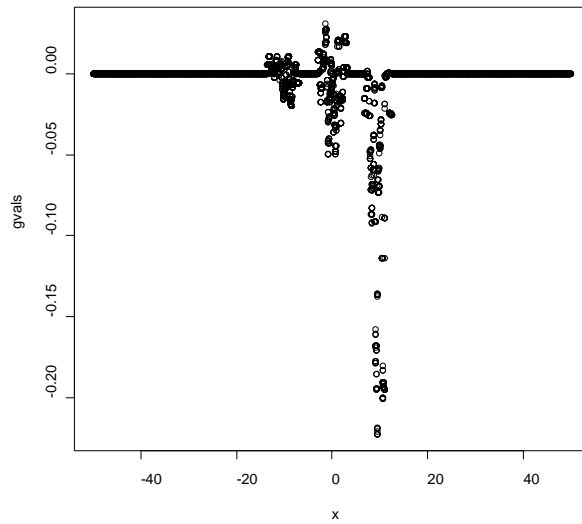
it takes 179.464000 seconds to test the local acceptance

1

[1] 12.88688
[1] 0.09355521
[1] 17.49032

2.3.4.6 case 182 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C = 1, \gamma = 0.5$ with fixed bandwidth

$b_n = 1$



Accepted 21843 out of 100000 (21.843%).

final beta = 0.644714

alpha(0.000000) is 0.180400

alpha(2.000000) is 0.421000

alpha(5.000000) is 0.989900

alpha(8.000000) is 0.352300

alpha(10.000000) is 0.160300

alpha(13.000000) is 0.285800

alpha(15.000000) is 0.348500

alpha(20.000000) is 0.356200

alpha(30.000000) is 0.348300

alpha(50.000000) is 0.359800

it takes 123.740000 seconds to run the adaptation algorithm

it takes 54.826000 seconds to compute g and sigma

it takes 21.707000 seconds to generate the first Markov Chain

it takes 22.307000 seconds to generate the second Markov Chain

it takes 22.245000 seconds to generate the third Markov Chain

it takes 22.370000 seconds to generate the fourth Markov Chain

it takes 21.890000 seconds to generate the fifth Markov Chain

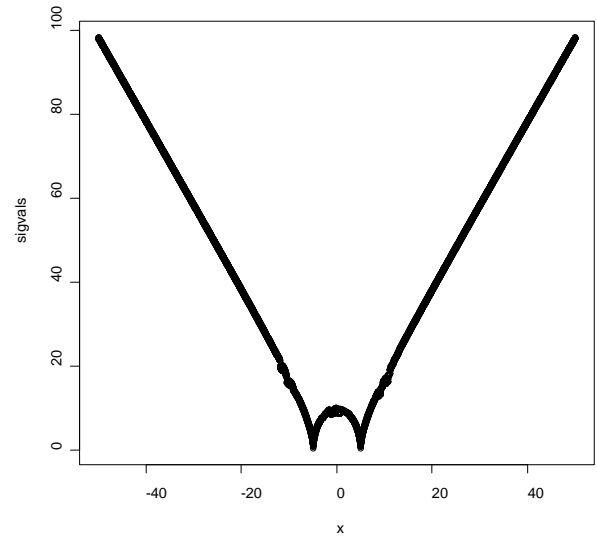
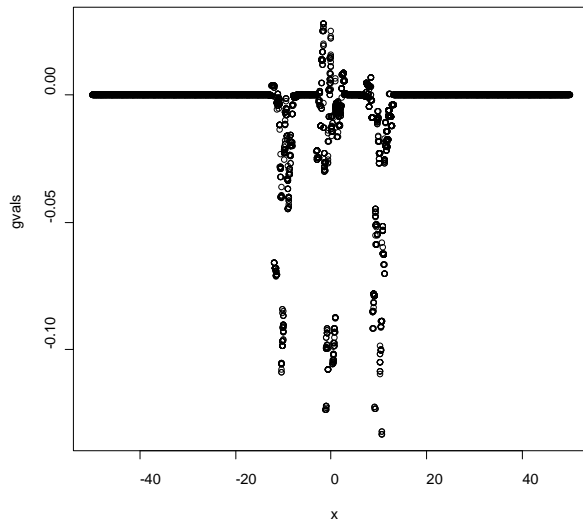
it takes 186.859000 seconds to test the local acceptance

1

[1] 12.92349
 [1] 0.09353589
 [1] 17.78533

2.3.4.7 case 183 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C = 10$, $\gamma = 0.5$ with fixed bandwidth

$b_n = 1$



Accepted 21715 out of 100000 (21.715%).

final beta = -0.470452

alpha(0.000000) is 0.182300

alpha(2.000000) is 0.417700

alpha(5.000000) is 0.854200

alpha(8.000000) is 0.343400

alpha(10.000000) is 0.157600

alpha(13.000000) is 0.283400

alpha(15.000000) is 0.336300

alpha(20.000000) is 0.341500

alpha(30.000000) is 0.349800

alpha(50.000000) is 0.338600

it takes 123.765000 seconds to run the adaptation algorithm

it takes 54.681000 seconds to compute g and sigma

it takes 21.766000 seconds to generate the first Markov Chain

it takes 22.020000 seconds to generate the second Markov Chain

it takes 21.988000 seconds to generate the third Markov Chain

it takes 22.060000 seconds to generate the fourth Markov Chain

it takes 22.170000 seconds to generate the fifth Markov Chain

it takes 185.693000 seconds to test the local acceptance

1

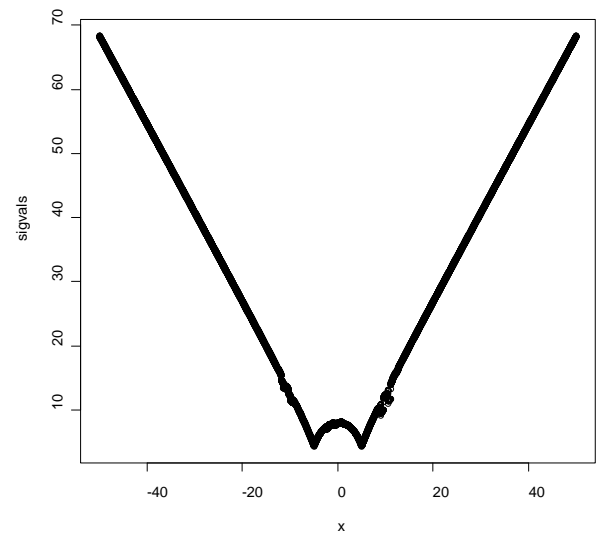
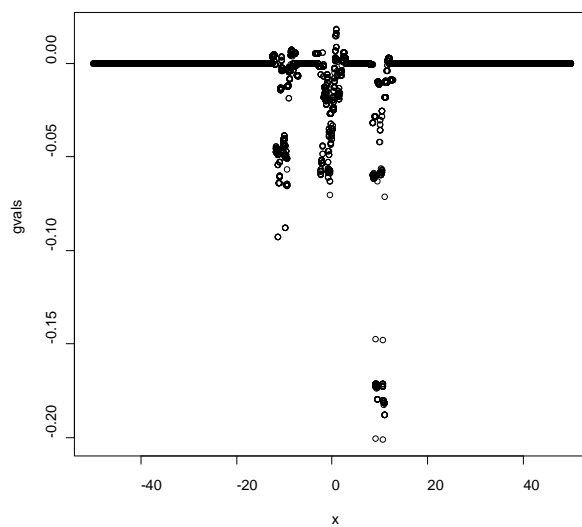
```

> source("xlist5");plot(xlist[(B+1):M],type="l");varfact(xlist[(B+1):M]);sd(xlist[(B+1):M]) /
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
[1] 12.94596
[1] 0.09434861
[1] 18.22428

```

2.3.4.8 case 184 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C = 0.1, \gamma = 0.5$ with fixed bandwidth

$b_n = 1$



Accepted 24373 out of 100000 (24.373%).

final beta = 1.466264

alpha(0.000000) is 0.210200

alpha(2.000000) is 0.455500

alpha(5.000000) is 0.990300

alpha(8.000000) is 0.371200

alpha(10.000000) is 0.176600

alpha(13.000000) is 0.324300

alpha(15.000000) is 0.422000

alpha(20.000000) is 0.431700

alpha(30.000000) is 0.422100

alpha(50.000000) is 0.429400

it takes 124.755000 seconds to run the adaptation algorithm

it takes 55.057000 seconds to compute g and sigma

it takes 19.595000 seconds to generate the first Markov Chain

it takes 20.079000 seconds to generate the second Markov Chain

it takes 20.256000 seconds to generate the third Markov Chain

it takes 19.634000 seconds to generate the fourth Markov Chain

it takes 19.287000 seconds to generate the fifth Markov Chain

it takes 165.799000 seconds to test the local acceptance

|

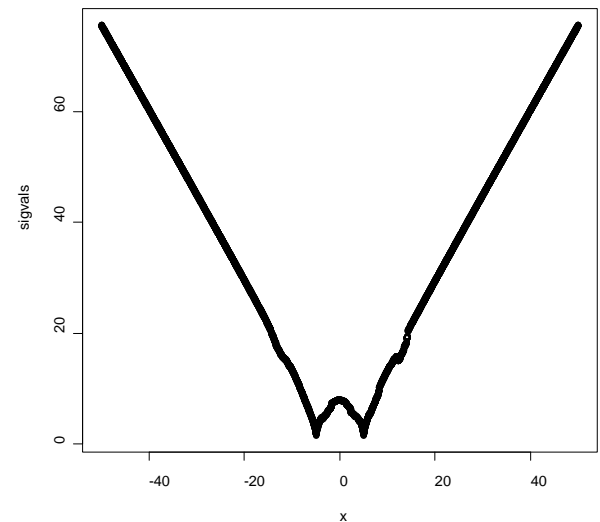
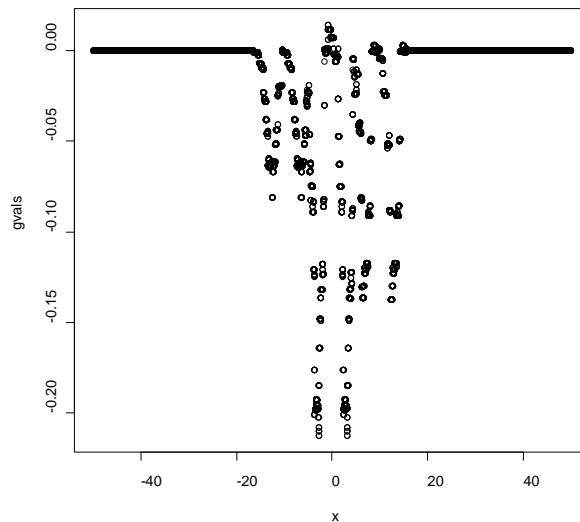
```
sqrt(M-B) * sqrt( varfact(xlist[(B+1):M]) );asjd(xlist[(B+1):M]);
```

```
[1] 14.67285
```

```
[1] 0.09916782
```

```
[1] 16.07759
```

2.3.4.9 case 185 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 2, $C = 1, \gamma = 0.5$ with fixed bandwidth $b_n = 1$



Accepted 24236 out of 100000 (24.236%).

final beta = 0.419881

alpha(0.000000) is 0.225300

alpha(2.000000) is 0.469700

alpha(5.000000) is 0.985200

alpha(8.000000) is 0.385800

alpha(10.000000) is 0.166800

alpha(13.000000) is 0.313200

alpha(15.000000) is 0.379700

alpha(20.000000) is 0.408500

alpha(30.000000) is 0.409600

alpha(50.000000) is 0.403300

it takes 124.924000 seconds to run the adaptation algorithm

it takes 55.695000 seconds to compute g and sigma

it takes 19.998000 seconds to generate the first Markov Chain

it takes 19.831000 seconds to generate the second Markov Chain

it takes 19.483000 seconds to generate the third Markov Chain

it takes 21.227000 seconds to generate the fourth Markov Chain

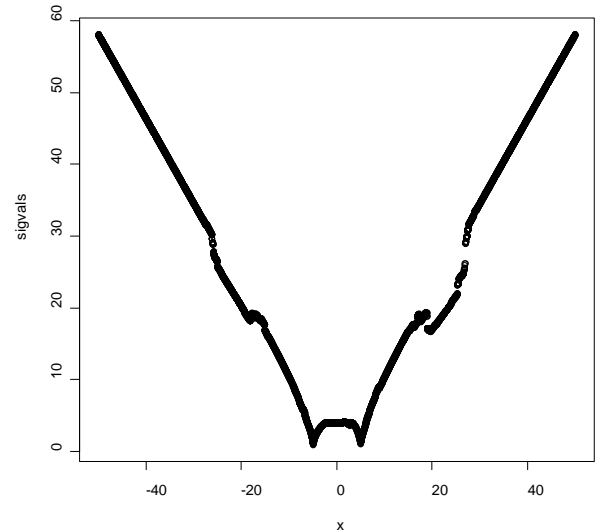
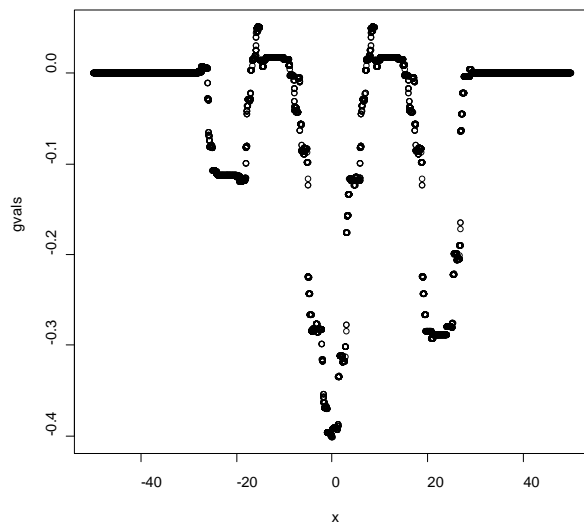
it takes 22.338000 seconds to generate the fifth Markov Chain

it takes 169.441000 seconds to test the local acceptance

1

[1] 14.55493
[1] 0.09914065
[1] 16.28342

2.3.4.10 case 186 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 8, $C = 1$, $\gamma = 0.5$ with fixed bandwidth $b_n = 1$



Accepted 24475 out of 100000 (24.475%).

final beta = 0.154851

alpha(0.000000) is 0.285300

alpha(2.000000) is 0.494800

alpha(5.000000) is 0.980600

alpha(8.000000) is 0.380900

alpha(10.000000) is 0.131100

alpha(13.000000) is 0.302800

alpha(15.000000) is 0.395800

alpha(20.000000) is 0.480100

alpha(30.000000) is 0.460000

alpha(50.000000) is 0.446200

it takes 124.161000 seconds to run the adaptation algorithm

it takes 55.555000 seconds to compute g and sigma

it takes 19.451000 seconds to generate the first Markov Chain

it takes 19.152000 seconds to generate the second Markov Chain

it takes 19.122000 seconds to generate the third Markov Chain

it takes 19.160000 seconds to generate the fourth Markov Chain

it takes 19.256000 seconds to generate the fifth Markov Chain

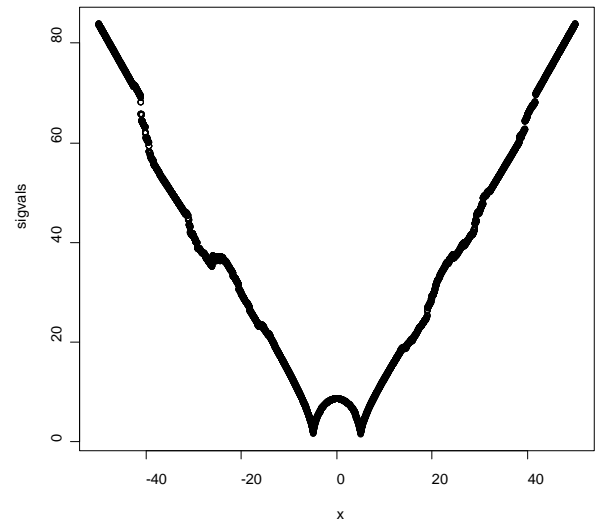
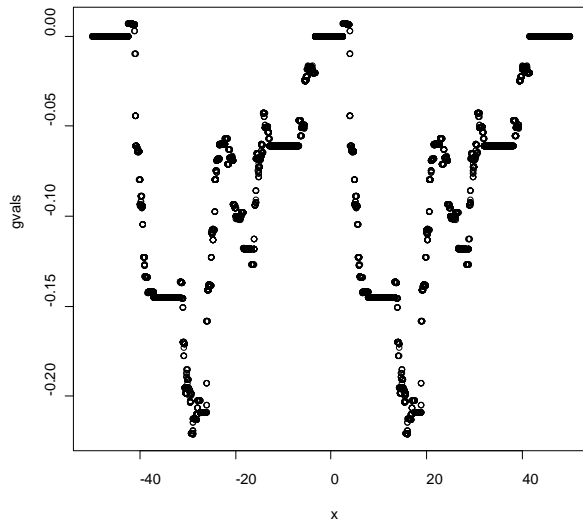
it takes 155.375000 seconds to test the local acceptance

1

[1] 29.62488
[1] 0.1409916
[1] 7.644844

2.3.4.11 case 187 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 15, $C = 1, \gamma = 0.5$ with fixed bandwidth

$b_n = 1$



Accepted 23608 out of 100000 (23.608%).

final beta = 0.522466

alpha(0.000000) is 0.205600

alpha(2.000000) is 0.439000

alpha(5.000000) is 0.985900

alpha(8.000000) is 0.384500

alpha(10.000000) is 0.174000

alpha(13.000000) is 0.318700

alpha(15.000000) is 0.409000

alpha(20.000000) is 0.417200

alpha(30.000000) is 0.402000

alpha(50.000000) is 0.386800

it takes 125.527000 seconds to run the adaptation algorithm

it takes 56.435000 seconds to compute g and sigma

it takes 21.357000 seconds to generate the first Markov Chain

it takes 22.341000 seconds to generate the second Markov Chain

it takes 20.670000 seconds to generate the third Markov Chain

it takes 19.801000 seconds to generate the fourth Markov Chain

it takes 19.573000 seconds to generate the fifth Markov Chain

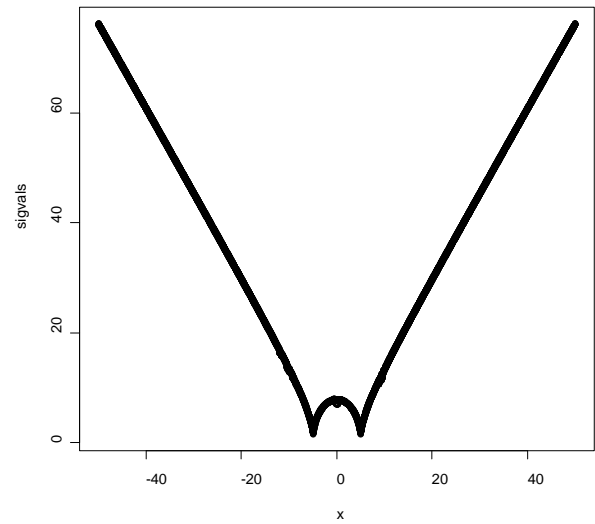
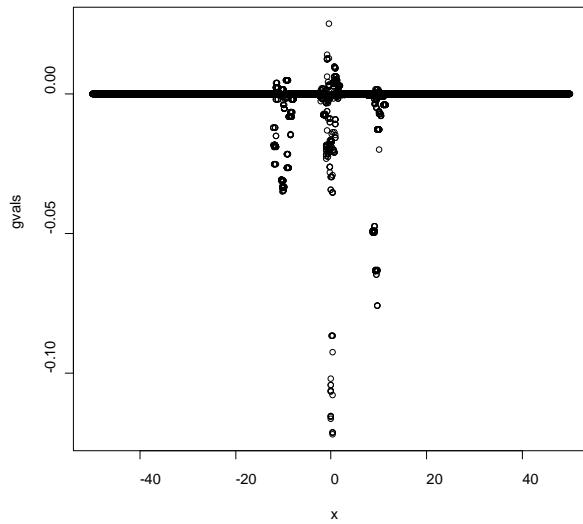
it takes 171.328000 seconds to test the local acceptance

1

[1] 13.02177
[1] 0.09372085
[1] 16.78987

2.3.4.12 case 188 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.1, $C = 1$, $\gamma = 0.5$ with fixed bandwidth

$b_n = 1$



Accepted 23881 out of 100000 (23.881%).

final beta = 0.426753

alpha(0.000000) is 0.217900

alpha(2.000000) is 0.453400

alpha(5.000000) is 0.985100

alpha(8.000000) is 0.373600

alpha(10.000000) is 0.163700

alpha(13.000000) is 0.308000

alpha(15.000000) is 0.388000

alpha(20.000000) is 0.410700

alpha(30.000000) is 0.401100

alpha(50.000000) is 0.408400

it takes 126.962000 seconds to run the adaptation algorithm

it takes 56.884000 seconds to compute g and sigma

it takes 20.672000 seconds to generate the first Markov Chain

it takes 19.828000 seconds to generate the second Markov Chain

it takes 19.207000 seconds to generate the third Markov Chain

it takes 20.404000 seconds to generate the fourth Markov Chain

it takes 20.557000 seconds to generate the fifth Markov Chain

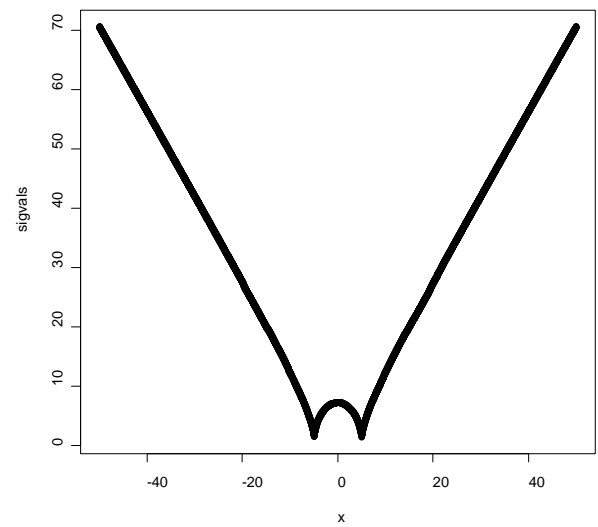
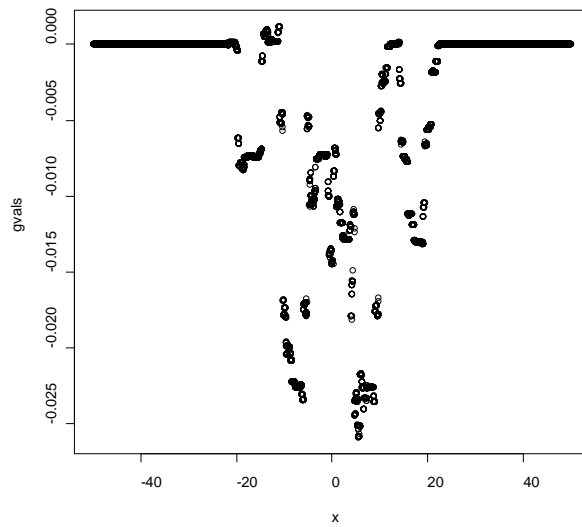
it takes 172.155000 seconds to test the local acceptance

1

[1] 14.18767
[1] 0.09807043
[1] 16.43629

2.3.4.13 case 190 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C = 1, \gamma = 0.5$ with fixed bandwidth

$b_n = 10$



Accepted 24986 out of 100000 (24.986%).

final beta = 0.348742

alpha(0.000000) is 0.230200

alpha(2.000000) is 0.466600

alpha(5.000000) is 0.986900

alpha(8.000000) is 0.387100

alpha(10.000000) is 0.173500

alpha(13.000000) is 0.312200

alpha(15.000000) is 0.406000

alpha(20.000000) is 0.421100

alpha(30.000000) is 0.419100

alpha(50.000000) is 0.425200

it takes 128.936000 seconds to run the adaptation algorithm

it takes 58.141000 seconds to compute g and sigma

it takes 19.376000 seconds to generate the first Markov Chain

it takes 20.517000 seconds to generate the second Markov Chain

it takes 21.659000 seconds to generate the third Markov Chain

it takes 21.121000 seconds to generate the fourth Markov Chain

it takes 20.021000 seconds to generate the fifth Markov Chain

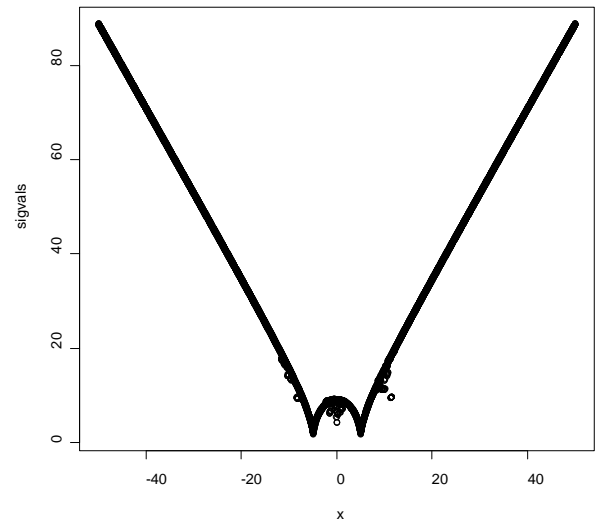
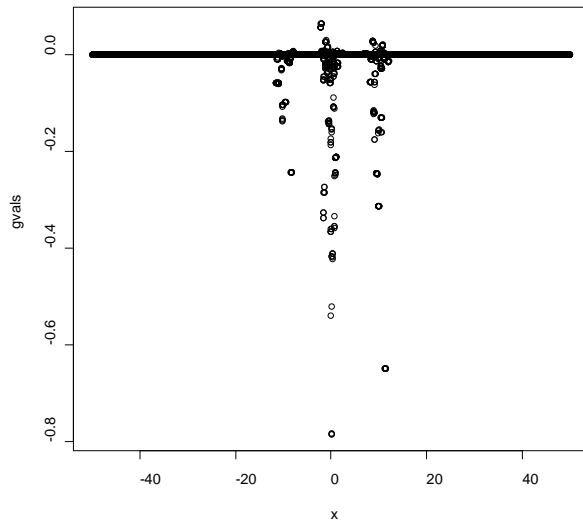
it takes 172.470000 seconds to test the local acceptance

1

[1] 14.28311
[1] 0.09859633
[1] 15.87459

2.3.4.14 case 191 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C = 1$, $\gamma = 0.5$ with fixed bandwidth

$b_n = 0.1$



Accepted 22412 out of 100000 (22.412%).

final beta = 0.580059

alpha(0.000000) is 0.192800

alpha(2.000000) is 0.430700

alpha(5.000000) is 0.987700

alpha(8.000000) is 0.353300

alpha(10.000000) is 0.162300

alpha(13.000000) is 0.295400

alpha(15.000000) is 0.371700

alpha(20.000000) is 0.374300

alpha(30.000000) is 0.376500

alpha(50.000000) is 0.372300

it takes 129.581000 seconds to run the adaptation algorithm

it takes 57.591000 seconds to compute g and sigma

it takes 21.501000 seconds to generate the first Markov Chain

it takes 21.500000 seconds to generate the second Markov Chain

it takes 21.806000 seconds to generate the third Markov Chain

it takes 21.157000 seconds to generate the fourth Markov Chain

it takes 21.346000 seconds to generate the fifth Markov Chain

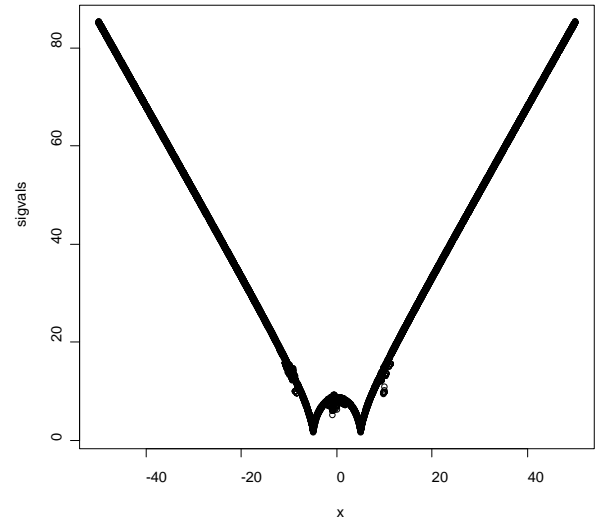
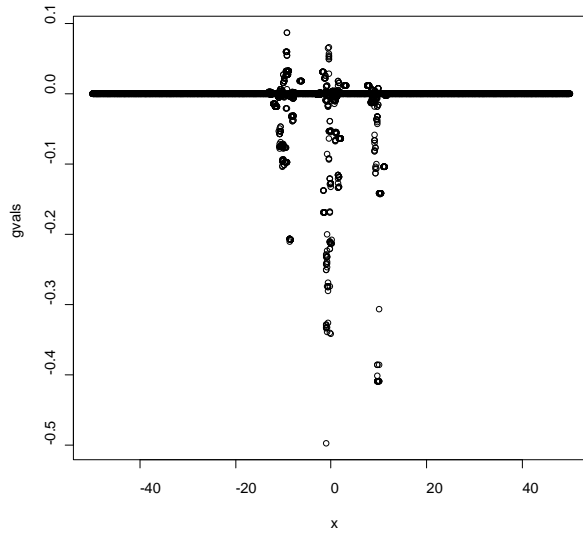
it takes 187.114000 seconds to test the local acceptance

1

[1] 13.28312
 [1] 0.09494838
 [1] 17.80852

2.3.4.15 case 192 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, $C = 1, \gamma = 0.5$ with decreasing bandwidth

$$b_n = \frac{1}{n^{0.2}}$$



Accepted 23078 out of 100000 (23.078%).

final beta = 0.539463

alpha(0.000000) is 0.205900

alpha(2.000000) is 0.454600

alpha(5.000000) is 0.986500

alpha(8.000000) is 0.355300

alpha(10.000000) is 0.160800

alpha(13.000000) is 0.296500

alpha(15.000000) is 0.365300

alpha(20.000000) is 0.382200

alpha(30.000000) is 0.379000

alpha(50.000000) is 0.373800

it takes 129.994000 seconds to run the adaptation algorithm

it takes 57.687000 seconds to compute g and sigma

it takes 20.977000 seconds to generate the first Markov Chain

it takes 21.497000 seconds to generate the second Markov Chain

it takes 23.012000 seconds to generate the third Markov Chain

it takes 21.125000 seconds to generate the fourth Markov Chain

it takes 20.858000 seconds to generate the fifth Markov Chain

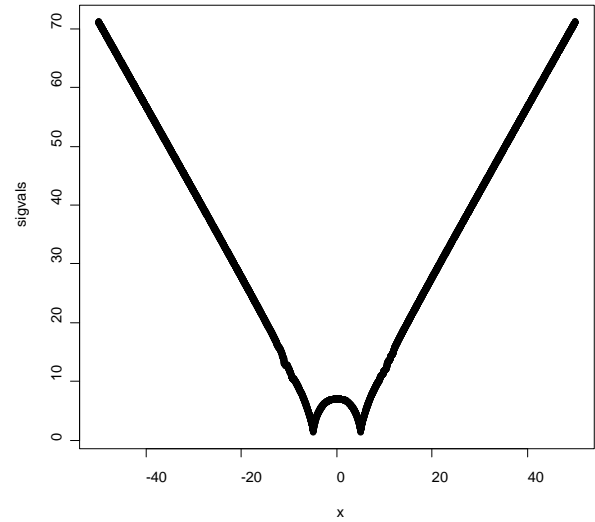
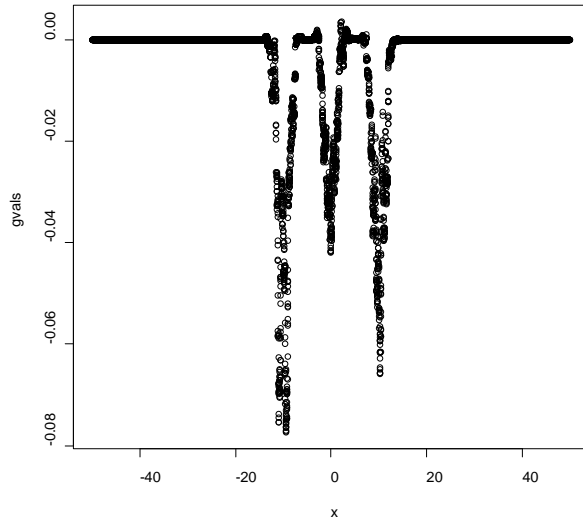
it takes 186.591000 seconds to test the local acceptance

1

[1] 12.70254
[1] 0.09291843
[1] 17.29666

2.3.4.16 case 193 $\eta_n = \frac{1}{(n+5)^{0.8}}$, width = 0.5, C = 1, $\gamma = 0.5$ with fixed bandwidth

$b_n = 1$



Accepted 24964 out of 100000 (24.964%).

final beta = 0.357821

alpha(0.000000) is 0.238000

alpha(2.000000) is 0.464800

alpha(5.000000) is 0.984500

alpha(8.000000) is 0.392800

alpha(10.000000) is 0.164700

alpha(13.000000) is 0.311300

alpha(15.000000) is 0.394600

alpha(20.000000) is 0.421600

alpha(30.000000) is 0.425200

alpha(50.000000) is 0.421500

it takes 124.575000 seconds to run the adaptation algorithm

it takes 55.922000 seconds to compute g and sigma

it takes 19.610000 seconds to generate the first Markov Chain

it takes 19.339000 seconds to generate the second Markov Chain

it takes 19.417000 seconds to generate the third Markov Chain

it takes 19.444000 seconds to generate the fourth Markov Chain

it takes 19.706000 seconds to generate the fifth Markov Chain

it takes 163.433000 seconds to test the local acceptance

1

[1] 15.27249

[1] 0.101742

[1] 15.44641

2.3.5 constant $\sigma(x) = C$

```
> source("R1: sigma=C")
```

```
ran Metropolis algorithm for 1e+05 iterations, with burn-in 10000
```

```
acceptance rate = 0.2342
```

```
varfact is about 14.15845
```

```
standard error is about 0.09767042
```

```
average squared jump distance is about 15.54288
```



1

1

2.3.6 varfact comparison

kernel function $K(x) = e^{-\frac{ x ^{\alpha_1}}{\alpha_2}}$										
α_1	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run	
1	1	2	1	$\frac{1}{(n+5)^{0.5}}$	16.26846	14.57988	16.42912	86.86853	15.50366	
10					18.74016	18.43029	90.07437	91.53203	90.90502	
0.1					94.37575	93.97776	94.89696	93.97518	27.86239	
1		0.5			10	15.41126	16.27198	15.48657	15.75304	16.19362
10						14.65439	15.18358	13.33354	14.90325	14.06277
0.1						13.48694	12.5845	13.65186	13.35255	12.4874
1	10		1	12.64651	12.96737	12.65248	13.67789	12.82574		
0.1				0.1	12.92113	13.57182	14.02518	14.24815	13.62849	
					13.43403	13.49145	13.51024	13.90427	13.35211	
	10	13.31778	13.00656		12.33834	13.99267	13.74377			
	1	0.1	17.80311	15.6759	16.52688	16.10023	17.91262			
		$\frac{1}{n^{0.2}}$	13.21089	12.84258	13.86328	13.80823	14.55637			
		1	$\frac{1}{(n+5)^{0.8}}$	14.00937	13.22654	12.34942	13.38838	13.34282		

The best case is:

case 133 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 10, \gamma = 0.5$ with fixed bandwidth $b_n = 1$

kernel function $K(x) = \frac{1}{1 + \alpha_1 x ^{\alpha_2}}$									
α_1	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
1	1	2	1	$\frac{1}{(n+5)^{0.5}}$	83.99893	84.04238	83.67897	82.42829	13.66704
10					90.40186	89.71504	19.61744	90.32034	91.49129
0.1					86.46781	17.73197	87.82512	16.51479	88.28712
1	0.1	0.5			89.07015	9.307463	9.667522	88.64032	90.71062
	10				89.72487	89.13216	89.81371	88.89575	89.95243
	10				13.68547	13.03615	14.32362	14.0087	14.27748
0.1	1		14.44041	13.52041	13.55925	13.76832	12.43203		
			15.82955	15.23739	14.52674	15.13927	14.78932		
			10	13.3392	12.24885	13.38762	13.53404	13.72235	
10	0.1	15.14332	15.4522	14.88309	15.50852	14.91846			
	10	13.4966	12.38203	14.30898	14.33035	13.31069			
	1	16.47299	15.41183	15.58338	16.51207	16.61734			

		0.5	10		20.44234	21.46451	19.50774	21.96715	21.61043
			0.1		17.52911	18.1089	17.64972	17.20674	17.48015
			$\frac{1}{n^{0.2}}$		17.33197	17.97494	17.86626	16.96093	17.77595
			$\frac{1}{(n+5)^{0.8}}$		13.86666	13.45143	13.59058	13.00682	12.96691

The best case is

case 148 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 10, \gamma = 0.5$ with fixed bandwidth $b_n = 1$

kernel function $K(x) = \begin{cases} 0, & x \geq 2 * width \\ -1 * height, & width < x < 2 * width \\ 1 * height, & x \leq width \end{cases}$													
height	width	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run			
0.5	0.5	1	0.5	1	$\frac{1}{(n+5)^{0.5}}$	17.77124	17.56957	17.15754	18.71177	17.85295			
		10				14.5163	13.97646	14.53291	15.26343	13.60182			
		0.1				14.47679	13.60182	12.84939	13.38512	12.99476			
		2				13.44326	14.87757	12.65287	13.89331	13.87151			
		5				14.77333	15.53957	15.15622	14.71878	14.70888			
10	22.74932	21.23517	21.51277	22.1724		21.28494							
0.1	0.5	0.1	0.1	1		13.12834	12.62207	13.73153	13.44643	13.29028			
						2	12.32118	12.50984	12.6972	13.12091	13.51672		
						8	13.52936	12.9048	12.80928	12.16642	13.63757		
						15	15.11477	15.55721	15.568	16.00962	15.62307		
						0.1	13.27735	13.54215	14.14683	13.06055	13.0853		
	2		0.5	0.1		0.5	1	14.92786	15.62123	15.38949	16.17938	14.62442	
								10	12.76971	12.85744	12.76055	12.98399	12.96732
								0.1	13.06958	13.49213	13.10409	13.37818	12.68868
								$\frac{1}{n^{0.2}}$	12.83056	12.70031	13.2164	12.35389	12.13882
					1			13.6103	13.25533	12.66344	12.985	12.53176	

The best case is :

case 173 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.1, width = 2, C = 0.1, $\gamma = 0.5$ with fixed bandwidth

$b_n = 10$

$$\text{kernel function } K(x) = \begin{cases} 0, & |x| \geq 2 * \text{width} \text{ or } |x| \leq \text{width} \\ 1, & \text{width} < |x| < 2 * \text{width} \end{cases}$$

width	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run	
0.5	1	2	1	$\frac{1}{(n+5)^{0.5}}$	21.4667	91.91048	91.56507	91.52051	91.28675	
	10				83.076957	17.25225	84.51131	16.42809	17.12798	
	0.1				91.2014	91.82045	91.54555	12.36587	91.63516	
2	1	89.2247	19.79872		88.87049	20.77564	88.68445			
0.1		12.98	13.09344		12.8819	12.88677	12.88688			
0.5	1	0.5	1		12.43654	12.98527	12.4032	12.94385	12.92349	
	10				13.1587	13.1709	12.11507	13.44184	12.94596	
	0.1				15.58158	14.4539	15.0466	14.11616	14.67285	
2	1		14.21562		14.09779	14.64326	15.09419	14.55493		
8			29.03847		29.74645	30.26822	31.29497	29.62488		
15			13.74205		14.75585	13.3168	13.31694	13.02177		
0.1			14.67465		14.47777	14.09109	4.44332	14.18767		
0.5			1		10	14.74344	13.17465	14.85009	13.66765	14.28311
					0.1	12.6542	13.1784	13.38414	12.82934	13.28312
					$\frac{1}{n^{0.2}}$	13.92314	13.61308	13.15229	13.74245	12.70254
1	$\frac{1}{(n+5)^{0.8}}$		14.60853	14.70849	5.70829	15.25032	15.27249			

The best case is:

case 182 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, C = 1, $\gamma = 0.5$ with fixed bandwidth $b_n = 1$

constant $\sigma(x) = C$				
First run	Second run	Third run	Fourth run	Fifth run
14.15845	15.31856	13.73391	15.47598	14.98496

2.3.7 variance comparison

kernel function $K(x) = e^{-\frac{ x ^{\alpha_1}}{\alpha_2}}$									
α_1	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
1	1	2	1	$\frac{1}{(n+5)^{0.5}}$	0.01353855	0.01258219	0.01373153	0.3112750	0.01314821
10					0.01458137	0.01433285	0.3162902	0.3189283	0.3148806
0.1					0.3227189	0.324662	0.3258069	0.3235092	0.01766048
1		0.5			0.1014592	0.1061646	0.1022247	0.1033099	0.1044669
10					0.1005178	0.1018522	0.0955402	0.09975748	0.096773
0.1					0.09539856	0.09189677	0.09668277	0.09525747	0.09103119
1	10		0.09292519	0.09330761	0.0922181	0.09732262	0.09345714		
0.1	0.1		0.09362208	0.09749066	0.09749066	0.09815398	0.09637123		
	1	0.09595994	0.09619656	0.09564208	0.09727296	0.09567496			
	10	0.09477128	0.09377085	0.09106809	0.09720666	0.09702575			
	0.1	0.1095804	0.1027753	0.1056355	0.1045836	0.1104789			
	$\frac{1}{n^{0.2}}$	0.09481027	0.09343687	0.09703812	0.0966789	0.09964849			
	1	$\frac{1}{(n+5)^{0.8}}$	0.09799623	0.09448611	0.09128248	0.09492446	0.09514207		

The best case is:

case 133 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 10, \gamma = 0.5$ with fixed bandwidth $b_n = 1$

kernel function $K(x) = \frac{1}{1 + \alpha_1 x ^{\alpha_2}}$									
α_1	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
1	1	2	1	$\frac{1}{(n+5)^{0.5}}$	0.3070454	0.3068906	0.3052713	0.3048297	0.01207831
10					0.3162226	0.3175898	0.01470637	0.3185251	0.3193592
0.1					0.3120735	0.01419517	0.3107338	0.01337576	0.3145201
1	0.1	0.3149874			0.0102625	0.01038378	0.3151718	0.3180162	
	10	0.3138015			0.3144775	0.3119324	0.3141539	0.3179866	
10	1	0.5			0.09629609	0.09412796	0.09878587	0.0973144	0.09757993
0.1			0.09918275	0.09574896	0.09617135	0.09636164	0.0918699		
10	10		0.1044797	0.1014555	0.09926426	0.1026024	0.09995486		
			0.0948684	0.09043256	0.09575366	0.09641464	0.09650097		
	0.1		0.101807	0.102022	0.1004197	0.1020636	0.1007374		
	10	0.09532997	0.09173752	0.09862858	0.0989875	0.09509448			
10	10	0.1	0.1062357	0.1024435	0.102358	0.1059048	0.1063952		
		1	0.1185137	0.1212922	0.1148601	0.1225326	0.1214091		
		0.5	10						

			0.1		0.1094693	0.1108987	0.1093262	0.1075092	0.108967
			$\frac{1}{n^{0.2}}$		0.1097906	0.1107658	0.1109778	0.1064364	0.1097439
				$\frac{1}{(n+5)^{0.8}}$	0.09686088	0.09565276	0.09584571	0.09404183	0.09388677

The best case is

case 148 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 10, \gamma = 0.5$ with fixed bandwidth $b_n = 1$

kernel function $K(x) = \begin{cases} 0, & x \geq 2 * width \\ -1 * height, & width < x < 2 * width \\ 1 * height, & x \leq width \end{cases}$													
height	width	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run			
0.5	0.5	1	0.5	1	$\frac{1}{(n+5)^{0.5}}$	0.1096651	0.1084375	0.1067751	0.1127673	0.1088777			
		10				0.0987999	0.0980836	0.0997633	0.1016252	0.0965179			
		0.1				0.0983502	0.0958647	0.0936723	0.0953152	0.0938777			
		2				0.0952151	0.1007342	0.0924407	0.0971953	0.0967851			
		5				0.0995773	0.1026557	0.1013624	0.1004220	0.098975			
10	0.1249001	0.1207218	0.1206259	0.1231427		0.1196420							
0.1	0.5	0.1	0.5	1		0.0943379	0.0925746	0.0955971	0.0950350	0.0946926			
						2	0.0906348	0.0923965	0.0928345	0.0951008	0.0956070		
						8	0.0966672	0.0930716	0.0933293	0.0910570	0.0965149		
						15	0.100082	0.102526	0.1019249	0.1035333	0.1033918		
						0.1	0.0940607	0.0956745	0.0976864	0.0942801	0.0941309		
	2		0.1	0.5		0.5	$\frac{1}{n^{0.2}}$	0.1004776	0.1030413	0.1023623	0.1049767	0.0996596	
								10	0.0929315	0.0933425	0.0922779	0.0940506	0.0933517
								0.1	0.0942665	0.0954377	0.0946791	0.095681	0.0922989
								$\frac{1}{n^{0.2}}$	0.0930883	0.0931727	0.093848	0.091052	0.090727
					1			0.096987	0.095062	0.093127	0.093600	0.091170	

The best case is:

case 175 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.1, width = 2, C = 0.1, $\gamma = 0.5$ with decreasing

bandwidth $b_n = \frac{1}{n^{0.2}}$

$$\text{kernel function } K(x) = \begin{cases} 0, & |x| \geq 2 * \text{width} \text{ or } |x| \leq \text{width} \\ 1, & \text{width} < |x| < 2 * \text{width} \end{cases}$$

width	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run	
0.5	1	2	1	$\frac{1}{(n+5)^{0.5}}$	0.01560605	0.3208122	0.3201209	0.3172555	0.3161601	
	10				0.3043341	0.01413039	0.3057916	0.01335597	0.01378514	
	0.1				0.319614	0.3210132	0.3201003	0.01201751	0.3196954	
2	1	0.316767	0.01488253		0.3156092	0.01514421	0.3080952			
0.1		0.09400533	0.09445313		0.09332865	0.09327825	0.09355521			
0.5	1	0.5	1		0.09160858	0.09325567	0.09206486	0.09338538	0.09353589	
	10				0.0943911	0.09383944	0.09069657	0.0952836	0.09434861	
	0.1				0.102896	0.09876851	0.1006781	0.09787487	0.09916782	
2	1		0.09793323		0.09871597	0.09948697	0.1016156	0.09914065		
8			0.1399522		0.1428308	0.1440682	0.1472225	0.1409916		
15			0.09698082		0.1003973	0.09533199	0.09510083	0.09372085		
0.1			0.09981102		0.09970097	0.09808324	0.09874253	0.09807043		
0.5			1		10	0.1004022	0.09453277	0.1004871	0.09610355	0.09859633
					0.1	0.0927094	0.09423476	0.09581283	0.09348766	0.09494838
					$\frac{1}{n^{0.2}}$	0.09759395	0.09547936	0.09430047	0.09667705	0.09291843
1			$\frac{1}{(n+5)^{0.8}}$	0.09948617	0.09938801	0.1030033	0.1019863	0.101742		

The best case is:

case 182 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, C = 1, $\gamma = 0.5$ with fixed bandwidth $b_n = 1$

constant $\sigma(x) = C$				
First run	Second run	Third run	Fourth run	Fifth run
0.09767042	0.1011924	0.09713788	0.09842107	0.1022126

2.3.8 comparison of average jump distance

kernel function $K(x) = e^{-\frac{ x ^{\alpha_1}}{\alpha_2}}$										
α_1	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run	
1	1	2	1	$\frac{1}{(n+5)^{0.5}}$	0.2751228	0.2759929	0.2706779	1.680425	0.2709634	
10					0.2420872	0.2420623	1.300179	1.100248	1.137486	
0.1					0.7802203	0.8506236	0.75010	0.8316456	0.1633702	
1		0.5			10	14.88102	14.89564	14.8591	15.10428	14.77388
10						16.15489	15.7693	16.31433	16.00171	15.95296
0.1						17.58205	17.69769	17.8748	17.63134	17.75754
1						10	17.64668	17.55073	17.72917	17.68229
0.1	10		17.24616	17.43554		17.11712	17.62766	17.20509		
	10		17.65325	17.40023		17.13826	17.25142	17.47388		
	10	17.16678	17.39617	17.29623	17.32788	17.61989				
	0.1	14.17684	14.39708	14.29359	14.24914	14.03917				
	$\frac{1}{n^{0.2}}$	17.09166	17.4916	17.58568	17.48781	16.96503				
			$\frac{1}{(n+5)^{0.8}}$	17.29917	17.58498	17.3033	17.30672	17.27245		

The best case is:

case 133 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 10, \gamma = 0.5$ with fixed bandwidth $b_n = 1$

kernel function $K(x) = \frac{1}{1 + \alpha_1 x ^{\alpha_2}}$									
α_1	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
1	1	2	1	$\frac{1}{(n+5)^{0.5}}$	2.032223	2.016114	2.033322	2.244812	0.3014526
10					1.229918	1.441011	0.2134324	1.313225	1.163729
0.1					1.775863	0.2643402	1.454854	0.2695992	1.458424
1	0.1	1.453122			0.4300739	0.4270017	1.449158	1.260599	
	10	1.264062			1.348775	1.324255	1.389254	1.358456	
10	0.5	10			16.8956	17.15056	16.62733	16.56032	16.54765
0.1					16.91554	17.05386	17.0554	17.05604	17.23872
10					15.85114	16.04918	16.2265	16.07591	16.03785
					10	17.2243	17.46561	17.20456	17.48782
10	0.1	16.09596			15.91488	16.15975	15.87687	15.86291	
	10	0.1	17.01713	17.33785	16.88911	17.58669	17.21339		
		1	14.94124	14.47357	14.76298	14.378	14.43249		
		0.5	10	11.12058	11.09729	11.1061	11.01476	10.9672	

		0.1	13.53036	13.3978	13.39257	13.43201	13.33216
		$\frac{1}{n^{0.2}}$	13.75155	13.59613	13.75362	13.54406	13.55263
		$\frac{1}{(n+5)^{0.8}}$	17.50773	17.1296	16.98451	17.70879	17.26632

The best case is

case 148 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 10, \alpha_2 = 1, C = 10, \gamma = 0.5$ with fixed bandwidth $b_n = 1$

kernel function $K(x) = \begin{cases} 0, & x \geq 2 * width \\ -1 * height, & width < x < 2 * width \\ 1 * height, & x \leq width \end{cases}$												
height	width	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run		
0.5	0.5	1	0.5	1	$\frac{1}{(n+5)^{0.5}}$	13.26237	13.30066	13.43912	13.43278	13.29712		
		10				15.89375	16.29958	16.33701	16.20252	16.46537		
		0.1				17.25006	17.29043	17.44449	17.52067	17.25407		
		2				16.61506	16.81390	16.96739	17.08910	17.20643		
		5				15.34476	15.23875	14.98588	15.59716	14.76257		
10	12.40918	12.45344	12.24459	12.17052	12.15185							
0.1	0.5	0.1	0.1	1	$\frac{1}{(n+5)^{0.5}}$	17.56846	17.56847	17.56094	17.46663	17.58271		
						2	17.96944	18.08717	18.11135	17.80244	17.78677	
						8	17.80607	17.92915	17.32039	18.16933	17.84017	
						15	14.65539	14.81321	14.85105	15.0683	14.97829	
						0.1	16.80683	16.78677	16.69167	16.58419	16.67941	
	2	0.1	0.1	0.5	$\frac{1}{n^{0.2}}$	$\frac{1}{(n+5)^{0.8}}$	15.7515	15.63679	15.41598	15.38731	15.71839	
							10	18.04347	18.16659	17.67161	17.90958	17.73759
							0.1	17.56144	17.92892	17.91349	17.91258	17.97203
							$\frac{1}{n^{0.2}}$	17.79253	18.07391	17.8165	18.141	18.01603
							1	17.93693	17.97735	17.67513	17.42695	17.39284

The best case is :

case 173 $\eta_n = \frac{1}{(n+5)^{0.5}}$, height = 0.1, width = 2, C = 0.1, $\gamma = 0.5$ with fixed bandwidth

$b_n = 10$

$$\text{kernel function } K(x) = \begin{cases} 0, & |x| \geq 2 * \text{width} \text{ or } |x| \leq \text{width} \\ 1, & \text{width} < |x| < 2 * \text{width} \end{cases}$$

width	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run	
0.5	1	2	1	$\frac{1}{(n+5)^{0.5}}$	0.2160827	1.134826	1.111249	1.120923	1.140038	
	10				2.037578	0.2655736	2.010462	0.2639856	0.2614159	
	0.1				1.176037	1.131612	1.176397	0.3714259	1.21477	
2	1	1.329289	0.2200012		1.344635	0.2176641	1.326619			
0.1		17.5467	17.79094		18.01757	17.60527	17.49032			
0.5	1	0.5	1		17.93946	17.42754	17.92938	17.68764	17.78533	
	10				17.75638	17.64809	17.8715	17.66988	18.22428	
	0.1				15.48933	15.75263	15.99588	16.07236	16.07759	
2	1		16.3643		16.21187	16.19518	16.21535	16.28342		
8			7.740157		7.842474	7.7877	7.708015	7.644844		
15			16.73765		16.26973	16.97077	7.01989	16.78987		
0.1			16.32375		16.6559	16.6806	16.37162	16.43629		
0.5			1		10	15.59574	15.70382	15.66388	15.9781	15.87459
					0.1	17.38151	17.41642	17.40737	17.41414	17.80852
					$\frac{1}{n^{0.2}}$	16.799	16.79686	17.50548	16.96549	17.29666
1			$\frac{1}{(n+5)^{0.8}}$	5.57927	15.45931	15.21297	15.65399	15.44641		

The best case is:

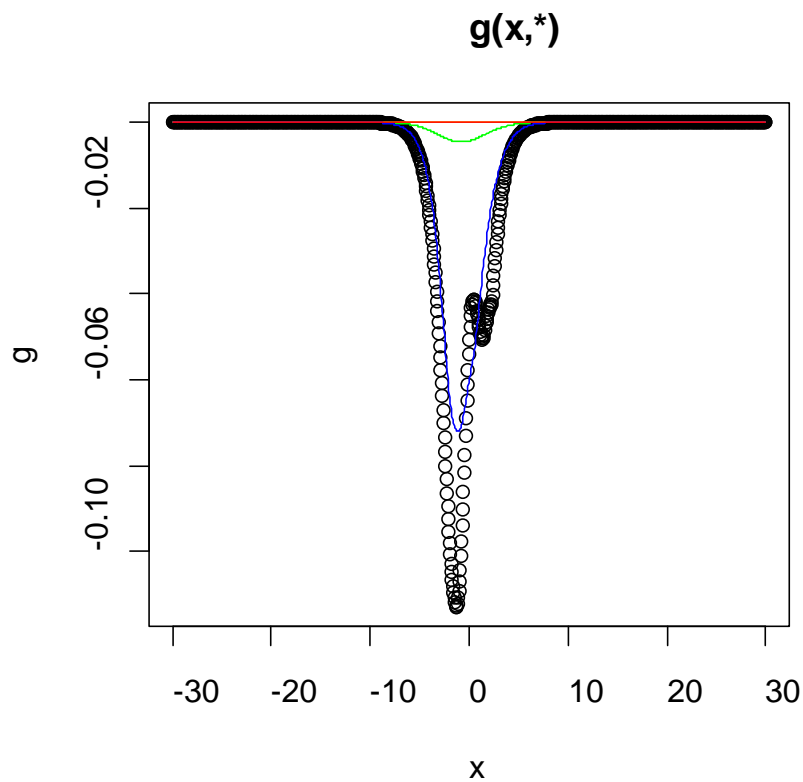
case 182 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 0.5, C = 1, $\gamma = 0.5$ with fixed bandwidth $b_n = 1$

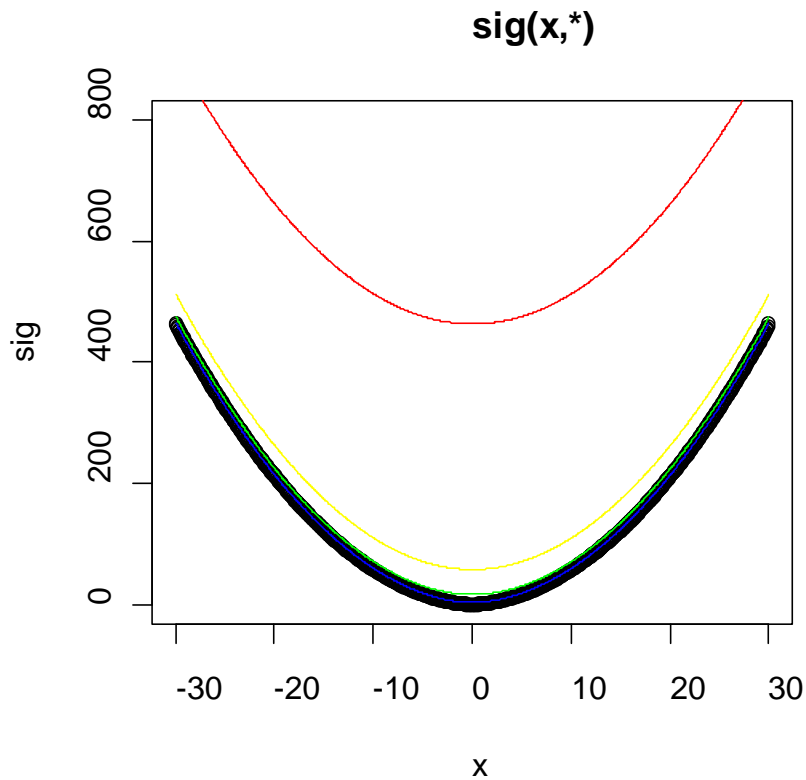
constant $\sigma(x) = C$				
First run	Second run	Third run	Fourth run	Fifth run
15.54288	15.35994	15.284	15.54276	15.54288

2.4 Example 4: normal distribution in R^2

2.4.1 kernel function $K(x) = e^{-\frac{|x|^{\alpha_1}}{\alpha_2}}$

2.4.1.1 case 194 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$





Without

approximation:

$\alpha(0.000000, 0.000000)$ is about 0.758800

$\alpha(0.000000, 2.000000)$ is about 0.138100

$\alpha(5.000000, 5.000000)$ is about 0.024000

$\alpha(2.000000, 10.000000)$ is about 0.015000

$\alpha(10.000000, 10.000000)$ is about 0.007900

$\alpha(20.000000, 50.000000)$ is about 0.000700

$\alpha(50.000000, 50.000000)$ is about 0.000200

it takes 296.759000 seconds to run the adaptation algorithm

it takes 10001.982000 seconds to plot g and sigma

it takes 3674.517000 seconds to generate the first Markov Chain

it takes 3806.229000 seconds to generate the second Markov Chain

it takes 3813.156000 seconds to generate the third Markov Chain

it takes 3638.899000 seconds to generate the fourth Markov Chain

it takes 3640.485000 seconds to generate the fifth Markov Chain

it takes 2712.386000 seconds to test the local acceptance

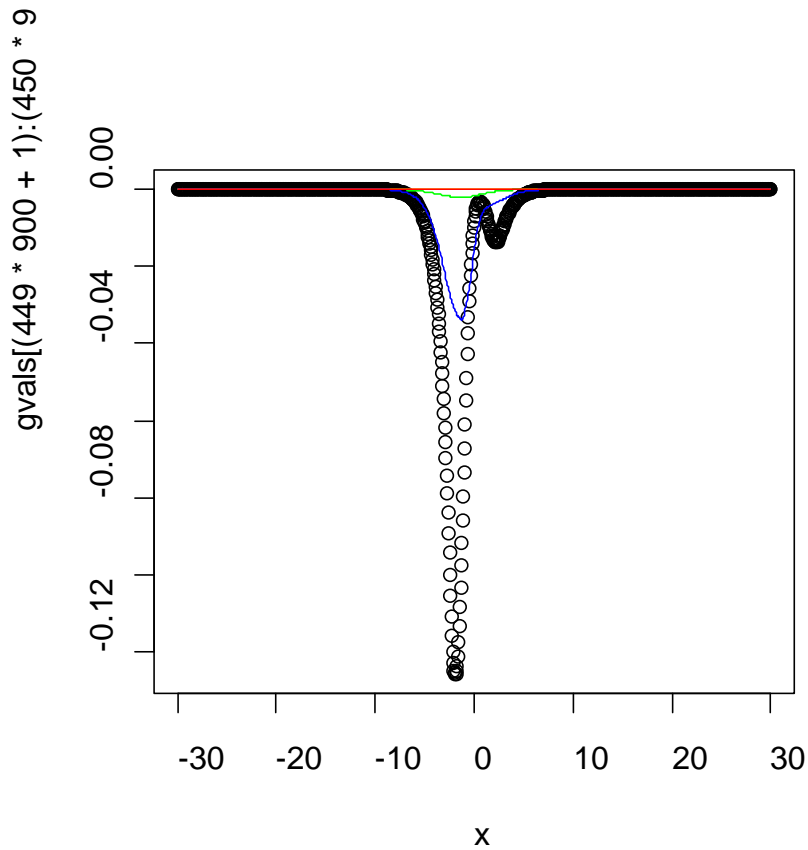


```

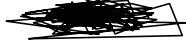
> source("xlist3");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 17.56787
[1] 0.01787614
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.4192436
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 15.05131
[1] 0.01619204
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.4235149
> source("xlist4");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 16.71129
[1] 0.01723975
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.4241305
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 16.05023
[1] 0.0166278
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.4103297
> source("xlist5");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 15.7971
[1] 0.01652789
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.4156999
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 15.84213
[1] 0.01660798
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.4247686

```

With approximation:



alpha(0.000000,0.000000) is about 0.677500
 alpha(0.000000,2.000000) is about 0.137900
 alpha(5.000000,5.000000) is about 0.025100
 alpha(2.000000,10.000000) is about 0.011400
 alpha(10.000000,10.000000) is about 0.007900
 alpha(20.000000,50.000000) is about 0.000900
 alpha(50.000000,50.000000) is about 0.000400
 it takes 310.314000 seconds to run the adaptation algorithm
 it takes 123.634000 seconds to compute g and sigma
 it takes 9939.710000 seconds to plot g and sigma
 it takes 512.742000 seconds to generate the first Markov Chain
 it takes 471.932000 seconds to generate the second Markov Chain
 it takes 496.096000 seconds to generate the third Markov Chain
 it takes 514.006000 seconds to generate the fourth Markov Chain
 it takes 468.624000 seconds to generate the fifth Markov Chain
 it takes 2030.625000 seconds to test the local acceptance



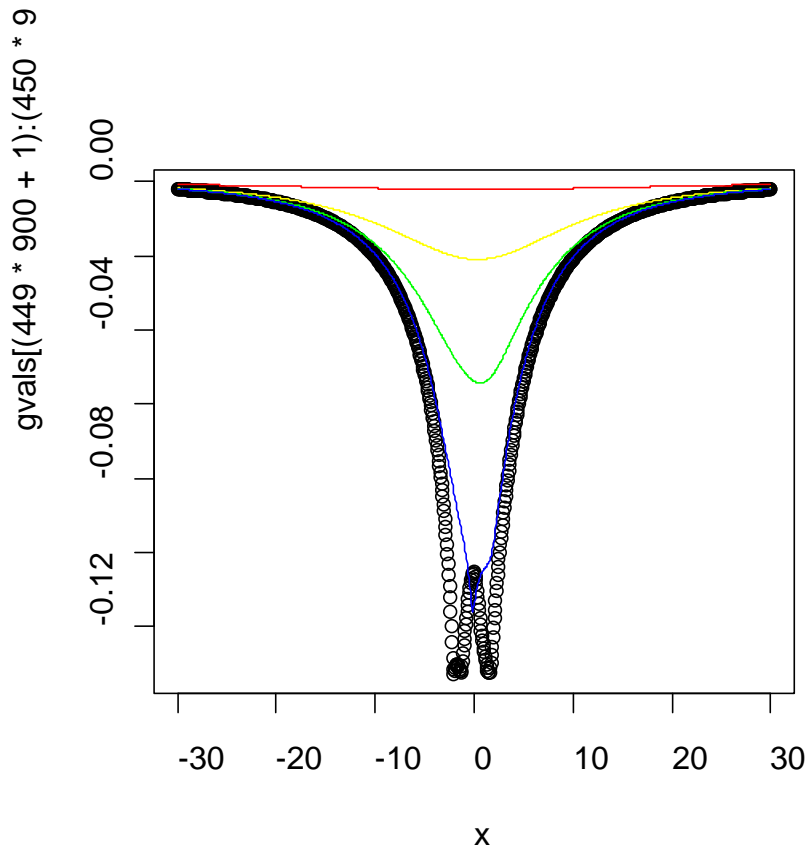

```

> source("xlist3");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 17.83584
[1] 0.01795715
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.37771
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 18.94229
[1] 0.01861971
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.3819818
> source("xlist4");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 19.21391
[1] 0.0187782
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.3715975
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 17.64572
[1] 0.01804834
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.382282
> source("xlist5");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 18.30911
[1] 0.01796832
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.3769988
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 18.34555
[1] 0.01780736
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.3663442

```

2.4.1.2 case 195 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.5, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth

$$b_n = 1$$



alpha(0.000000,0.000000) is about 0.743500
 alpha(0.000000,2.000000) is about 0.140300
 alpha(5.000000,5.000000) is about 0.025400
 alpha(2.000000,10.000000) is about 0.013000
 alpha(10.000000,10.000000) is about 0.008200
 alpha(20.000000,50.000000) is about 0.000200
 alpha(50.000000,50.000000) is about 0.000400
 it takes 697.040000 seconds to run the adaptation algorithm
 it takes 278.120000 seconds to compute g and sigma
 it takes 1394.863520 seconds to plot g and sigma
 it takes 2056.040000 seconds to generate the first Markov Chain
 it takes 2026.420000 seconds to generate the second Markov Chain
 it takes 2127.810000 seconds to generate the third Markov Chain
 it takes 2047.300000 seconds to generate the fourth Markov Chain
 it takes 2019.330000 seconds to generate the fifth Markov Chain
 it takes 775.512704 seconds to test the local acceptance



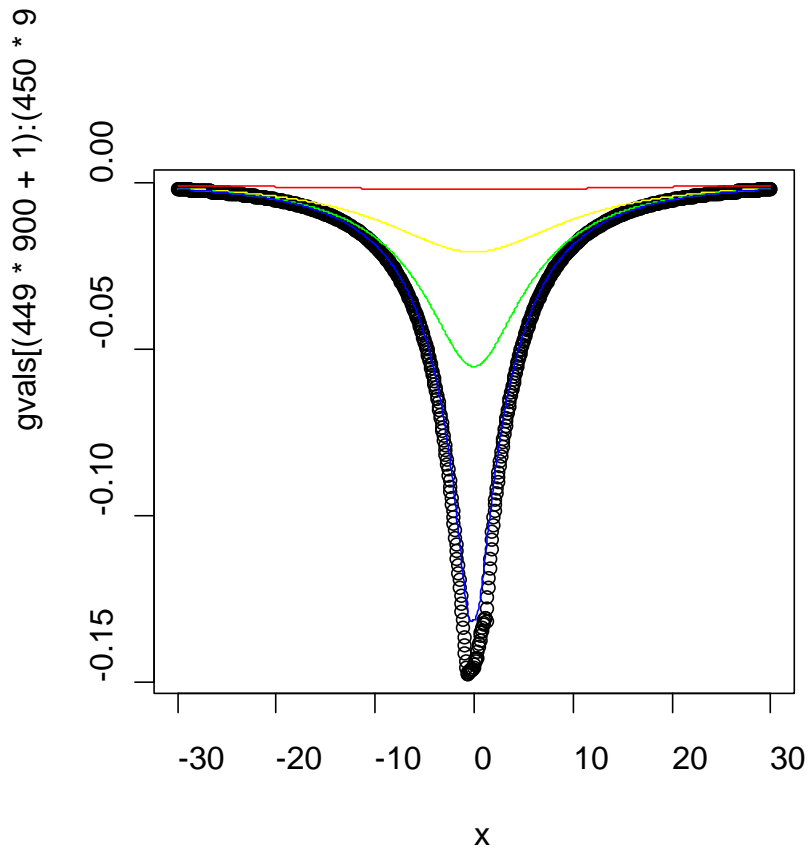
```

> source("xlist3");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 16.17414
[1] 0.01657182
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.3948022
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 17.14889
[1] 0.01751794
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.3982419
> source("xlist4");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 18.61931
[1] 0.01846755
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.3851333
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 16.61003
[1] 0.01718756
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.3953794
> source("xlist5");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 14.81985
[1] 0.01588587
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.4055987
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 15.54527
[1] 0.01654854
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.4082785

```

2.4.1.3 case 196 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 0.5, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$$b_n = 1$$



alpha(0.000000,0.000000) is about 0.215700
 alpha(0.000000,2.000000) is about 0.285000
 alpha(5.000000,5.000000) is about 0.328900
 alpha(2.000000,10.000000) is about 0.335800
 alpha(10.000000,10.000000) is about 0.319200
 alpha(20.000000,50.000000) is about 0.157600
 alpha(50.000000,50.000000) is about 0.124300
 it takes 308.418000 seconds to run the adaptation algorithm
 it takes 120.640000 seconds to compute g and sigma
 it takes 9777.420000 seconds to plot g and sigma
 it takes 233.015000 seconds to generate the first Markov Chain
 it takes 236.232000 seconds to generate the second Markov Chain
 it takes 230.846000 seconds to generate the third Markov Chain
 it takes 233.644000 seconds to generate the fourth Markov Chain
 it takes 234.809000 seconds to generate the fifth Markov Chain
 it takes 1859.186000 seconds to test the local acceptance



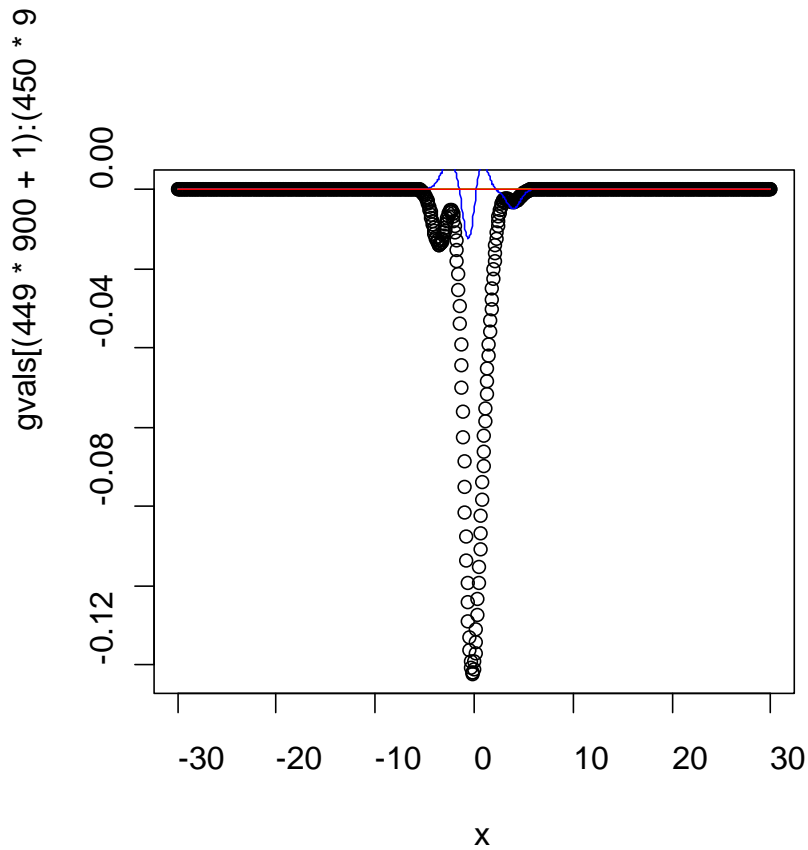
```

> source("xlist3");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 8.026836
[1] 0.009977178
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.4939001
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 8.258773
[1] 0.01015497
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.4959621
> source("xlist4");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 8.63622
[1] 0.01044986
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.4918952
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 8.127733
[1] 0.01004813
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.4806261
> source("xlist5");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 7.844774
[1] 0.009936305
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.491927
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 8.082055
[1] 0.01011846
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.4961528
>

```

2.4.1.4 case 197 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 2, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$$b_n = 1$$



$\alpha(0.000000,0.000000)$ is about 0.213600
 $\alpha(0.000000,2.000000)$ is about 0.263100
 $\alpha(5.000000,5.000000)$ is about 0.324800
 $\alpha(2.000000,10.000000)$ is about 0.329200
 $\alpha(10.000000,10.000000)$ is about 0.324500
 $\alpha(20.000000,50.000000)$ is about 0.155400
 $\alpha(50.000000,50.000000)$ is about 0.121100
 it takes 692.970000 seconds to run the adaptation algorithm
 it takes 275.750000 seconds to compute g and sigma
 it takes -1745.982960 seconds to plot g and sigma
 it takes 1540.860000 seconds to generate the first Markov Chain
 it takes 1553.610000 seconds to generate the second Markov Chain
 it takes 1544.950000 seconds to generate the third Markov Chain
 it takes 1550.080000 seconds to generate the fourth Markov Chain
 it takes 1543.870000 seconds to generate the fifth Markov Chain
 it takes 1162.082704 seconds to test the local acceptance



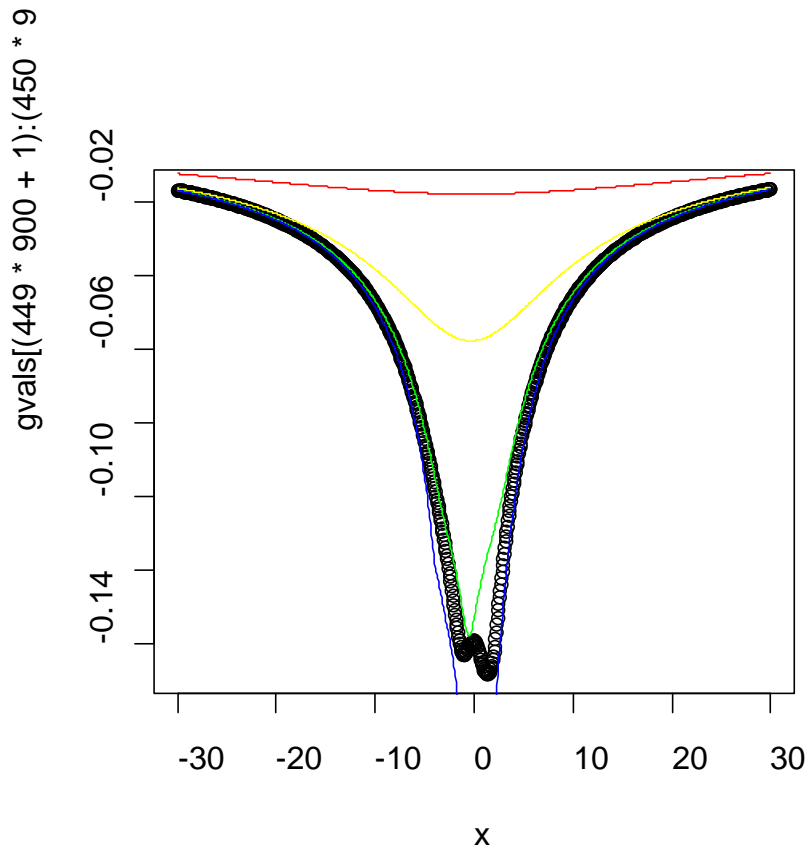
```

> source("xlist3");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 8.949513
[1] 0.01073386
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.4865919
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 8.598656
[1] 0.01047538
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.4712849
> source("xlist4");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 8.588107
[1] 0.01039507
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.4599503
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 8.953894
[1] 0.01072307
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.4720166
> source("xlist5");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 8.759423
[1] 0.01047106
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.4650114
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 7.537465
[1] 0.009703281
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.480265
>

```

2.4.2 kernel function $K(x) = \frac{1}{1 + \alpha_1 |x|^{\alpha_2}}$

2.4.2.1 case 198 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 1, \gamma = 2$ with fixed bandwidth $b_n = 1$



alpha(0.000000,0.000000) is about 0.812400
 alpha(0.000000,2.000000) is about 0.183100
 alpha(5.000000,5.000000) is about 0.032400
 alpha(2.000000,10.000000) is about 0.016800
 alpha(10.000000,10.000000) is about 0.010700
 alpha(20.000000,50.000000) is about 0.000800
 alpha(50.000000,50.000000) is about 0.000600
 it takes 265.875000 seconds to run the adaptation algorithm
 it takes 104.690000 seconds to compute g and sigma
 it takes 8658.581000 seconds to plot g and sigma
 it takes 358.066000 seconds to generate the first Markov Chain
 it takes 358.640000 seconds to generate the second Markov Chain
 it takes 385.815000 seconds to generate the third Markov Chain
 it takes 362.398000 seconds to generate the fourth Markov Chain
 it takes 385.542000 seconds to generate the fifth Markov Chain
 it takes 1678.442000 seconds to test the local acceptance

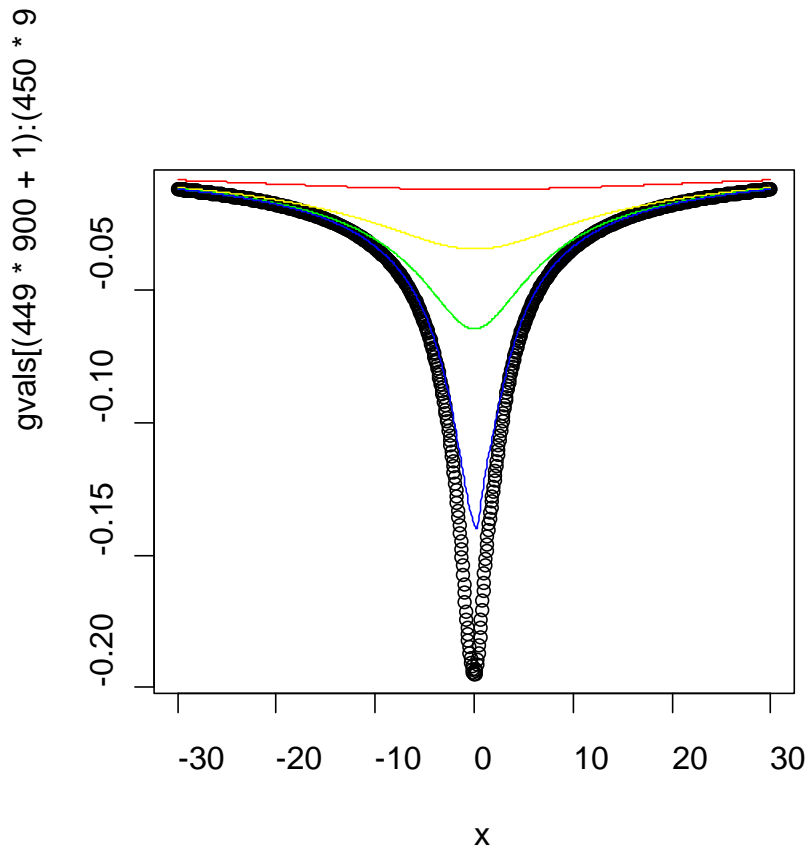

```

> source("xlist3");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 12.73097
[1] 0.01494266
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.4921363
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 13.90548
[1] 0.01589283
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.5000742
> source("xlist4");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 11.93283
[1] 0.01434084
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.4873498
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 14.43801
[1] 0.01607662
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.481112
> source("xlist5");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 12.03846
[1] 0.01445098
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.4984666
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 13.71947
[1] 0.01538246
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.4771416

```

2.4.2.2 case 199 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 1$ with fixed bandwidth

$$b_n = 1$$



alpha(0.000000,0.000000) is about 0.180900
 alpha(0.000000,2.000000) is about 0.282200
 alpha(5.000000,5.000000) is about 0.399500
 alpha(2.000000,10.000000) is about 0.409400
 alpha(10.000000,10.000000) is about 0.430200
 alpha(20.000000,50.000000) is about 0.451200
 alpha(50.000000,50.000000) is about 0.446700
 it takes 269.569000 seconds to run the adaptation algorithm
 it takes 106.705000 seconds to compute g and sigma
 it takes 8641.609000 seconds to plot g and sigma
 it takes 234.730000 seconds to generate the first Markov Chain
 it takes 230.138000 seconds to generate the second Markov Chain
 it takes 232.516000 seconds to generate the third Markov Chain
 it takes 234.278000 seconds to generate the fourth Markov Chain
 it takes 233.943000 seconds to generate the fifth Markov Chain
 it takes 1645.604000 seconds to test the local acceptance



```

> source("xlist3");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 7.61042
[1] 0.009621487
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.4751286
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 8.295657
[1] 0.009891014
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.4542424
> source("xlist4");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 8.137364
[1] 0.009998282
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.4802455
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 8.042155
[1] 0.009880959
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.4680676
> source("xlist5");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 8.286704
[1] 0.009931457
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.4713538
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 8.348549
[1] 0.01007295

```

2.4.2.3 case 200 $\eta_n = \frac{1}{(n+5)^{0.8}}$, $\alpha_1 = 1, \alpha_2 = 1, C = 0.1, \gamma = 2$ with fixed bandwidth

$$b_n = 10$$



```

> source("xlist3");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 8.845103
[1] 0.0103805
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.45205
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 8.806404
[1] 0.0105059
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.4572161
> source("xlist4");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 9.134059
[1] 0.01065294
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.4562965
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 8.585028
[1] 0.0103154
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.4593464
> source("xlist5");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 8.98815
[1] 0.01067445
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.4683815
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 8.692522
[1] 0.01038471
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.4767837

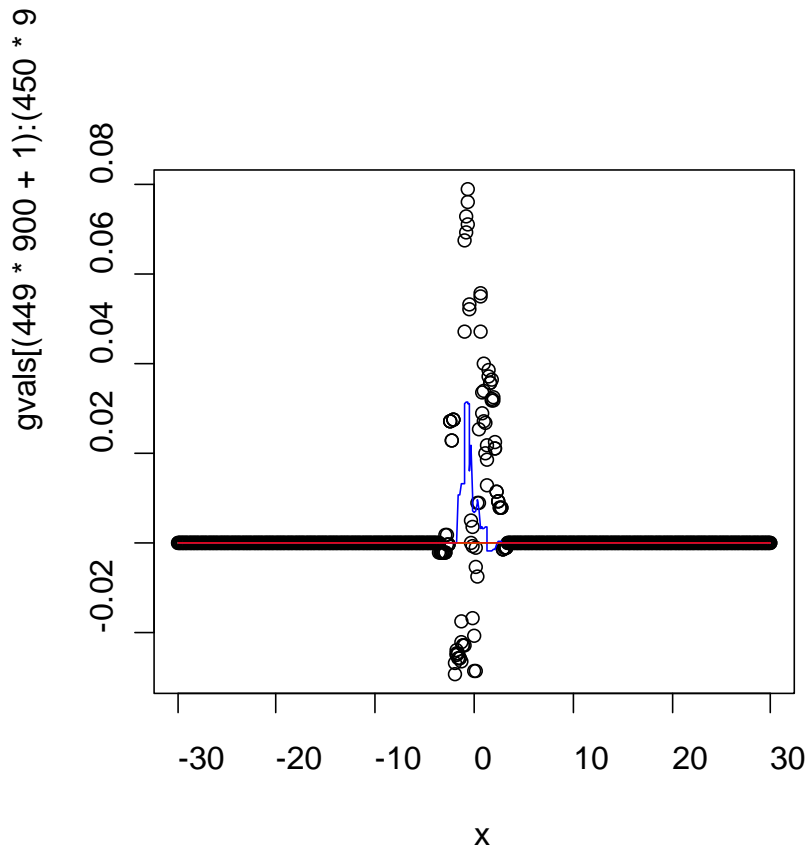
```

2.4.3 kernel function

$$K(x) = \begin{cases} 0, & |x| \geq 2 * width \\ -1 * height, & width < |x| < 2 * width \\ 1 * height, & |x| \leq width \end{cases}$$

2.4.3.1 case 201 $\eta_n = \frac{1}{(n+5)^{0.5}}$, $height = 0.5$, $width = 0.5$, $C = 0.01$, $\gamma = 10$ with fixed

bandwidth $b_n = 1$



alpha(0.000000,0.000000) is about 0.172500
 alpha(0.000000,0.000000) is about 0.168700
 alpha(5.000000,5.000000) is about 0.401600
 alpha(10.000000,10.000000) is about 0.395500
 alpha(20.000000,50.000000) is about 0.054200
 it takes 205.869000 seconds to run the adaptation algorithm
 it takes 79.808000 seconds to compute g and sigma
 it takes -1.#QNAN0 seconds to plot g and sigma
 it takes 198.873000 seconds to generate the first Markov Chain
 it takes 204.658000 seconds to generate the second Markov Chain
 it takes 202.383000 seconds to generate the third Markov Chain
 it takes 199.687000 seconds to generate the fourth Markov Chain
 it takes 198.928000 seconds to generate the fifth Markov Chain
 it takes 756.626000 seconds to test the local acceptance



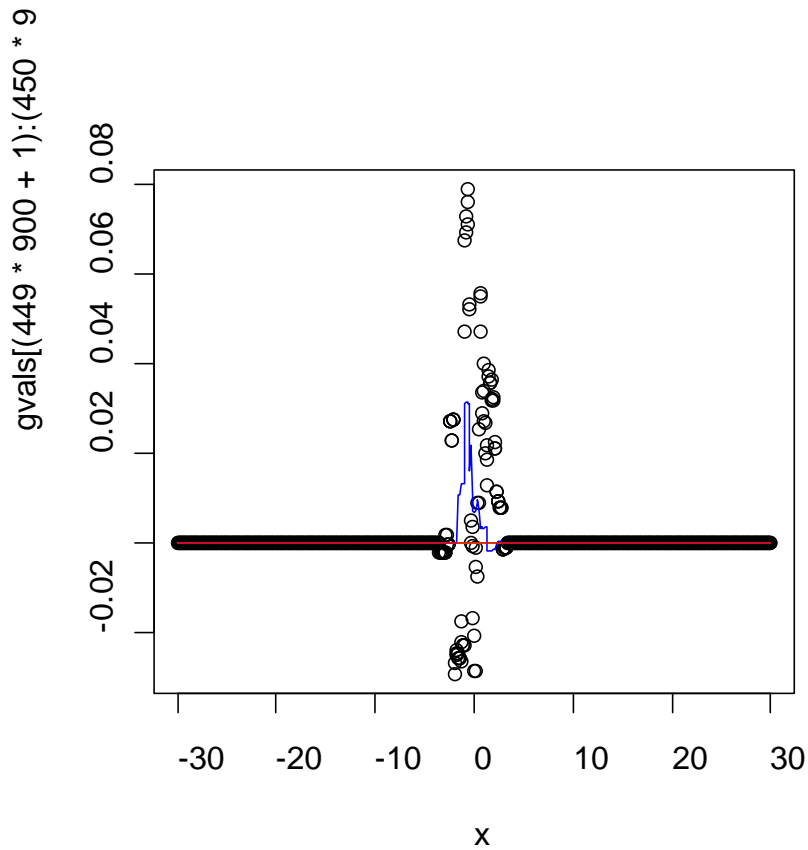
```

> source("xlist3");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 8.50804
[1] 0.009935555
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.4494896
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 8.373991
[1] 0.00991694
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.4568538
> source("xlist4");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 8.242958
[1] 0.009808818
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.4652114
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 8.407656
[1] 0.00984394
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.4524555
> source("xlist5");plot(xlist1[(B+1):M],xlist2[(B+1):M],type="l");
> varfact(xlist1[(B+1):M]);sd(xlist1[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist1[(B+1):M]) );
[1] 8.01933
[1] 0.009759364
> val = 0;for(i in (B+1):M ) val = val +(xlist1[i]-xlist1[i-1])^2;(val/(M-B));
[1] 0.4576324
> varfact(xlist2[(B+1):M]);sd(xlist2[(B+1):M]) / sqrt(M-B) * sqrt( varfact(xlist2[(B+1):M]) );
[1] 8.055316
[1] 0.009937325
> val = 0;for(i in (B+1):M ) val = val +(xlist2[i]-xlist2[i-1])^2;(val/(M-B));
[1] 0.4613729

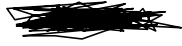
```

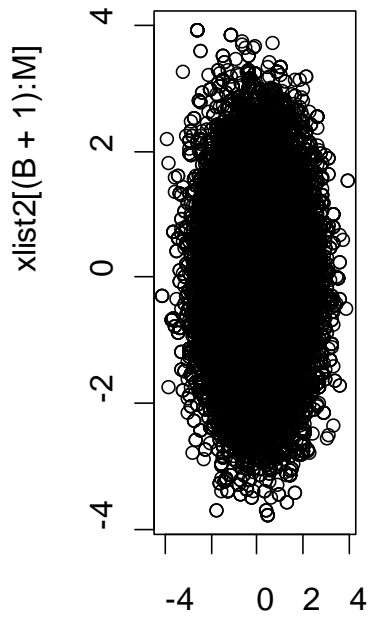
2.4.4 kernel function
$$K(x) = \begin{cases} 0, & |x| \geq 2 * width \text{ or } |x| \leq width \\ 1, & width < |x| < 2 * width \end{cases}$$

2.4.4.1 case 202 $\eta_n = \frac{1}{(n+5)^{0.5}}$, width = 5, C = 0.01, $\gamma = 2$ with fixed bandwidth $b_n = 1$



alpha(0.000000,0.000000) is about 0.127900
 alpha(0.000000,2.000000) is about 0.276100
 alpha(5.000000,5.000000) is about 0.466900
 alpha(2.000000,10.000000) is about 0.458900
 alpha(10.000000,10.000000) is about 0.461400
 alpha(20.000000,50.000000) is about 0.471300
 alpha(50.000000,50.000000) is about 0.475300
 it takes 203.986000 seconds to run the adaptation algorithm
 it takes 79.703000 seconds to compute g and sigma
 it takes -1.#QNAN0 seconds to plot g and sigma
 it takes 236.103000 seconds to generate the first Markov Chain
 it takes 234.442000 seconds to generate the second Markov Chain
 it takes 234.676000 seconds to generate the third Markov Chain
 it takes 236.654000 seconds to generate the fourth Markov Chain
 it takes 237.002000 seconds to generate the fifth Markov Chain
 it takes 1278.837000 seconds to test the local acceptance





$xlist1[(B + 1):M]$



acceptance rate = 0.23388
varfact is about 8.07853 and 8.904434
standard error is about 0.00939504 and 0.009958031
average squared jump distance is about 0.4340354 and 0.4327815
> source("R1 sigma=C")
ran Metropolis algorithm for 1e+05 iterations, with burn-in 10000
acceptance rate = 0.23235
varfact is about 8.492082 and 8.658637
standard error is about 0.009631347 and 0.009772716
average squared jump distance is about 0.4279432 and 0.4182256

2.4.6 varfact comparison

Kernel function : $K(x) = e^{-\frac{ x ^{\alpha_1}}{\alpha_2}}$									
α_1	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
0.5	0.1	2	1	$\frac{1}{(n+5)^{0.5}}$	8.011433	8.120745	8.026836	8.63622	7.844774
					8.390189	8.684449	8.258773	8.127733	8.08205

Kernel function : $K(x) = \frac{1}{1 + \alpha_1 x ^{\alpha_2}}$									
α_1	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
1	0.1	1	1	$\frac{1}{(n+5)^{0.5}}$	9.01875	8.05305	7.61042	8.137364	8.28670
					7.950148	8.35461	8.295657	8.042155	8.348549

Kernel function : $K(x) = \begin{cases} 0, & x \geq 2 * width \\ -1 * height, & width < x < 2 * width \\ 1 * height, & x \leq width \end{cases}$										
height	width	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
0.5	0.5	0.01	10	1	$\frac{1}{(n+5)^{0.5}}$	7.741678	7.79554	8.50804	8.24295	8.0193
						8.519492	7.76981	8.373991	8.407656	8.05531

Kernel function : $K(x) = \begin{cases} 0, & x \geq 2 * width \text{ or } x \leq width \\ 1, & width < x < 2 * width \end{cases}$									
width	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
5	0.01	2	1	$\frac{1}{(n+5)^{0.5}}$	9.507272	8.887635	8.88124	8.759379	8.603718
					9.231252	8.916839	9.160737	9.014931	9.049856

constant $\sigma(x) = C$				
8.584404	8.331632	8.68917	8.07853	8.492082
8.08258	8.4440	8.334455	8.904434	8.6586

2.4.7 variance

Kernel function : $K(x) = e^{-\frac{ x ^{\alpha_1}}{\alpha_2}}$									
α_1	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
0.5	0.1	2	1	$\frac{1}{(n+5)^{0.5}}$	0.009964	0.010117	0.009977	0.010449	0.009936
					78	33	178	86	305
					0.010343	0.010591	0.010154	0.010048	0.010118
					23	26	97	13	46

Kernel function : $K(x) = \frac{1}{1 + \alpha_1 x ^{\alpha_2}}$									
α_1	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
1	0.1	1	1	$\frac{1}{(n+5)^{0.5}}$	0.010531	0.009726	0.009621	0.009998	0.009931
					37	586	487	282	45
					0.009772	0.009948	0.009891	0.009880	0.010072
					318	752	014	959	95

Kernel function : $K(x) = \begin{cases} 0, & x \geq 2 * width \\ -1 * height, & width < x < 2 * width \\ 1 * height, & x \leq width \end{cases}$										
height	width	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
0.5	0.5	0.01	10	1	$\frac{1}{(n+5)^{0.5}}$	0.009485	0.009529	0.009935	0.009808	0.009759
						893	391	555	818	364
						0.010009	0.009559	0.009916	0.009843	0.009937
						65	542	94	94	325

Kernel function : $K(x) = \begin{cases} 0, & x \geq 2 * width \text{ or } x \leq width \\ 1, & width < x < 2 * width \end{cases}$									
width	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
5	0.01	2	1	$\frac{1}{(n+5)^{0.5}}$	0.010313	0.009982	0.010075	0.009845	0.009871
					62	451	45	031	89
					0.010103	0.010162	0.010063	0.010136	0.010109
					7	46	09	37	16

constant $\sigma(x) = C$				
0.00972953	0.0097068	0.009780478	0.00939504 an	0.009631347
0.0094686	0.009739506	0.00954663	0.009958031	0.009772716

2.4.8 comparison of average squared jump distance

Kernel function : $K(x) = e^{-\frac{ x ^{\alpha_1}}{\alpha_2}}$									
α_1	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
0.5	0.1	2	1	$\frac{1}{(n+5)^{0.5}}$	0.506856	0.504129	0.493900	0.491895	0.491927
					0.506880	0.50175	0.495962	0.480626	0.496152

Kernel function : $K(x) = \frac{1}{1 + \alpha_1 x ^{\alpha_2}}$									
α_1	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
1	0.1	1	1	$\frac{1}{(n+5)^{0.5}}$	0.458961	0.461018	0.4751	0.480245	0.47135
					0.466943	0.467047	0.4542	0.4680	0.45683

Kernel function : $K(x) = \begin{cases} 0, & x \geq 2 * width \\ -1 * height, & width < x < 2 * width \\ 1 * height, & x \leq width \end{cases}$										
height	width	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
0.5	0.5	0.01	10	1	$\frac{1}{(n+5)^{0.5}}$	0.463001	0.46015	0.449489	0.465211	0.457632
						0.461200	0.465179	0.456853	0.452455	0.461372

Kernel function : $K(x) = \begin{cases} 0, & x \geq 2 * width \text{ or } x \leq width \\ 1, & width < x < 2 * width \end{cases}$									
width	C	γ	b_n	η_n	First run	Second run	Third run	Fourth run	Fifth run
5	0.01	2	1	$\frac{1}{(n+5)^{0.5}}$	0.394871	0.406117	0.404594	0.396869	0.414291
					0.40248	0.421151	0.404090	0.40975	0.413094

constant $\sigma(x) = C$				
0.4365735	0.4408152	0.421703	0.4340354	0.4279432
0.4396845	0.4289132	0.4226133	0.4327815	0.4182256